

Field-level inference and new observables for the next era of galaxy surveys

or why I am excited about large-scale structure cosmology

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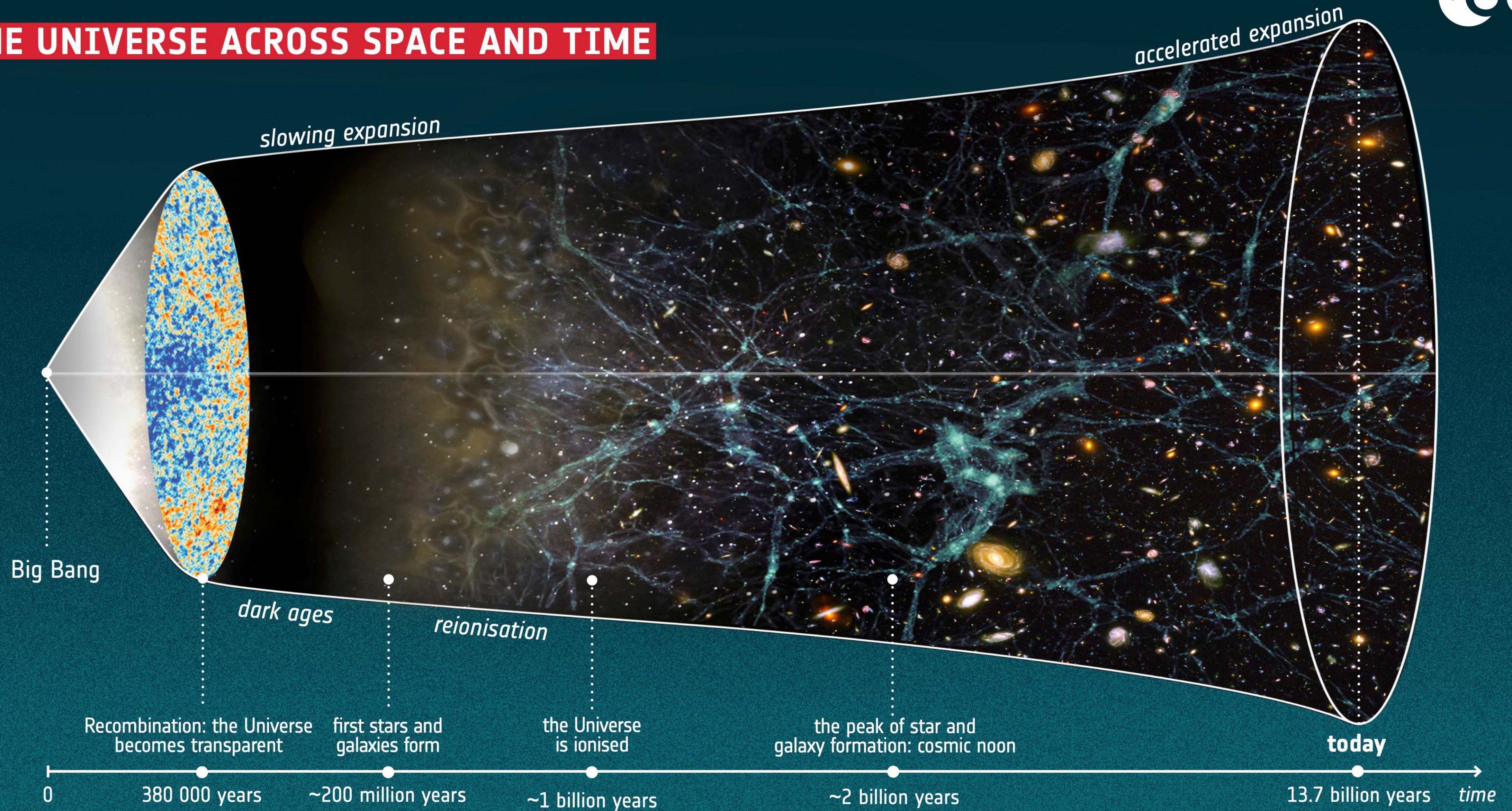


A visualization of the cosmic web, showing a complex network of dark matter filaments and galaxy clusters. The structure is rendered in shades of blue and white against a black background, with a prominent diagonal filament running from the top left towards the bottom right.

Why do we do cosmology (from LSS)?

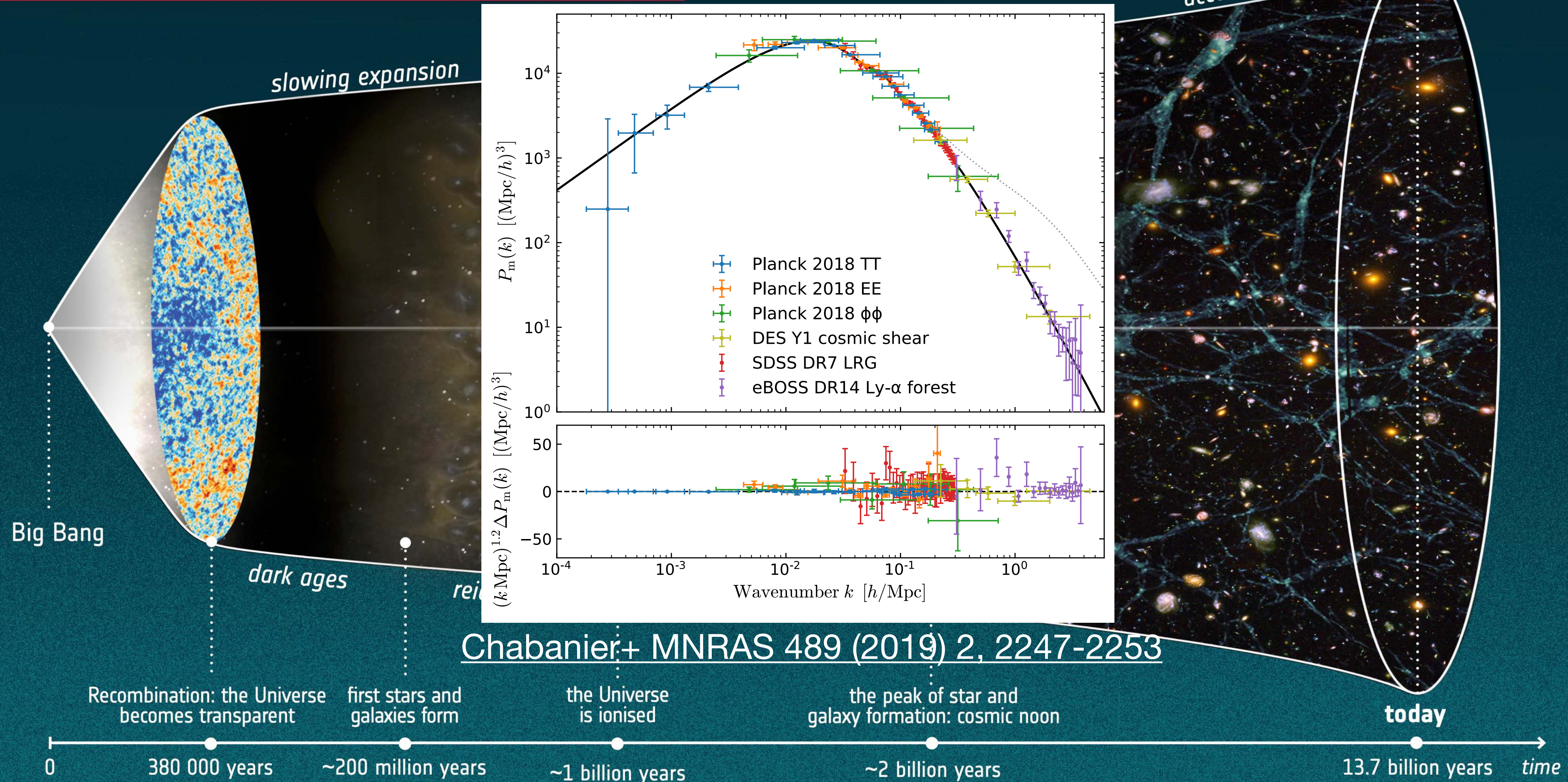
Credit: Dark Energy Spectroscopic Instrument

THE UNIVERSE ACROSS SPACE AND TIME



Linear matter power spectrum in Λ CDM

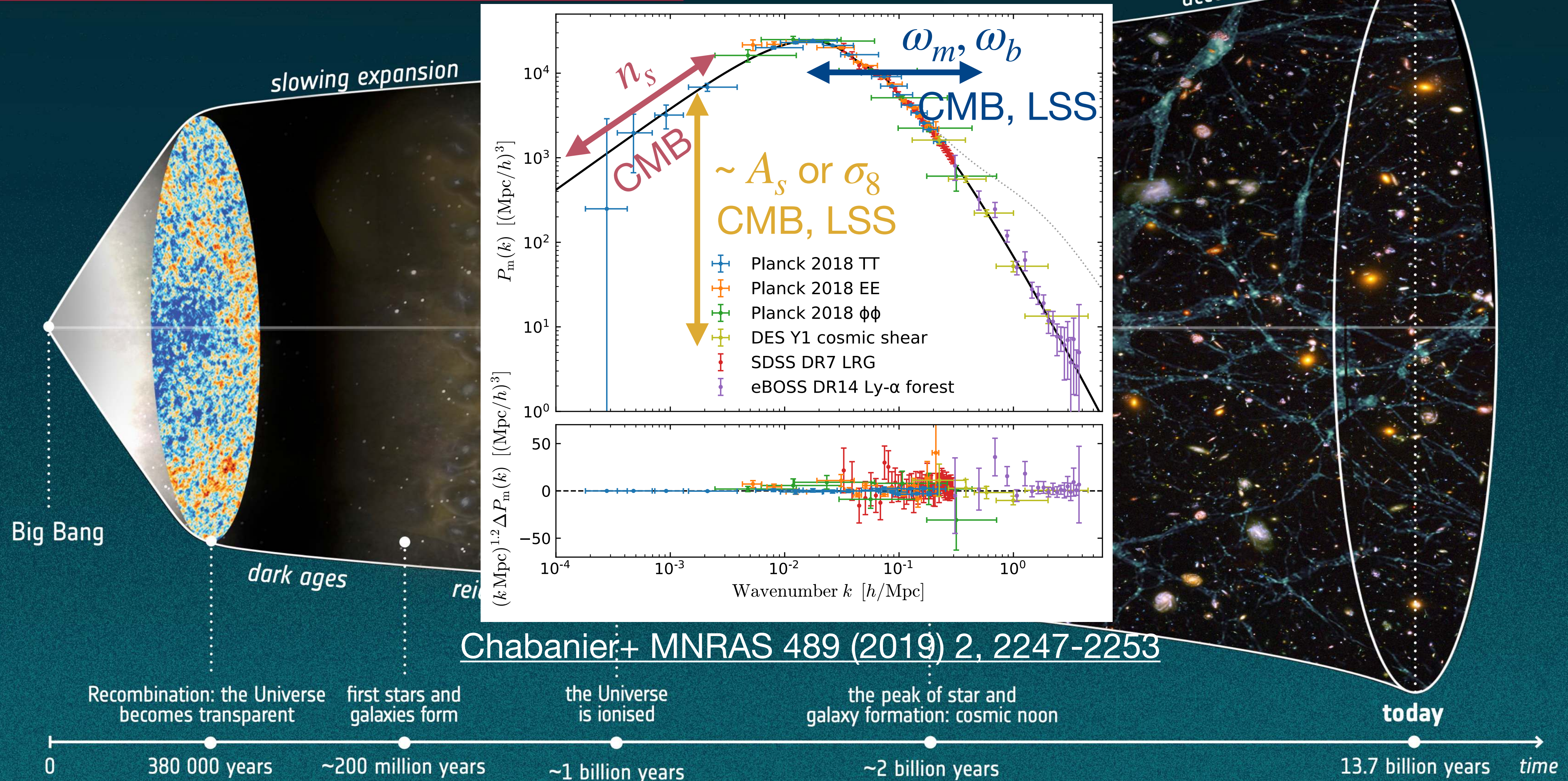
THE UNIVERSE ACROSS SPACE AND TIME



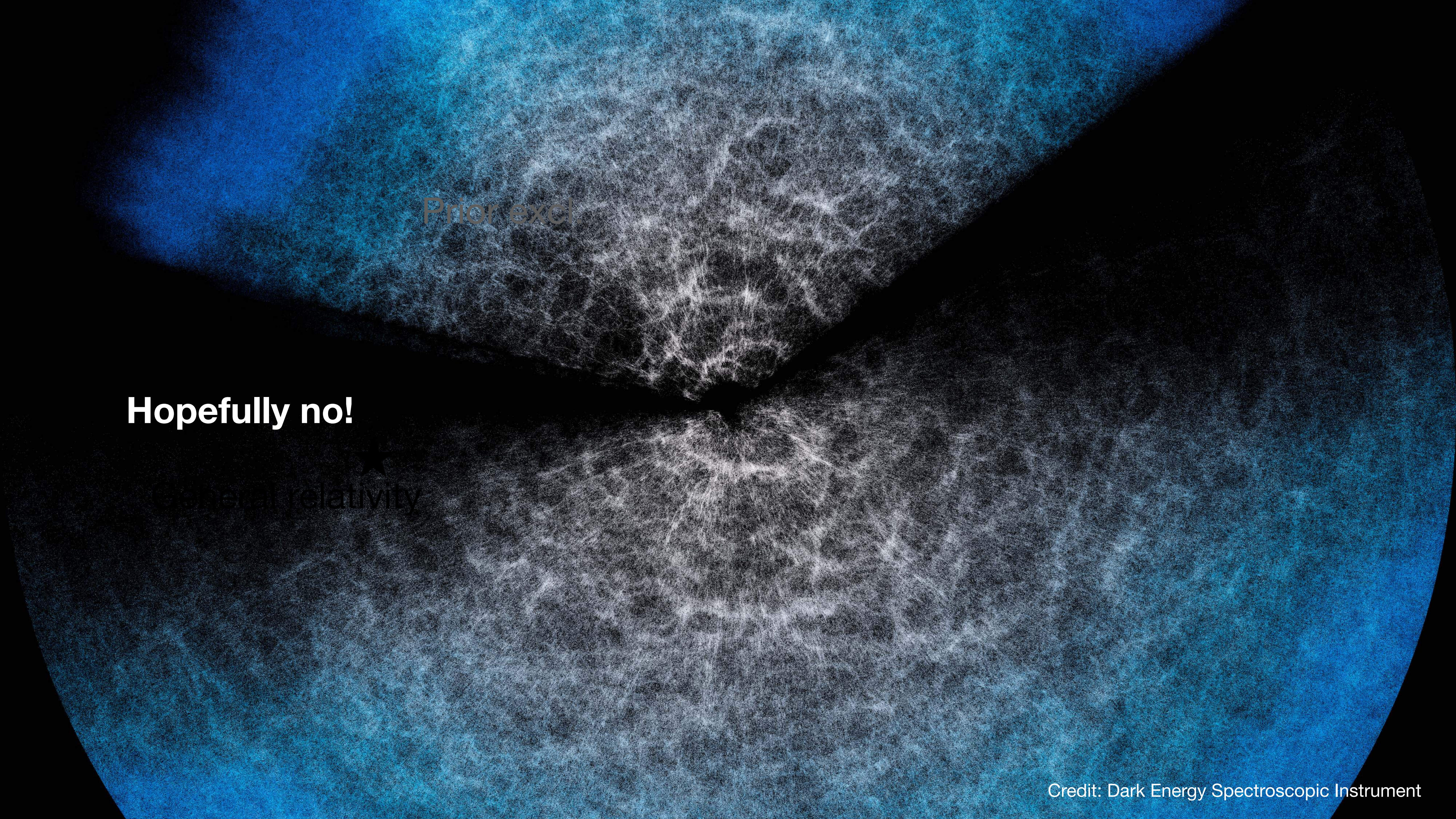
Cosmology from LSS aims to find the model that describes both CMB and LSS

Linear matter power spectrum in Λ CDM

THE UNIVERSE ACROSS SPACE AND TIME



The standard model Λ CDM is boringly robust. Is it the end of cosmology (from LSS)?

A visualization of the cosmic web, showing a dense network of filaments and clusters of galaxies. The background is a deep blue, and the filaments are depicted as bright, glowing structures. A dark, irregular shape is overlaid on the left side, representing a region of interest or a specific model.

Prior excl.

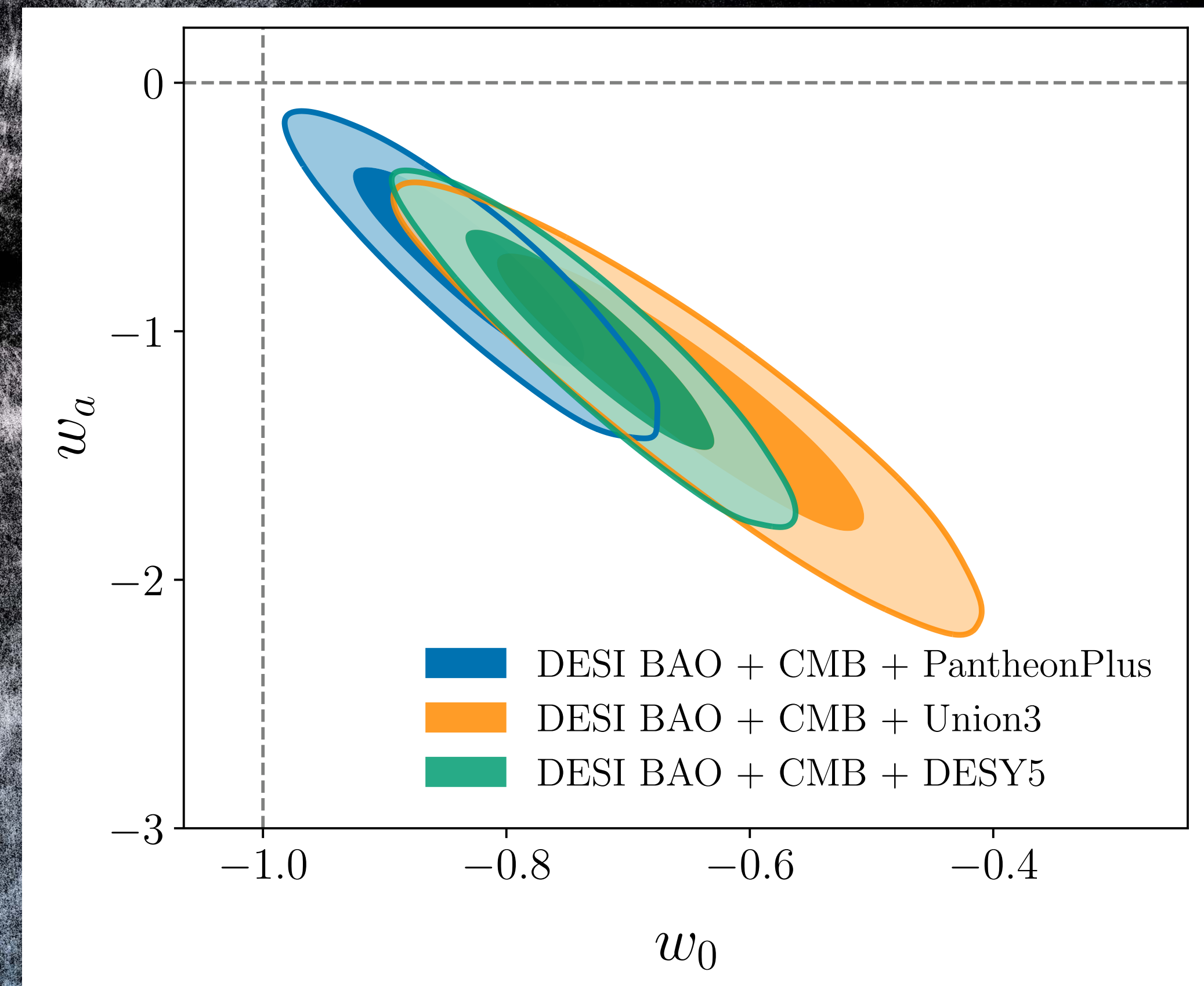
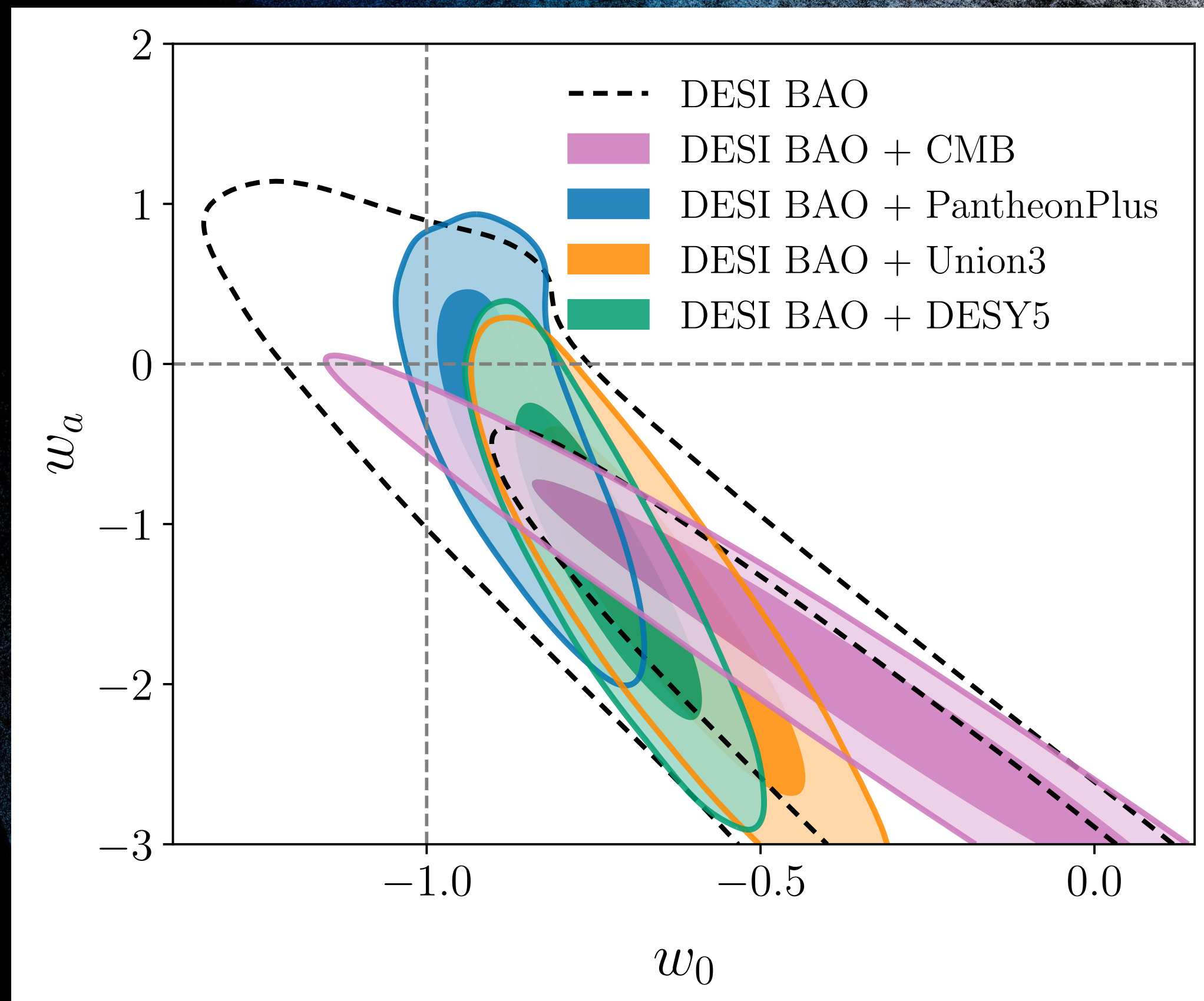
Hopefully no!

★
General relativity

What I am generally excited about - Cosmic Acceleration and Dynamical Dark Energy

Dark energy appears to be evolving with time as $w = w_0 + w_a(1 - a)$

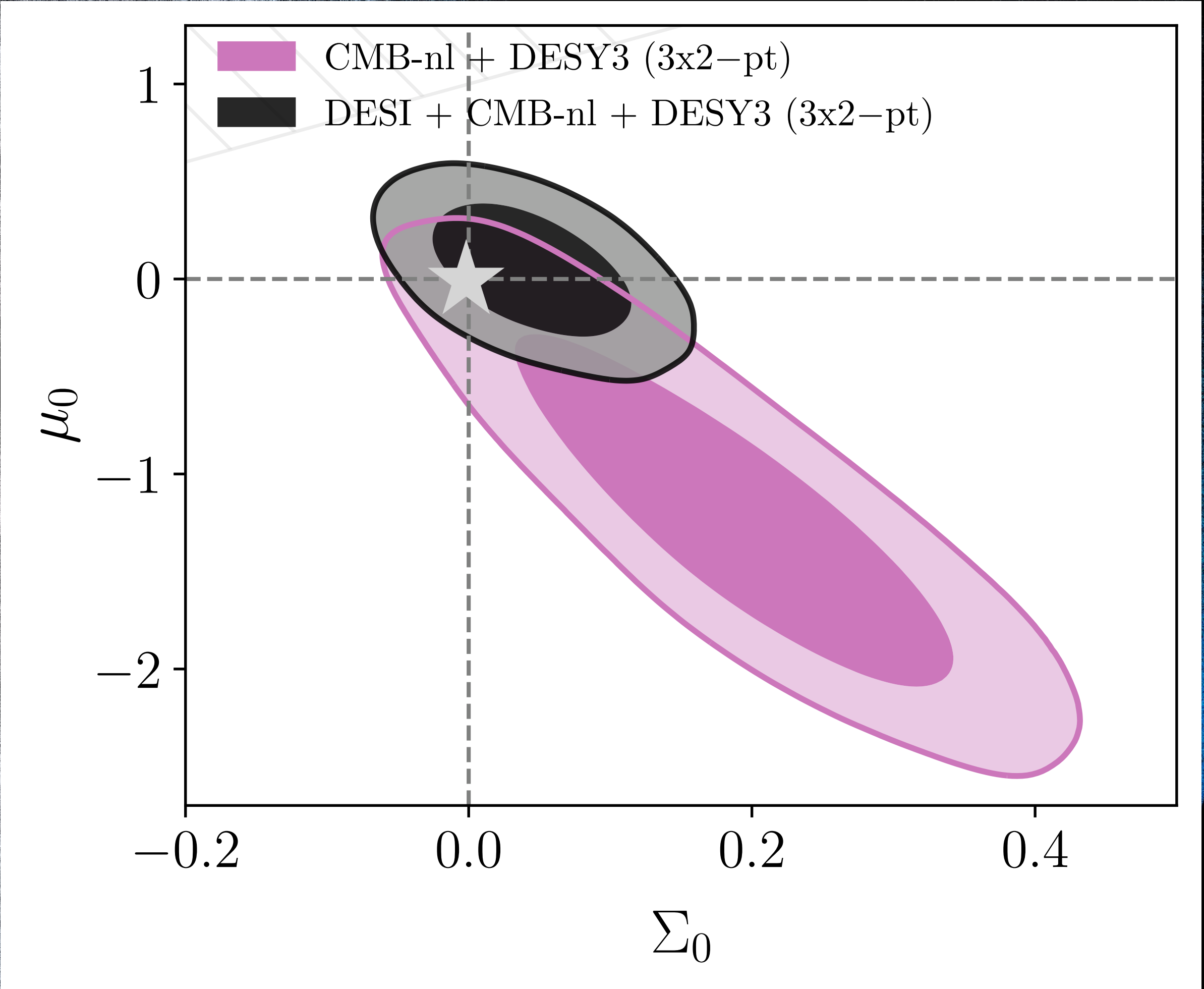
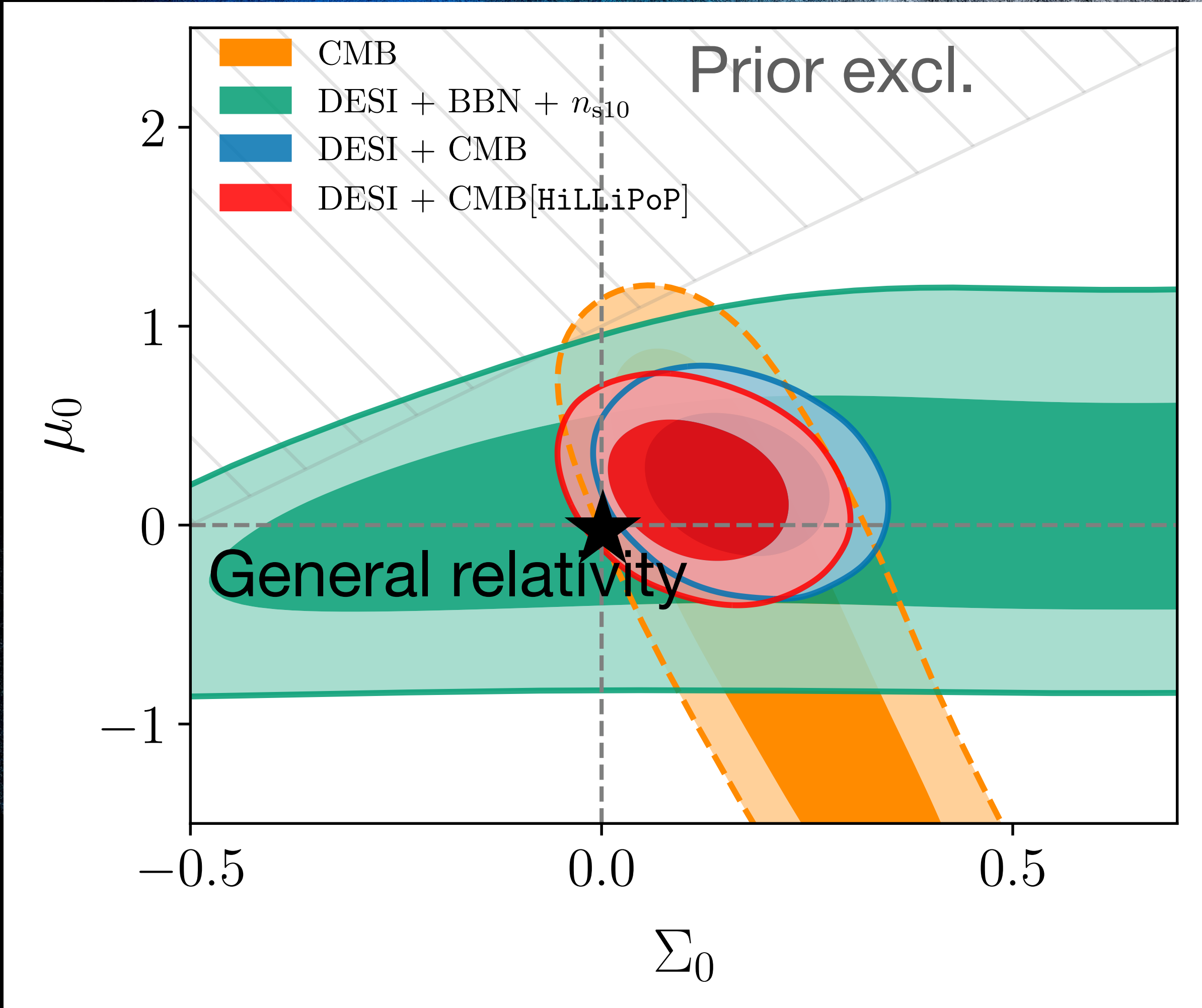
DESI 2024 VI, JCAP02(2025) incl. MN



Same conclusion at higher significance in DESI DR2 Results II, PRD 112, 083515

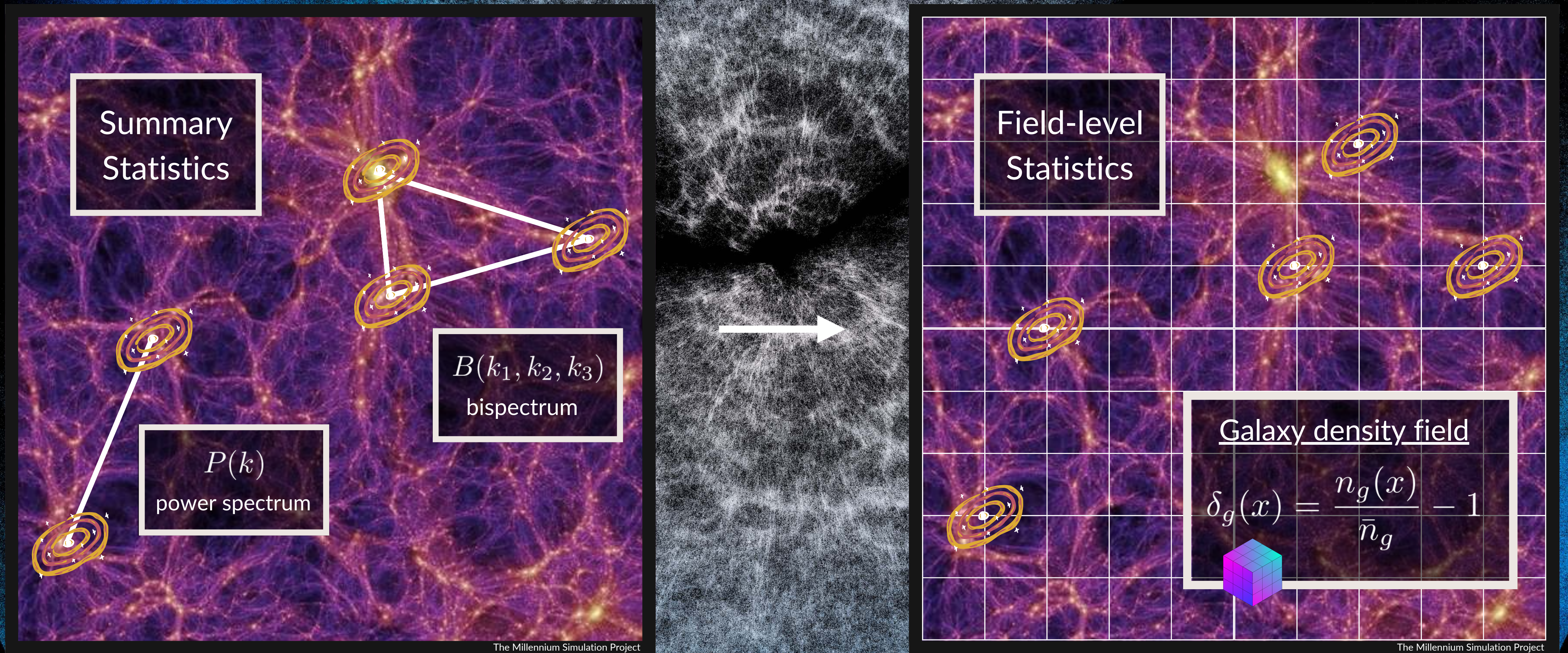
What I am generally excited about - Growth of Structure and Modified Gravity

No evidence for modified gravity beyond GR in (μ_0, Σ_0) extension



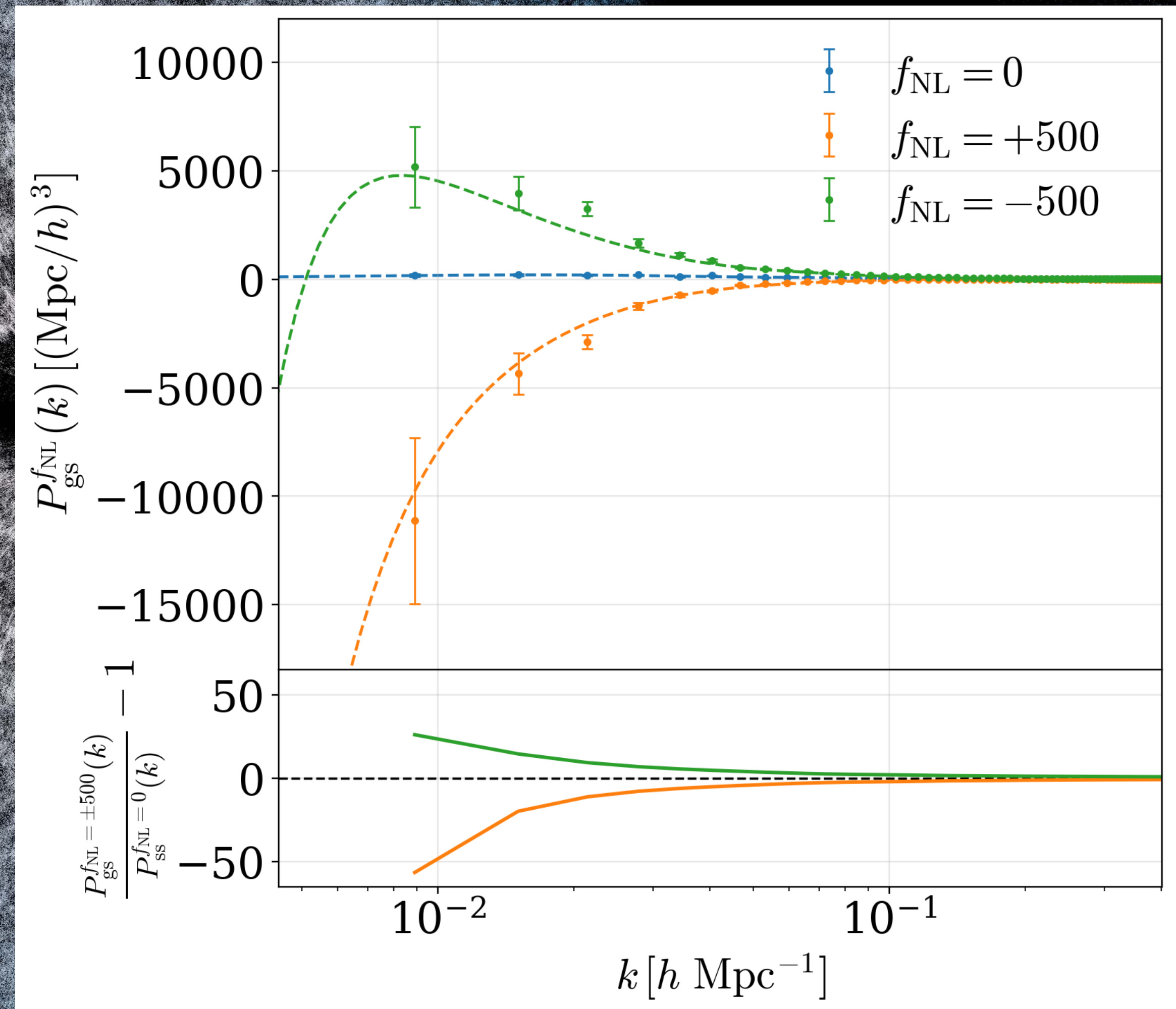
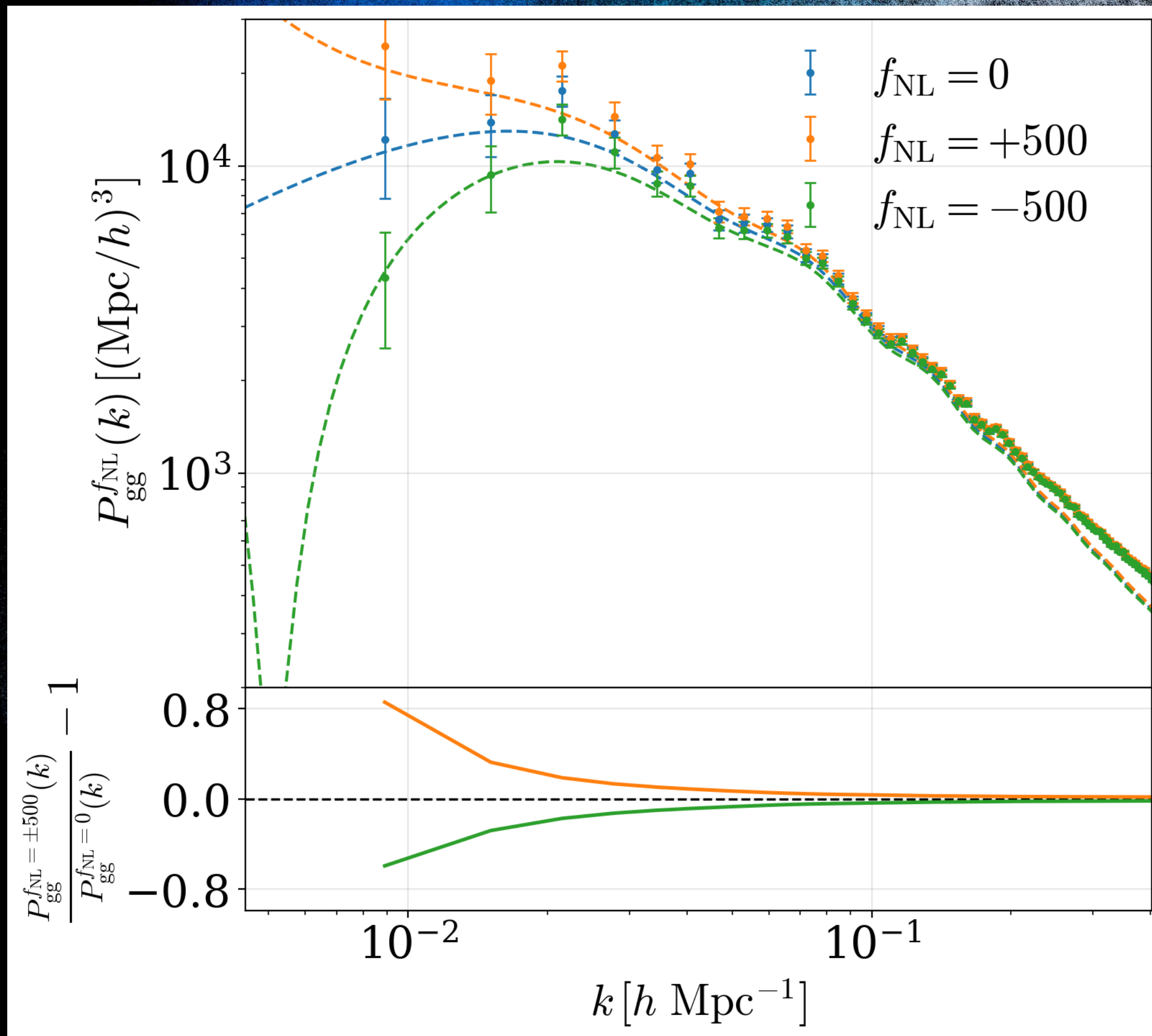
What I am generally excited about - Field-level inference

How much information can be extracted from galaxy distribution?



What I am recently excited about - tiny Primordial non-Gaussianity in the early universe

The galaxy distribution on large scales is modulated by local PNG



The current and next era of galaxy surveys



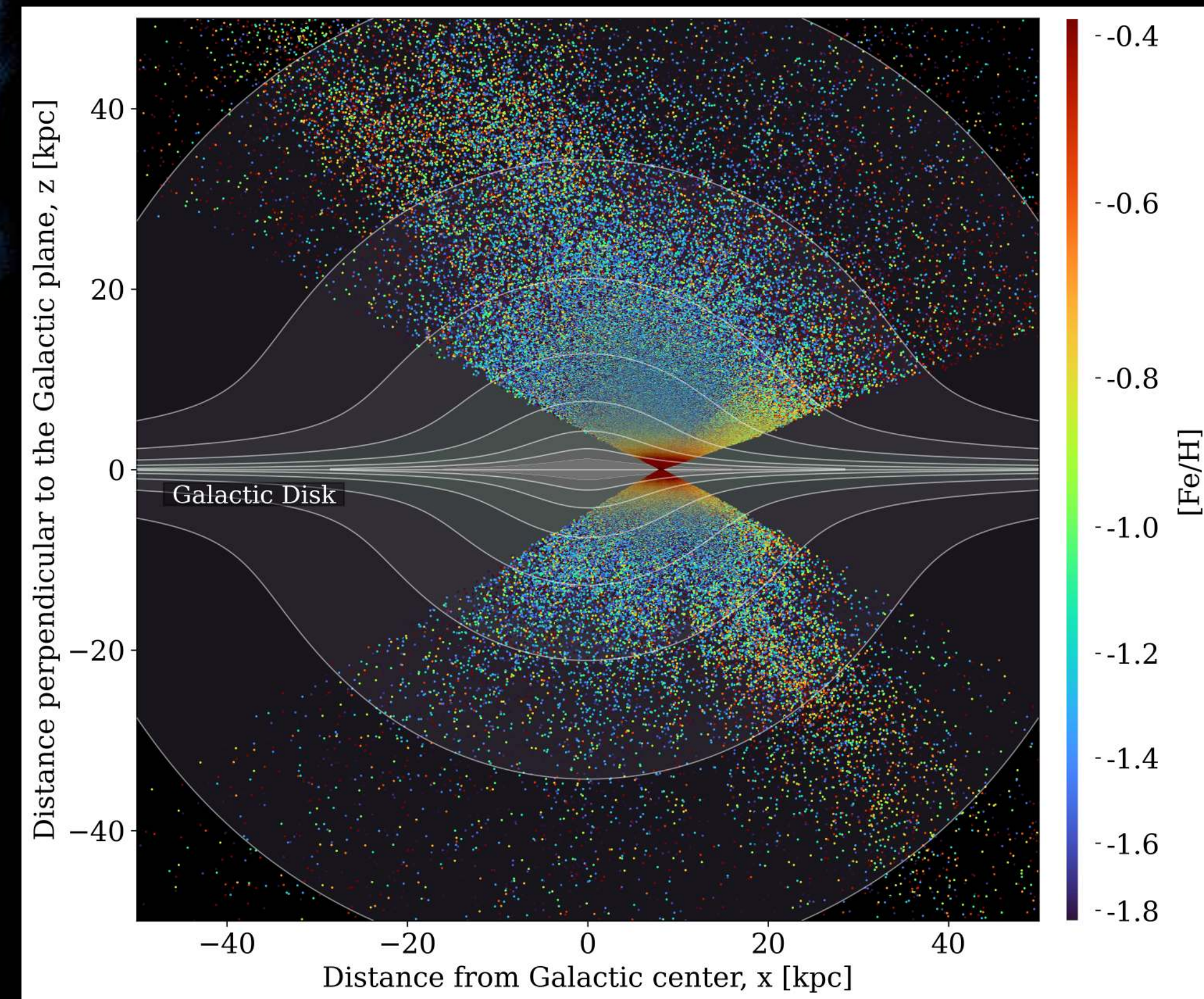
DARK ENERGY
SPECTROSCOPIC
INSTRUMENT

U.S. Department of Energy Office of Science



Credit: Dark Energy Spectroscopic Instrument

~15M galaxies in DESI DR2

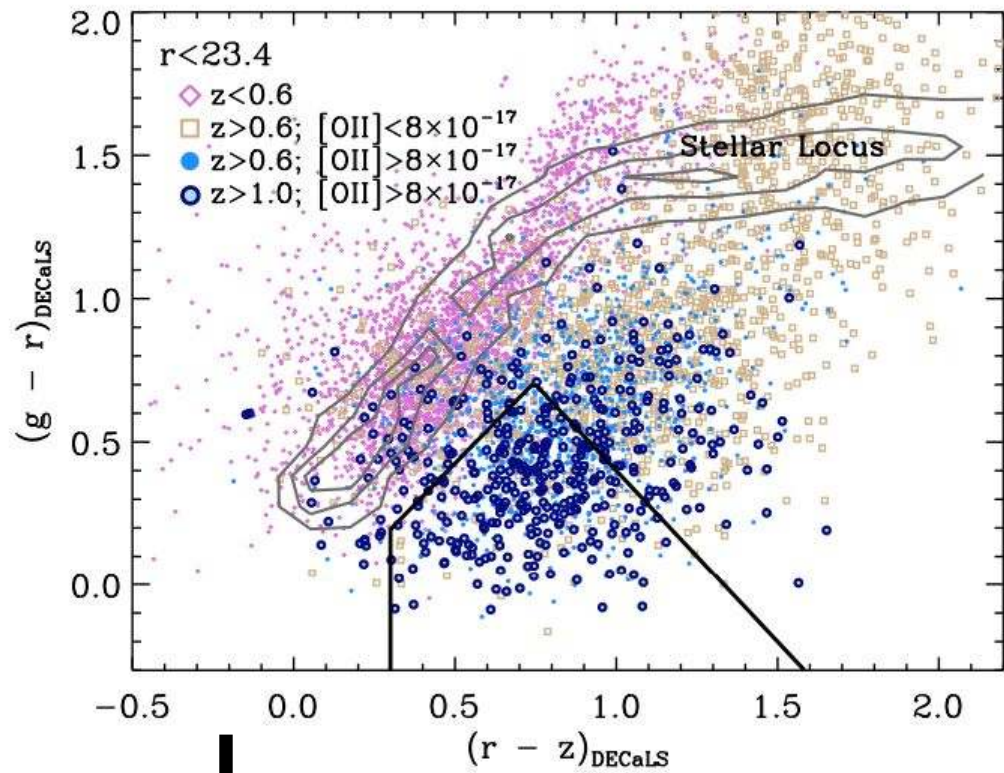


DESI DR1

Wide-field imaging survey(s) → target selection → spectroscopic survey



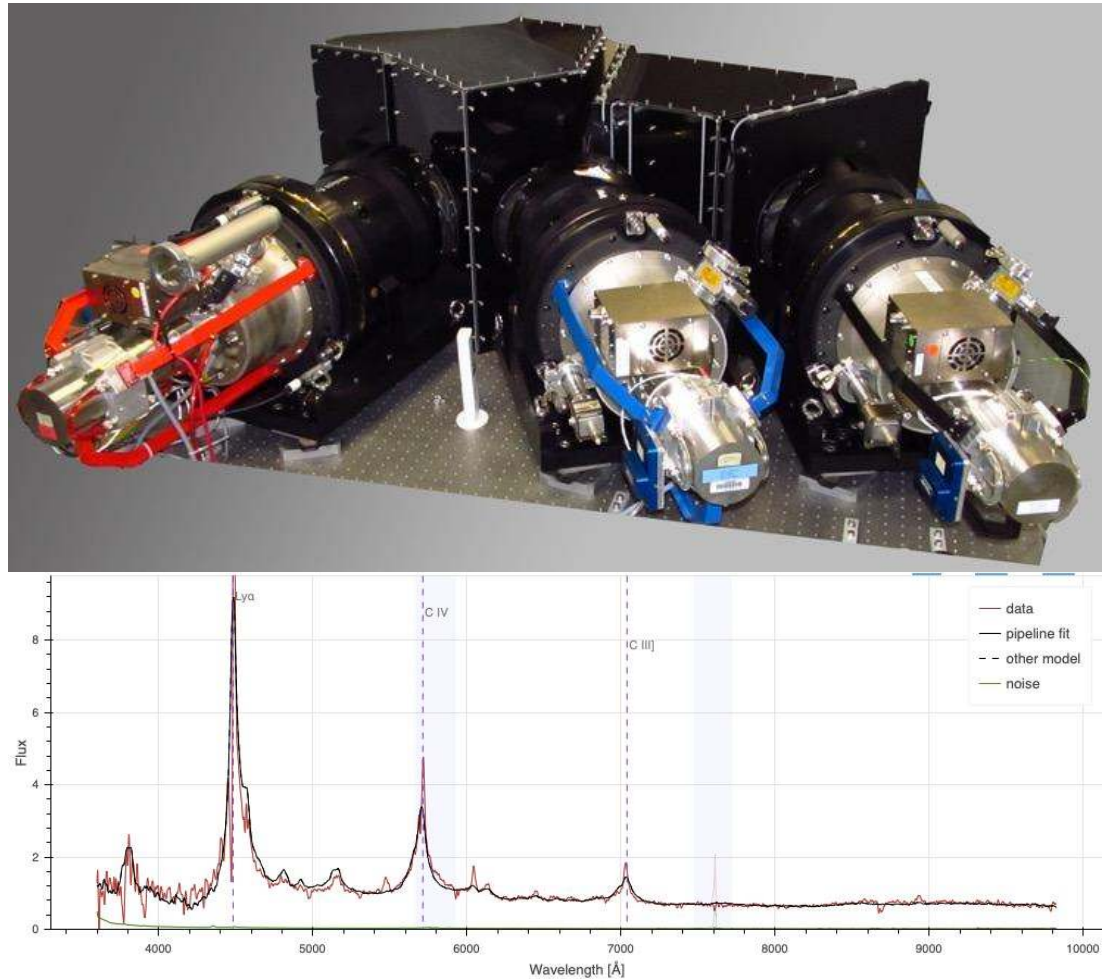
Target Selection



↓ Observation...

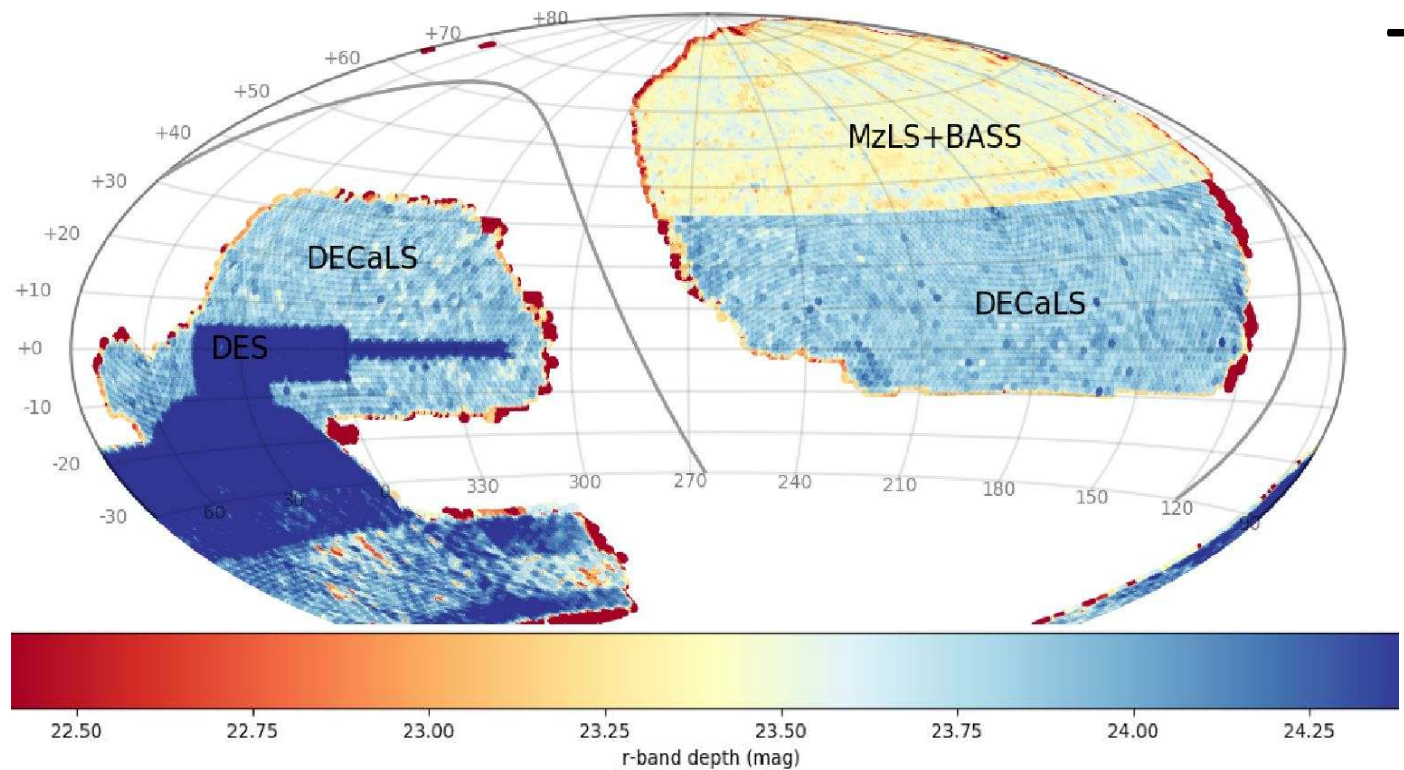


...of 5000 objects
every ~20mins...



Imaging Surveys (2014-2019)

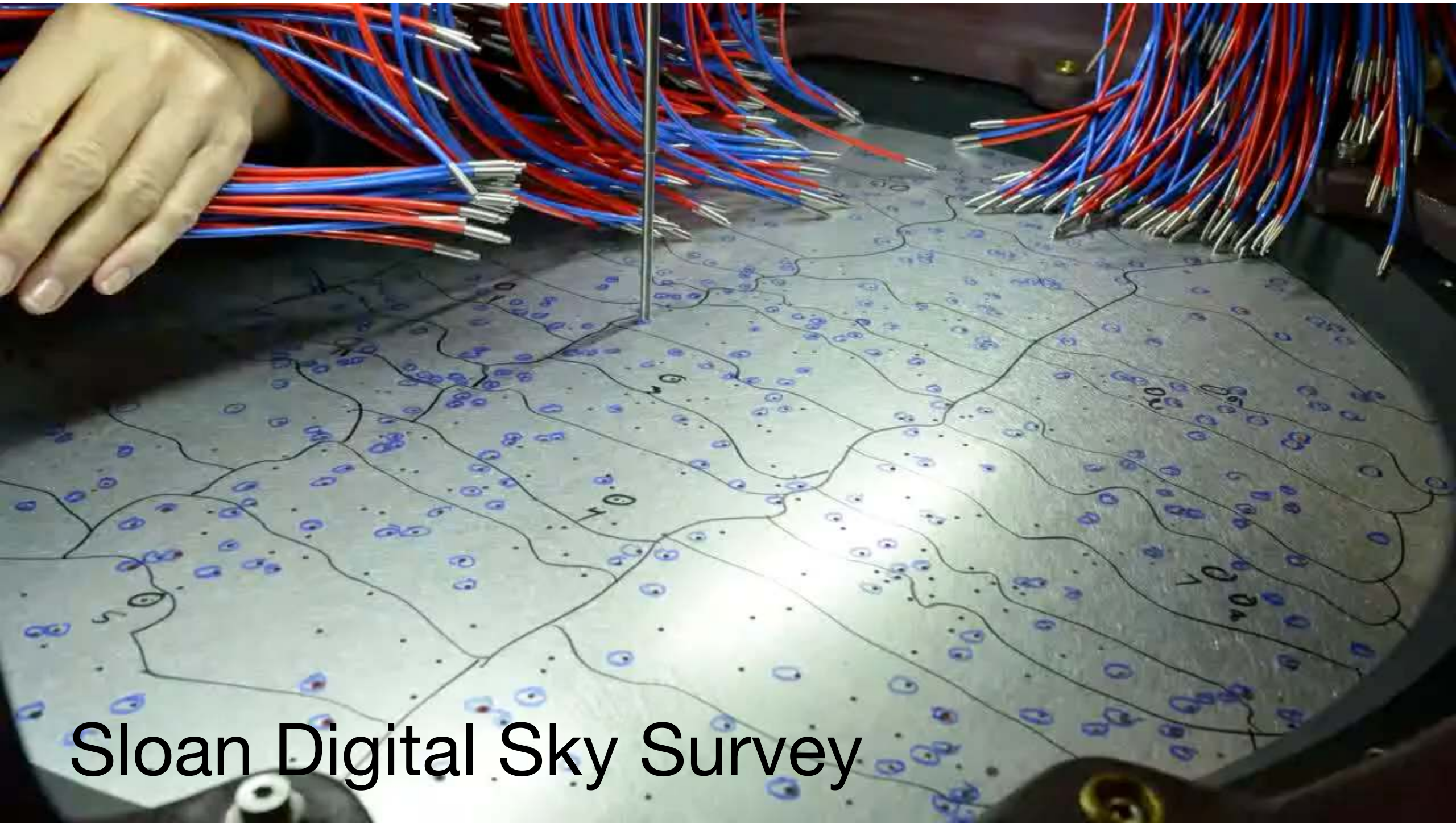
+WISE IR sat



...and measure their redshift

Advances in multi-object spectrograph really push the limit LSS survey number density

Plug plate



Sloan Digital Sky Survey

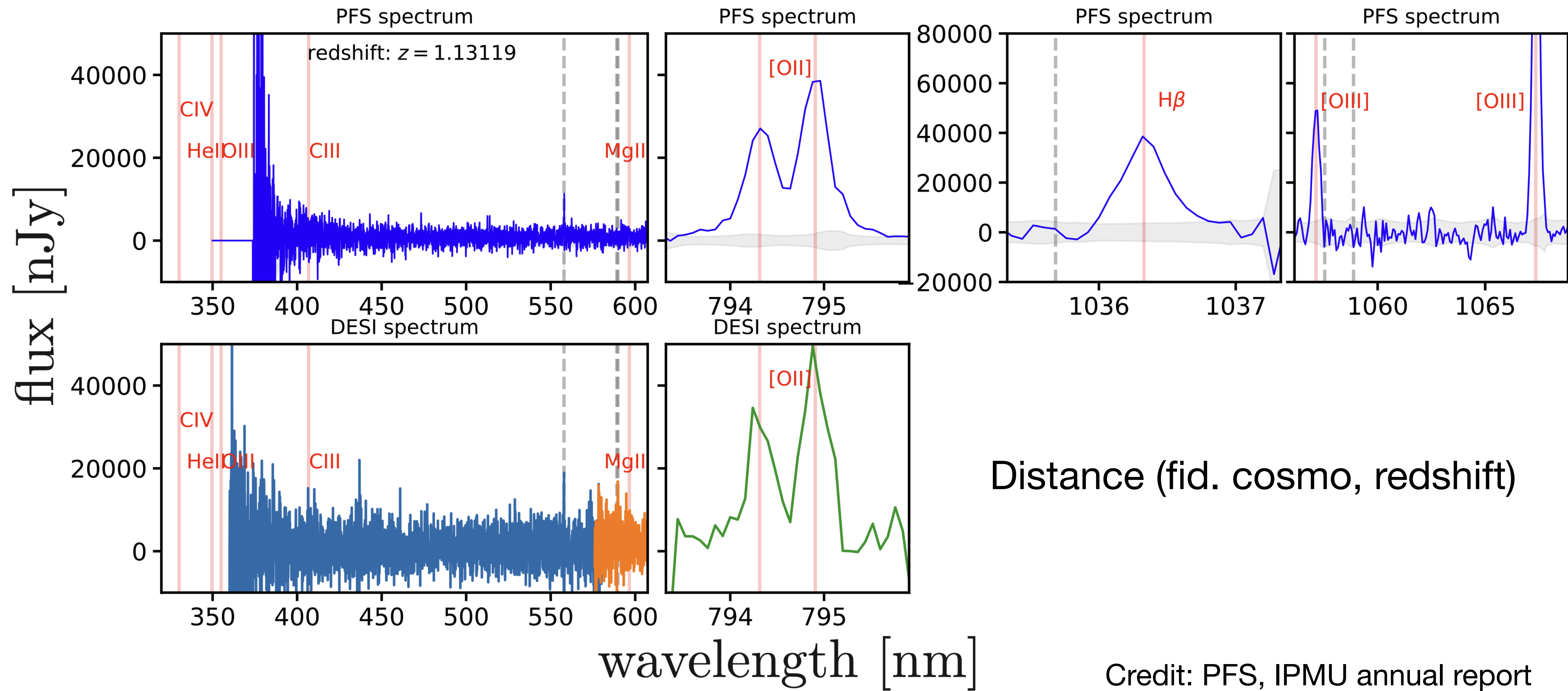
Robotic positioners



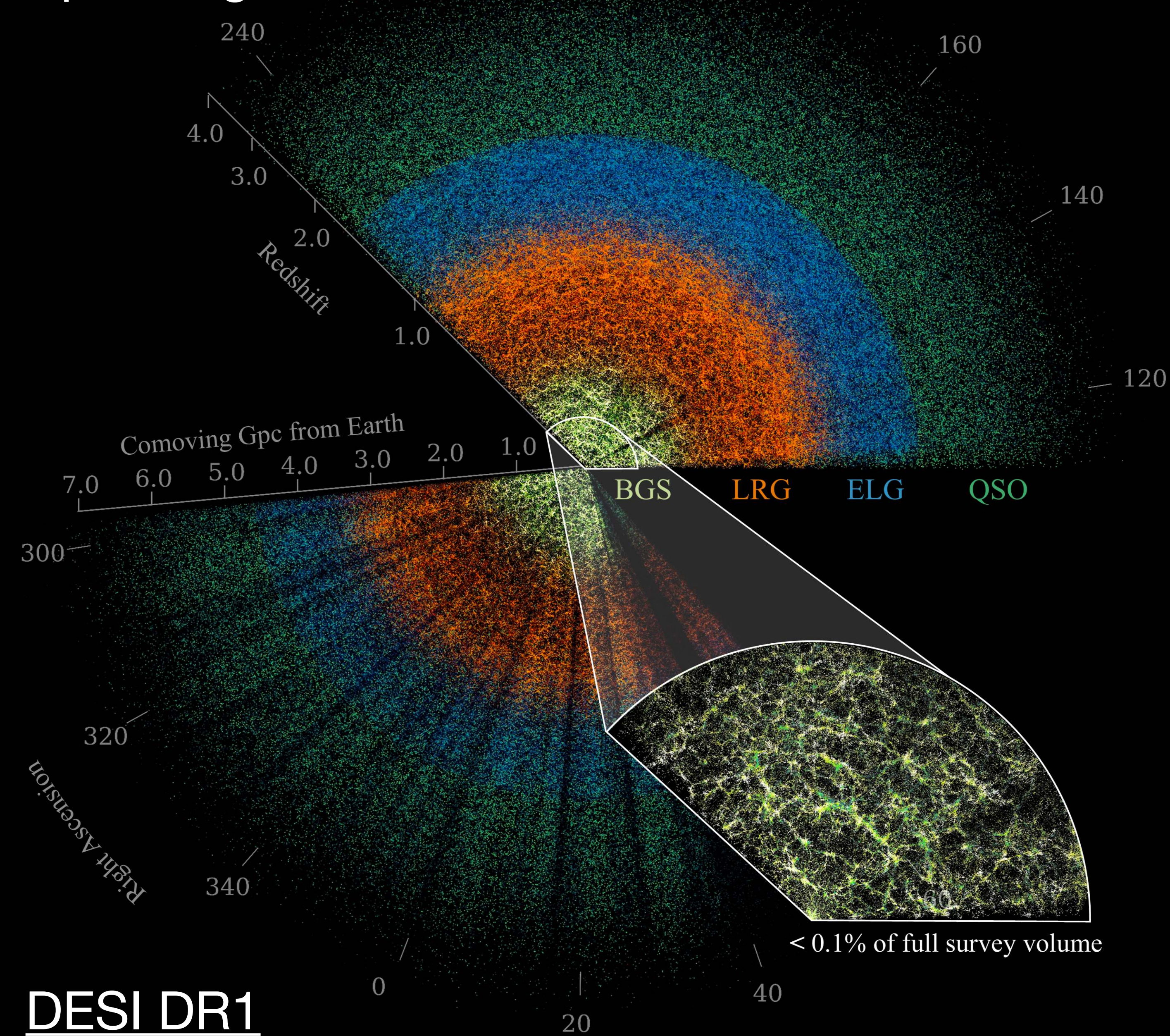
Dark Energy Spectroscopic Instrument

5000 objects in every ~20 minutes

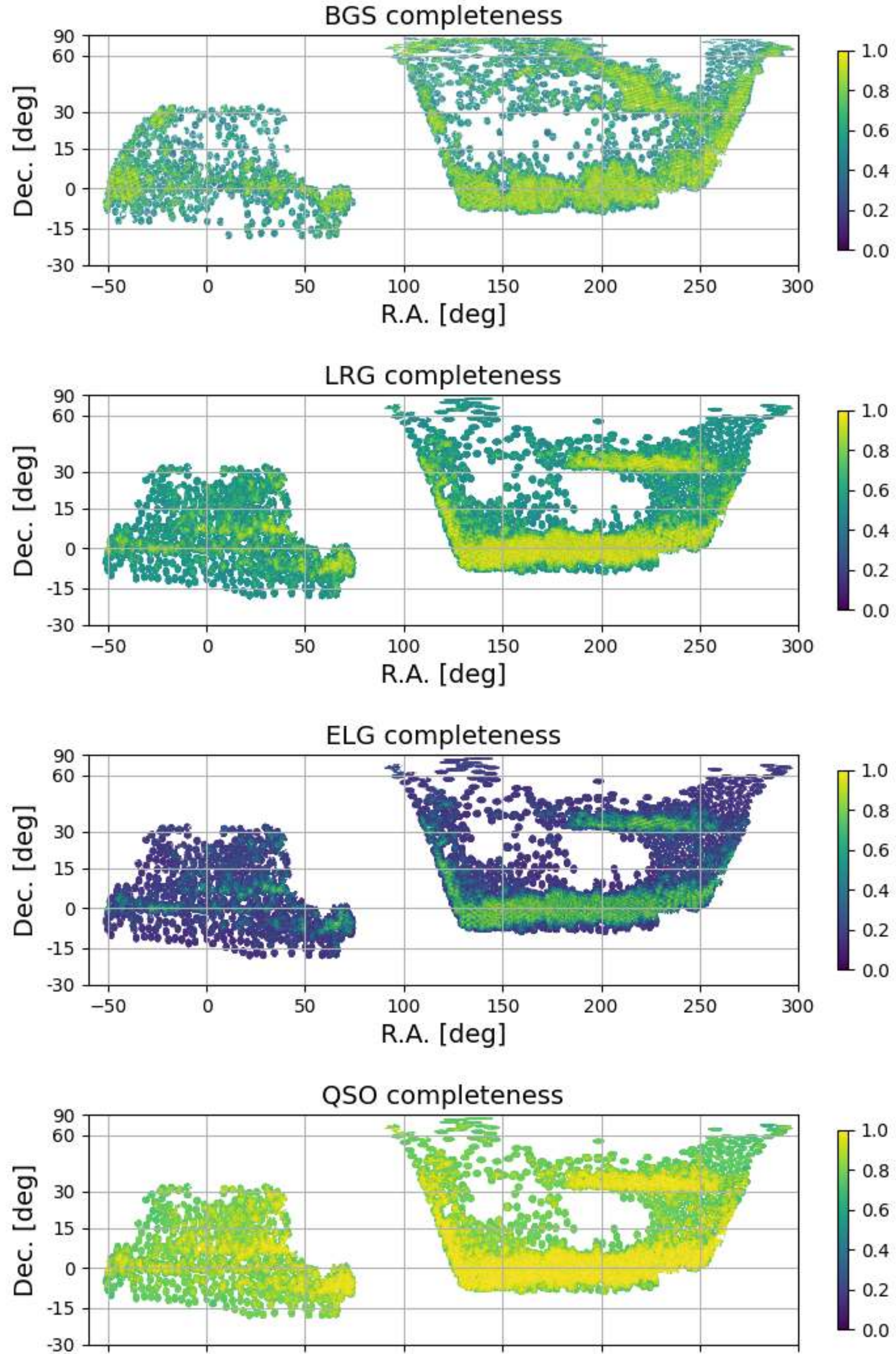
Assuming a fiducial cosmology, spectral redshifts can be converted to distances



Four galaxy populations
spanning redshift ~ 0.1 -4.1



DESI DR1



DESI 2024 II JCAP07(2025)017 incl. MN

The current analysis of galaxy surveys

Two-point statistics of galaxy clustering



DARK ENERGY
SPECTROSCOPIC
INSTRUMENT

U.S. Department of Energy Office of Science



Credit: Dark Energy Spectroscopic Instrument

(Hierarchical) Bayesian inference and two-point statistics of galaxy maps

$$P(\theta \mid d) = \frac{P(d \mid \theta) P(\theta)}{P(d)} \propto P(d \mid \theta) P(\theta)$$

What is the cosmology θ given the data d ?

(Hierarchical) Bayesian inference and two-point statistics of galaxy maps

$$P(\theta \mid d) = \frac{P(d \mid \theta) P(\theta)}{P(d)} \propto P(d \mid \theta) P(\theta)$$

What is the cosmology θ given the data d ?

$$n_g(\mathbf{x}, \tau) \longrightarrow n_g(\mathbf{x}) \longrightarrow \delta_g(\mathbf{x}) = \frac{n_g(\mathbf{x}) - \bar{n}_g}{\bar{n}_g}$$

Full 3D galaxy density field

(Hierarchical) Bayesian inference and two-point statistics of galaxy maps

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Full 3D galaxy density field

$$P(\theta \mid \delta_g(\mathbf{x})) \propto P(\theta) \int \mathcal{D}\delta_{\text{ini}} P(\delta_g(\mathbf{x}) \mid \delta_{\text{ini}}, \theta) P(\delta_{\text{ini}} \mid \theta)$$

Field-level inference analysis

(Hierarchical) Bayesian inference and two-point statistics of galaxy maps

$$P(\theta \mid d) = \frac{P(d \mid \theta) P(\theta)}{P(d)} \propto P(d \mid \theta) P(\theta)$$

What is the cosmology θ given the data d ?

$$n_g(\mathbf{x}, \tau) \longrightarrow n_g(\mathbf{x}) \longrightarrow \delta_g(\mathbf{x}) = \frac{n_g(\mathbf{x}) - \bar{n}_g}{\bar{n}_g}$$

Full 3D galaxy density field

$$\xi_g(\mathbf{r}) \equiv \left\langle \delta_g(\mathbf{x}) \delta_g(\mathbf{x} + \mathbf{r}) \right\rangle$$

Compressed two-point statistics

$$\xi_g(r) = \int_0^\infty \frac{k^2 dk}{2\pi^2} P_g(k) \frac{\sin kr}{kr}$$

$$P_{\text{lin}}^{\text{th}}(k; \theta) \equiv \left\langle |\delta_{\text{ini}}(\mathbf{k})|^2 \right\rangle_\theta$$

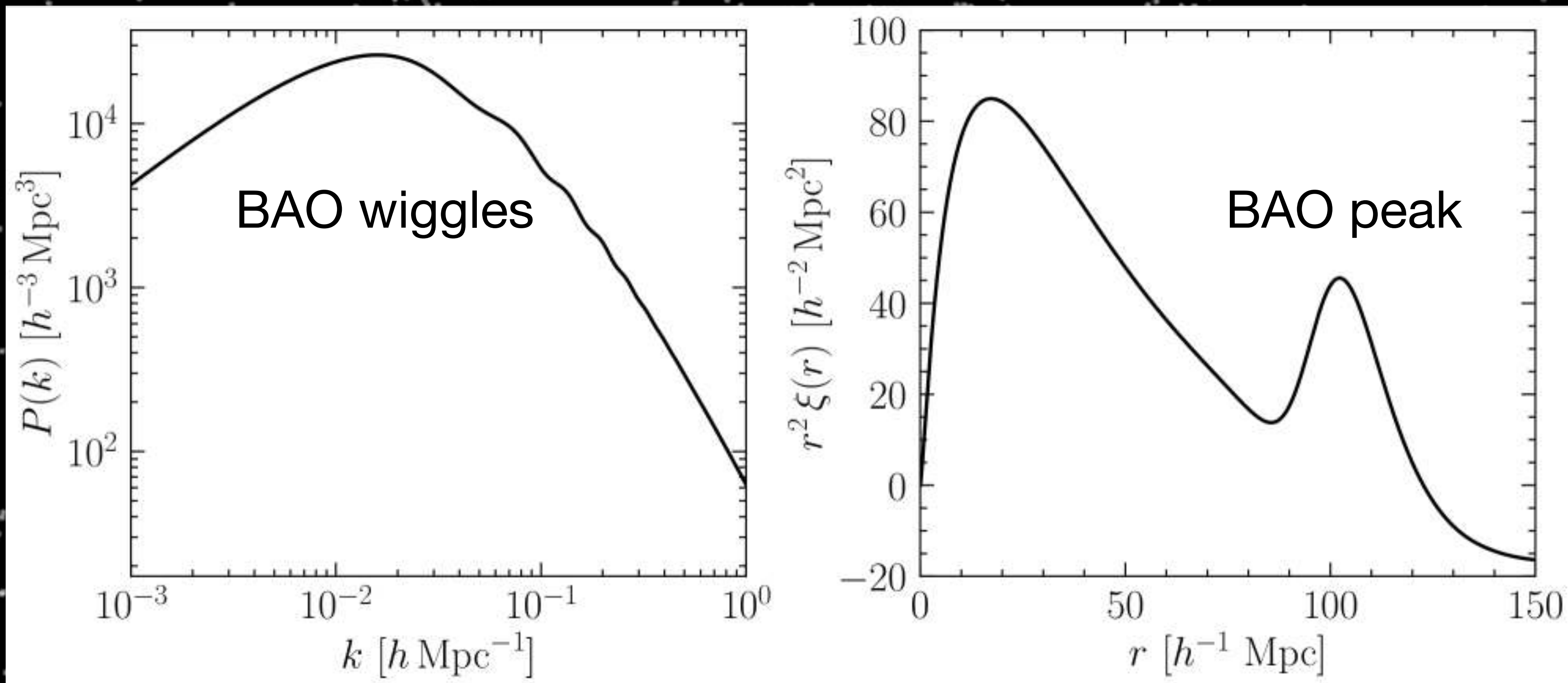
$$P(\theta \mid \widehat{P}_g(k)) \propto P(\theta) P(\widehat{P}_g(k) \mid P_{\text{lin}}^{\text{th}}(k; \theta), \theta)$$

Power-spectrum analysis

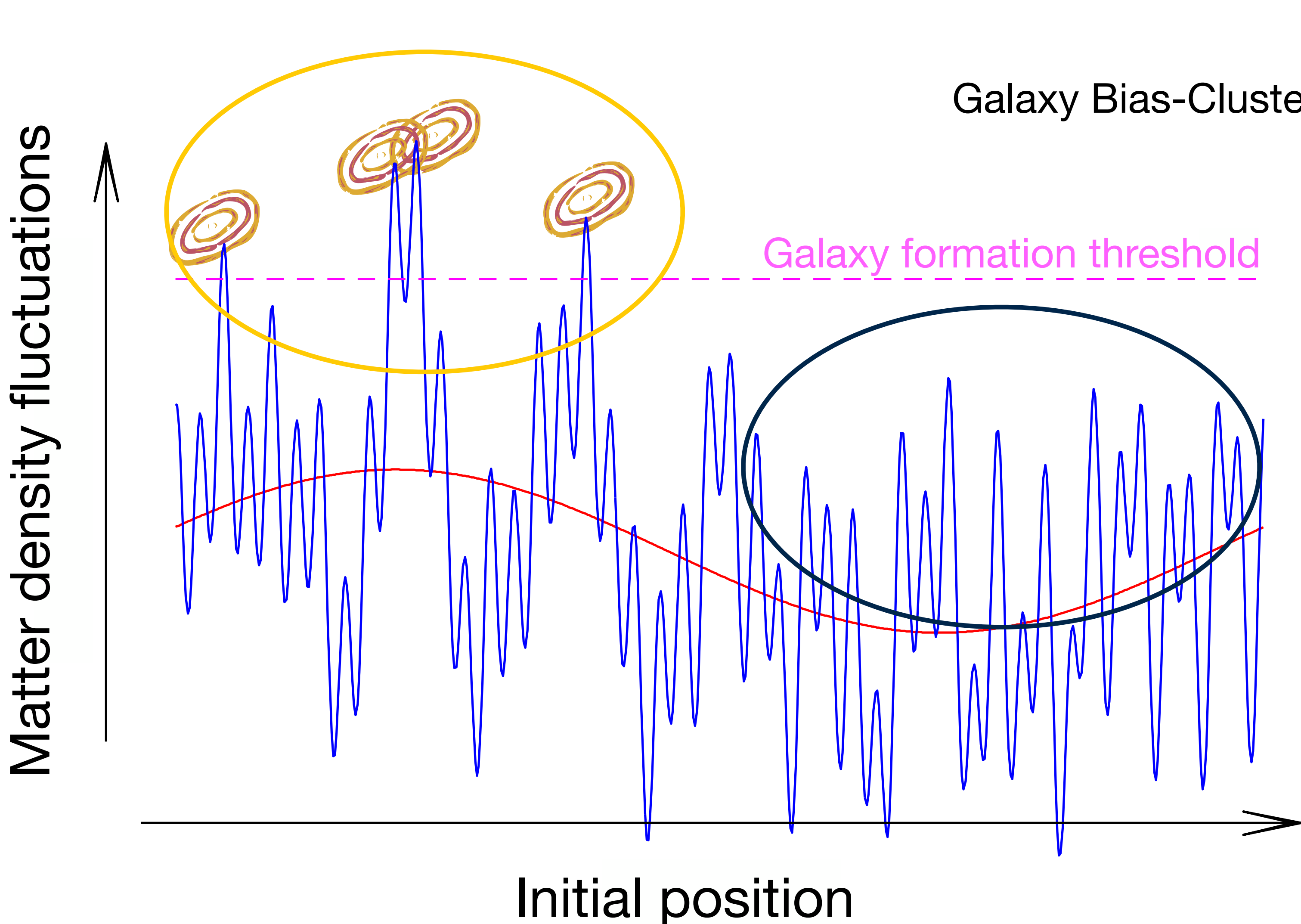
Baryon Acoustic Oscillation in the galaxy 2-point statistics

BAO imprints in the galaxy 2-point statistics

Power spectrum $\longleftrightarrow$ Fourier transform 2-point correlation function

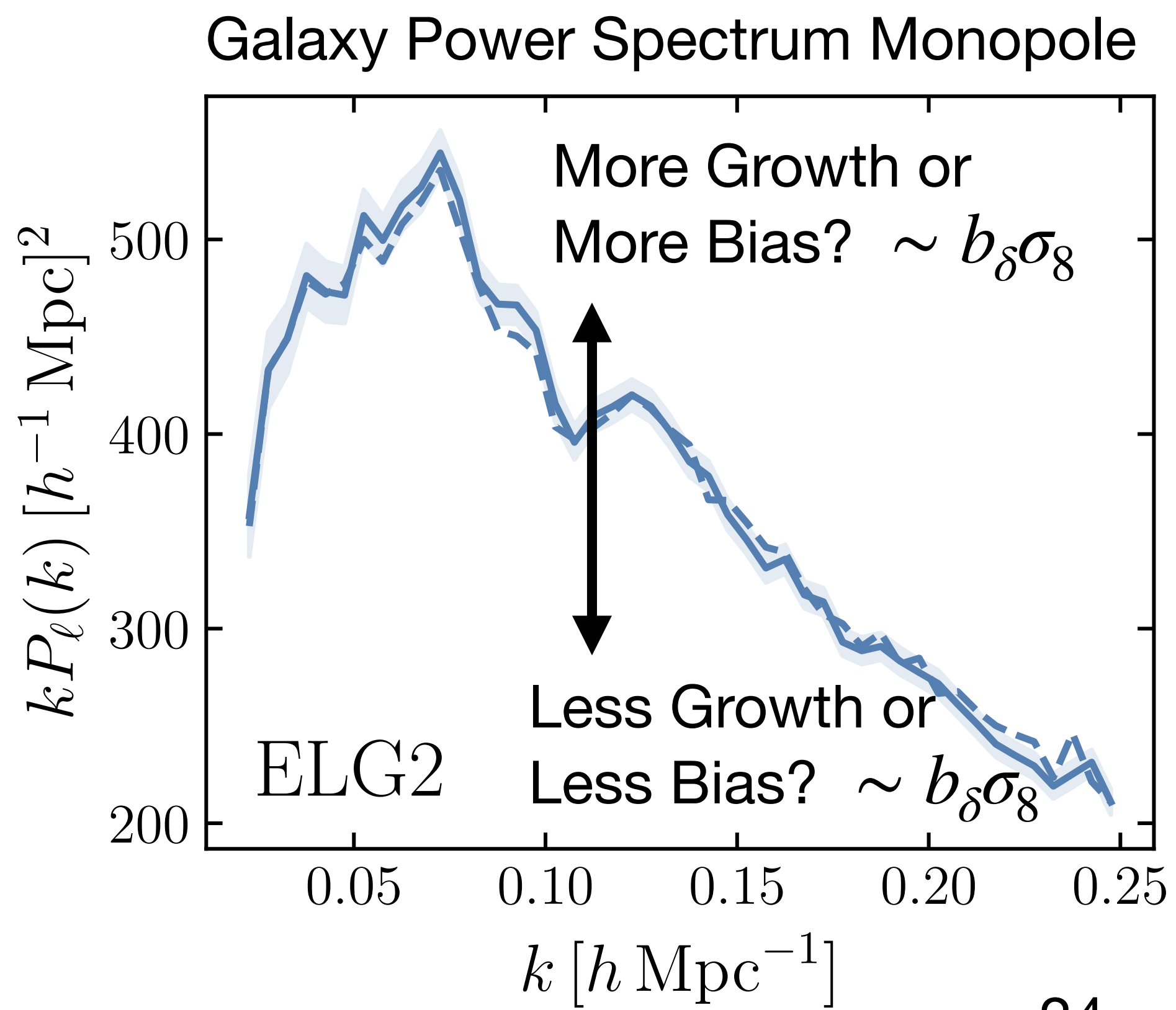


First complication: galaxies are rare peaks in matter fluctuations hence biased tracers

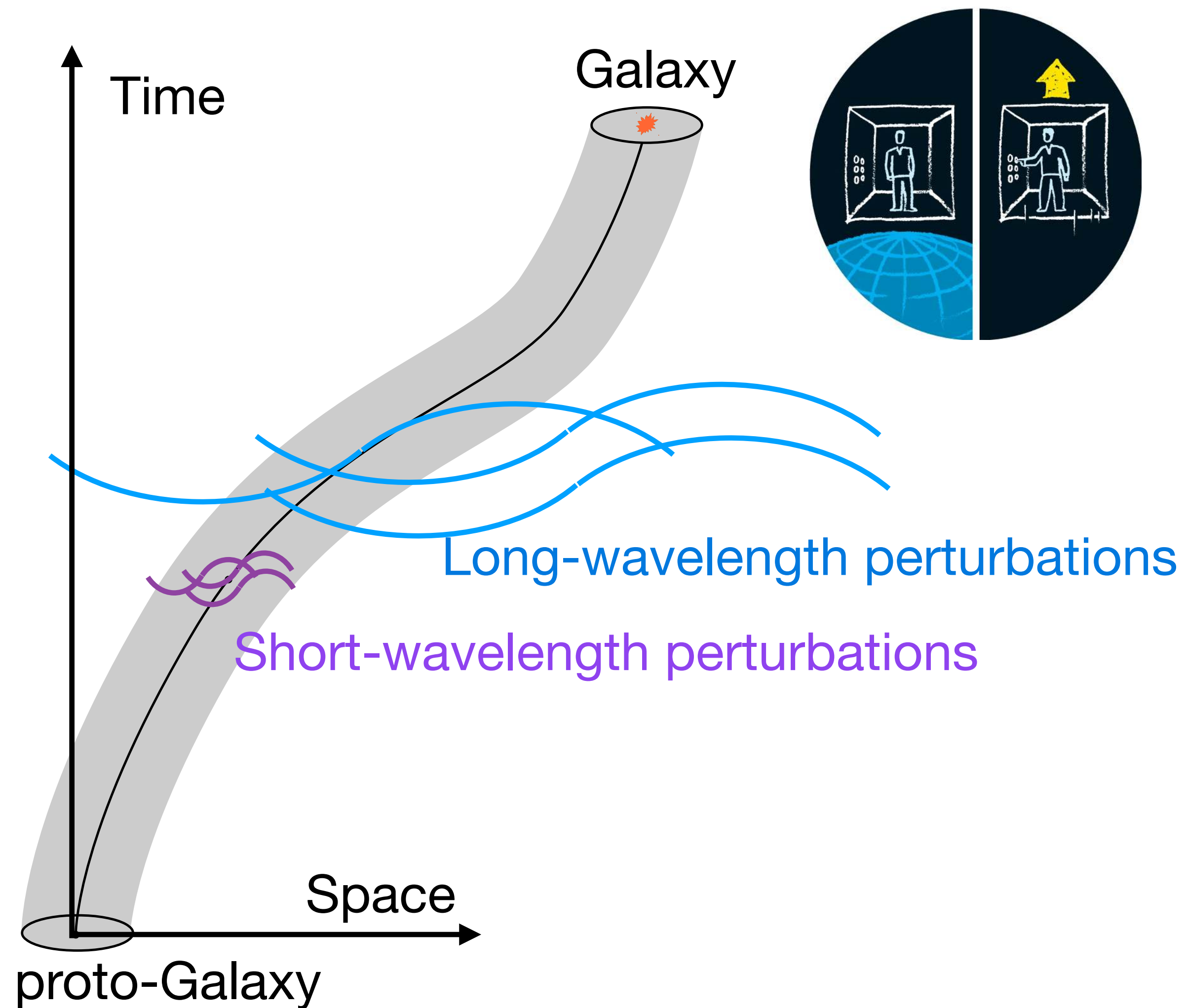


Galaxy Bias-Clustering Degeneracy

$$P_g \propto (b_\delta \sigma_8)^2$$



Still we can describe the galaxy-matter bias relation with Effective Field Theory of LSS



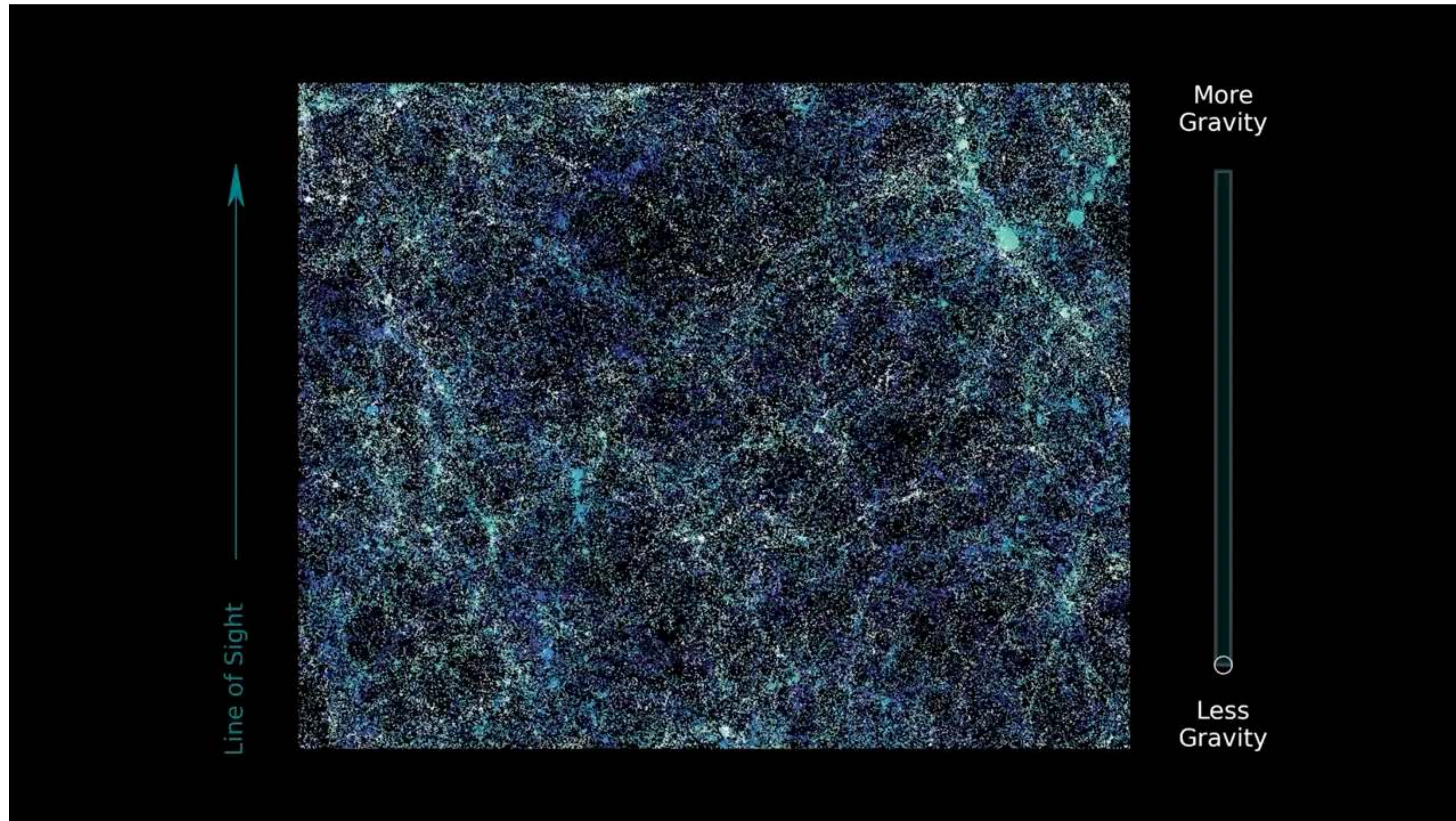
Equivalence principle

EFT galaxy bias expansion

$$\delta_g(\theta, \hat{s}) = \sum_O b_O O(\theta, \hat{s}) + \epsilon$$

bias expansion stochasticity

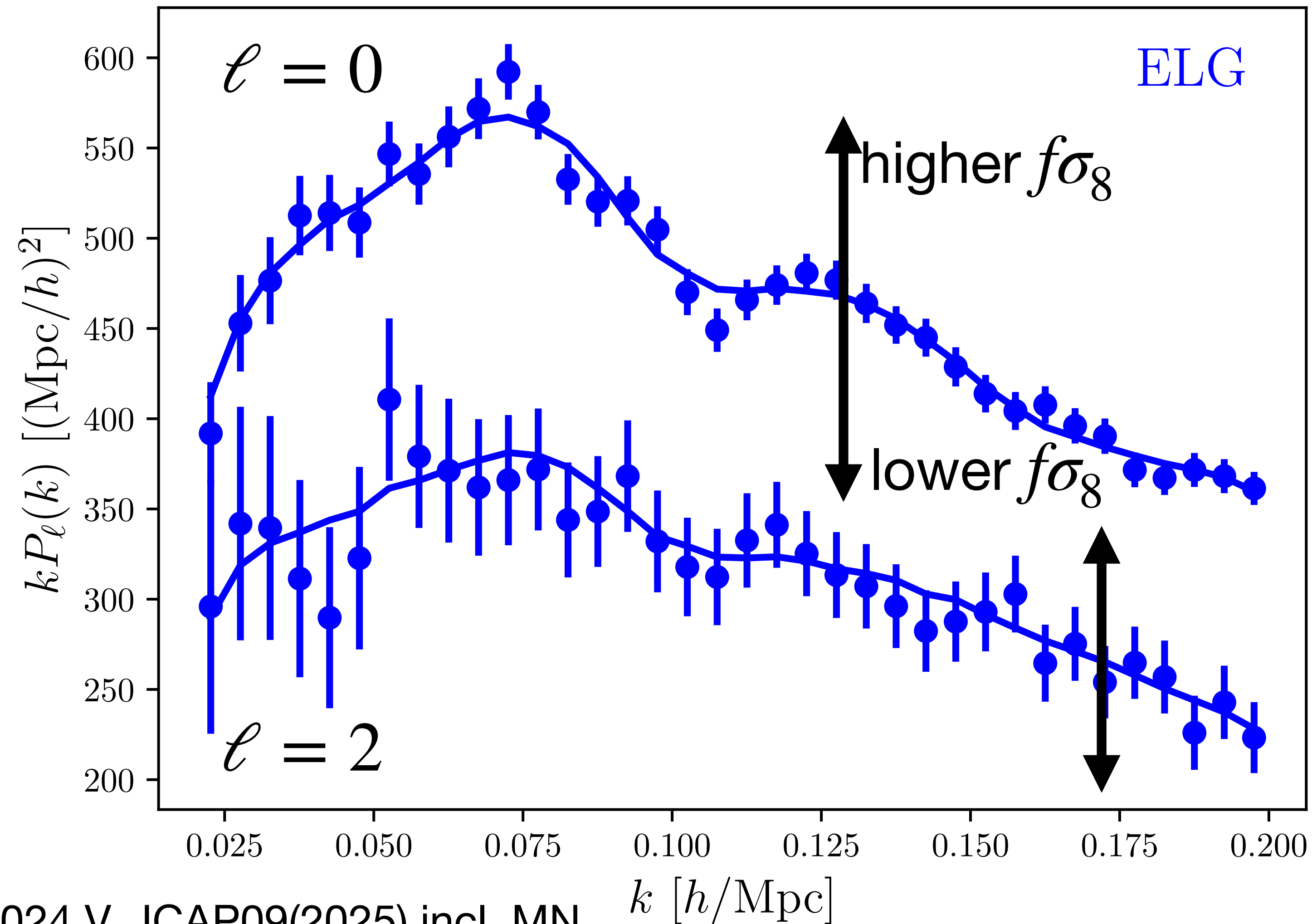
Second complication (or additional source of information): Redshift-space distortion



Credit: DESI, Claire Lamman and Michael Rashkovetskyi

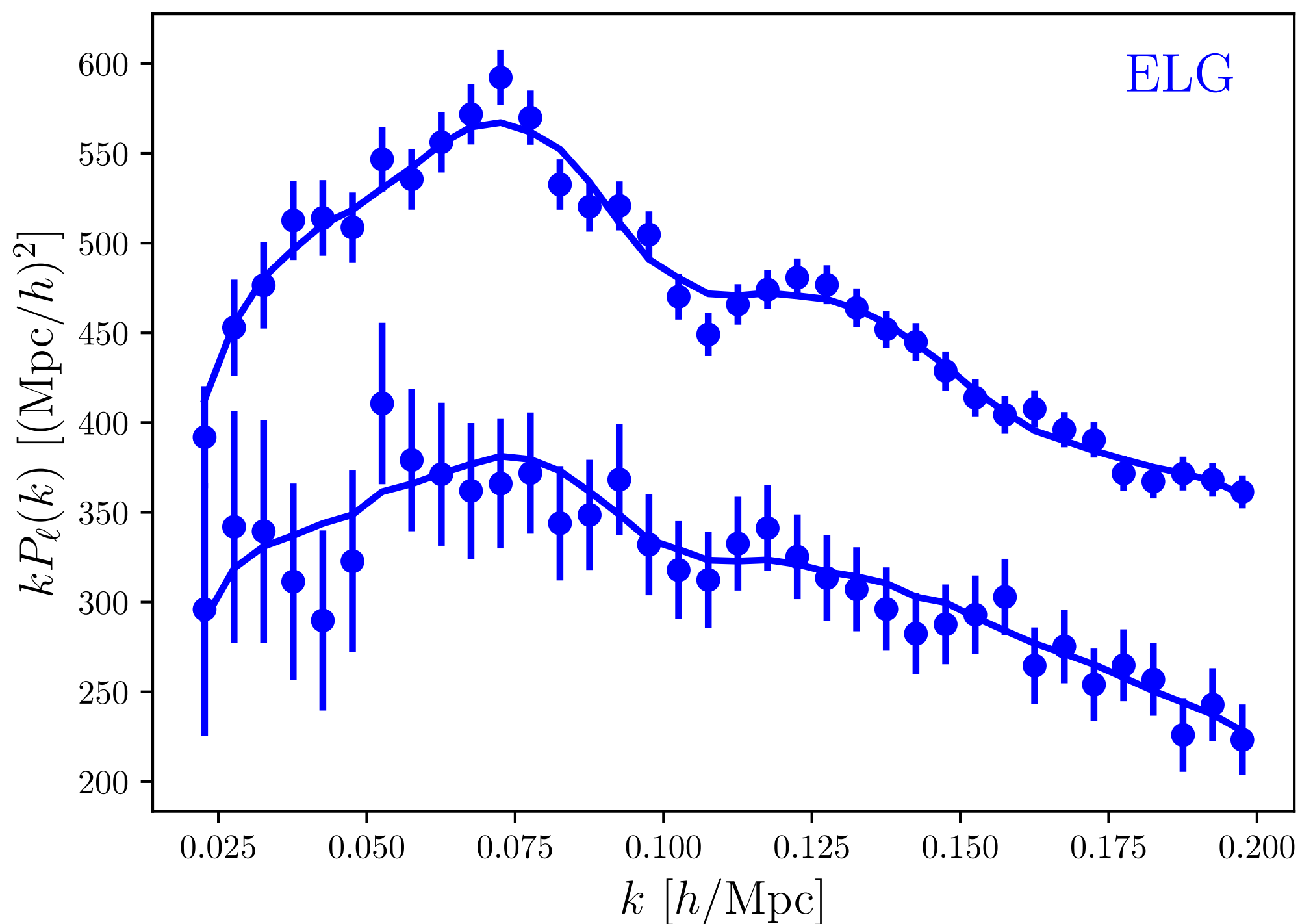
Putting everything together, we can predict the power spectrum in redshift space

$$P_{gg}^s(k, \mu) = P_{\ell=0}(k)L_0(\mu) + P_{\ell=2}(k)L_2(\mu) + P_{\ell=4}(k)L_4(\mu) + \dots$$

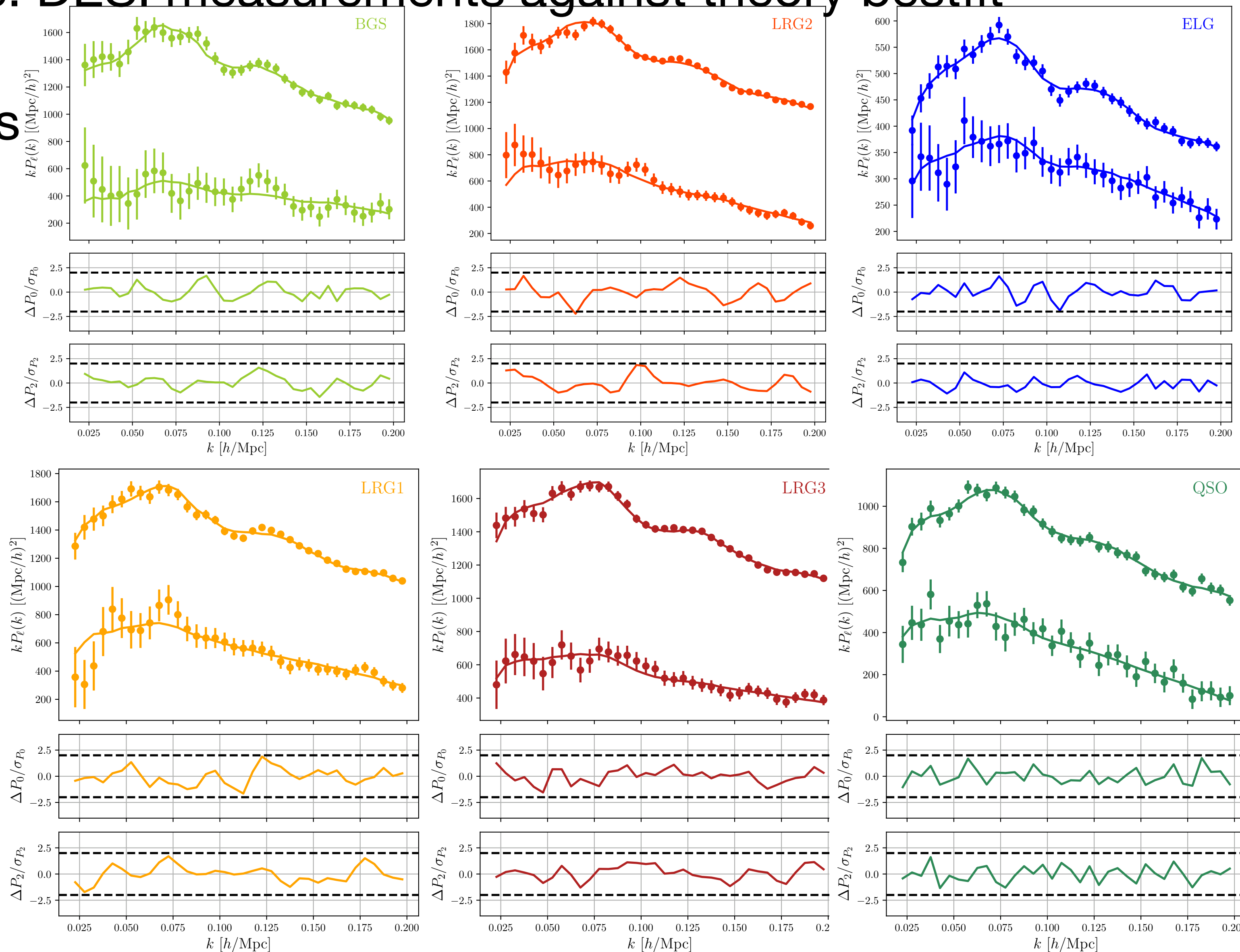


Power spectrum in redshift space: DESI measurements against theory bestfit

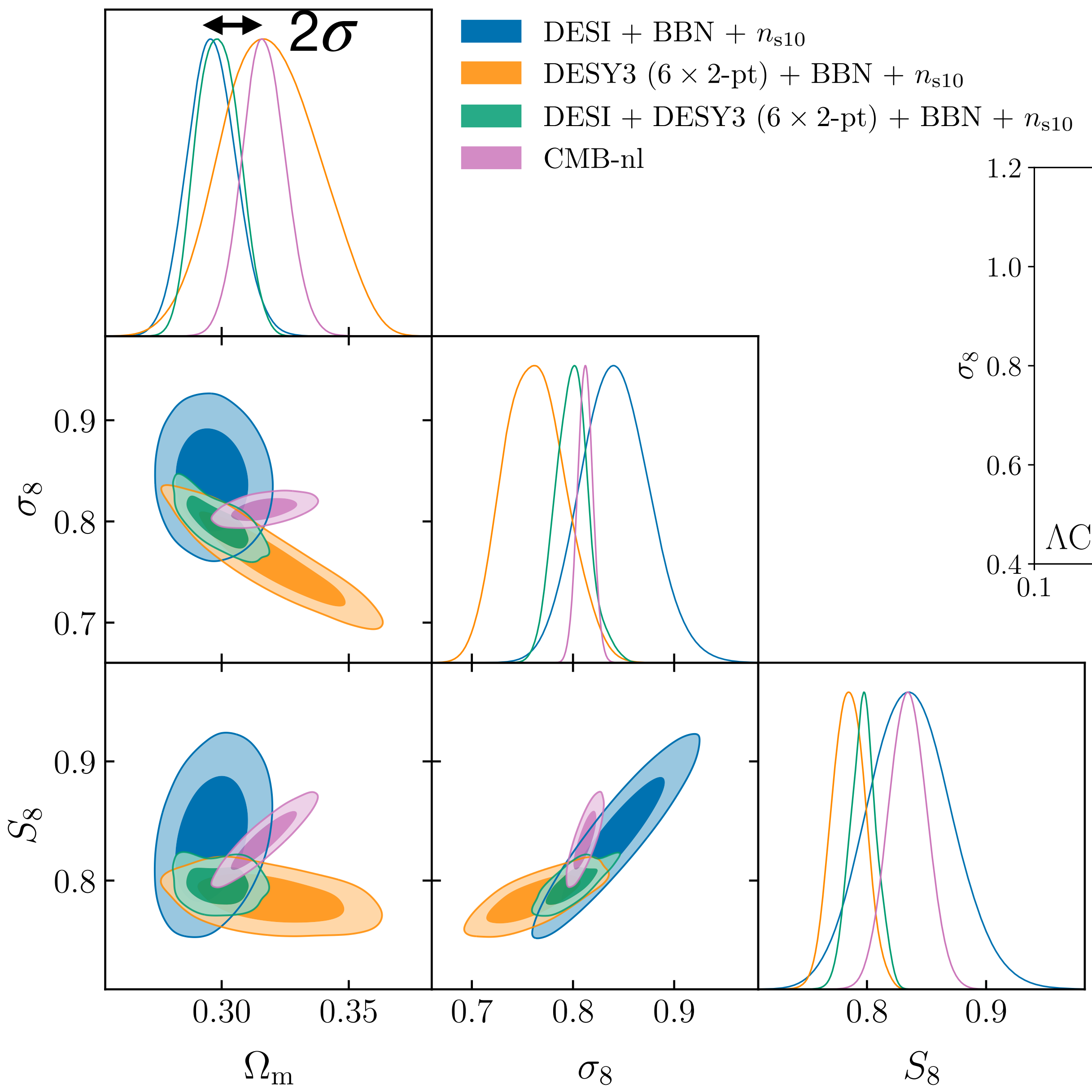
Galaxy power spectrum multipoles



DESI 2024 V, JCAP09(2025) incl. MN

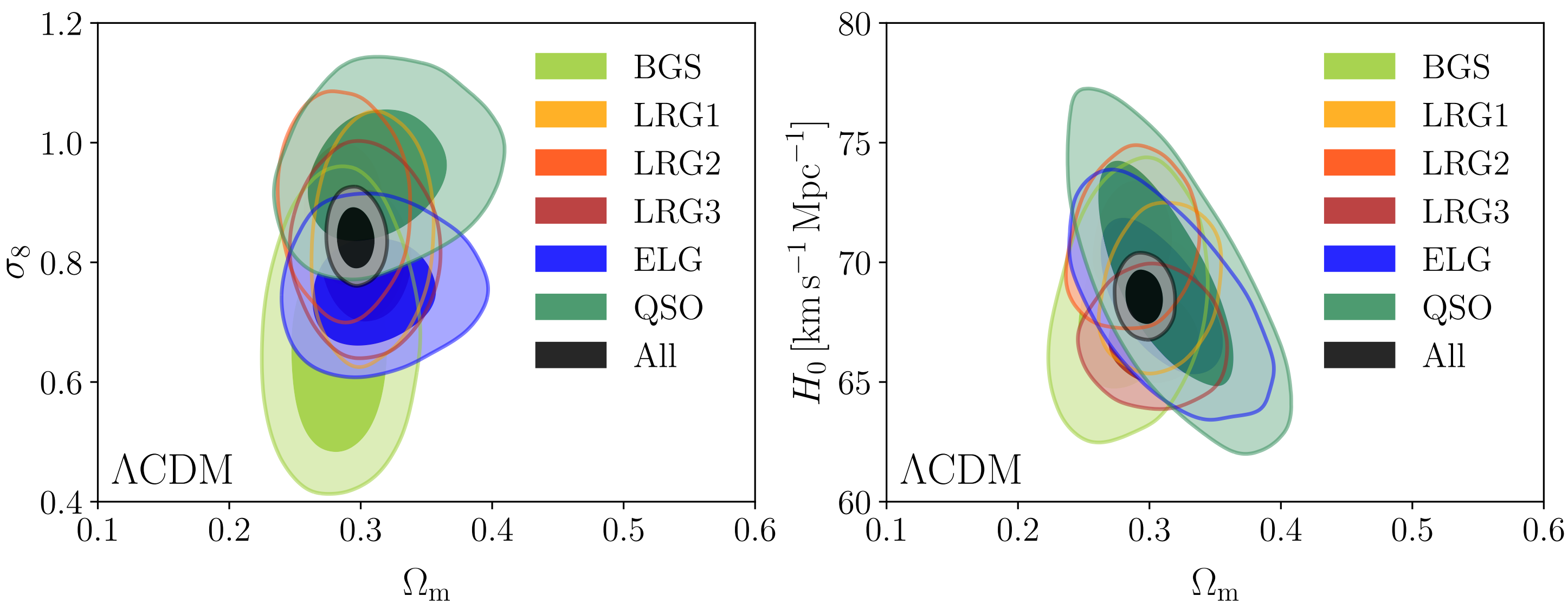


DESI DR1 results for the standard model Λ CDM



DESI 2024 V, JCAP09(2025) incl. MN

DESI 2024 VII, JCAP07(2025) incl. MN



DESI data alone is consistent with Λ CDM.

There is a mild ω_m tension with Planck CMB and SNe observations*.

*not shown, but please ask!

DESI DR1 results for beyond Λ CDM - dark energy

Dark energy appears to be evolving with time as $w = w_0 + w_a(1 - a)$

DESI 2024 VII, JCAP07(2025) incl. MN

--- DESI (BAO) + CMB + PantheonPlus

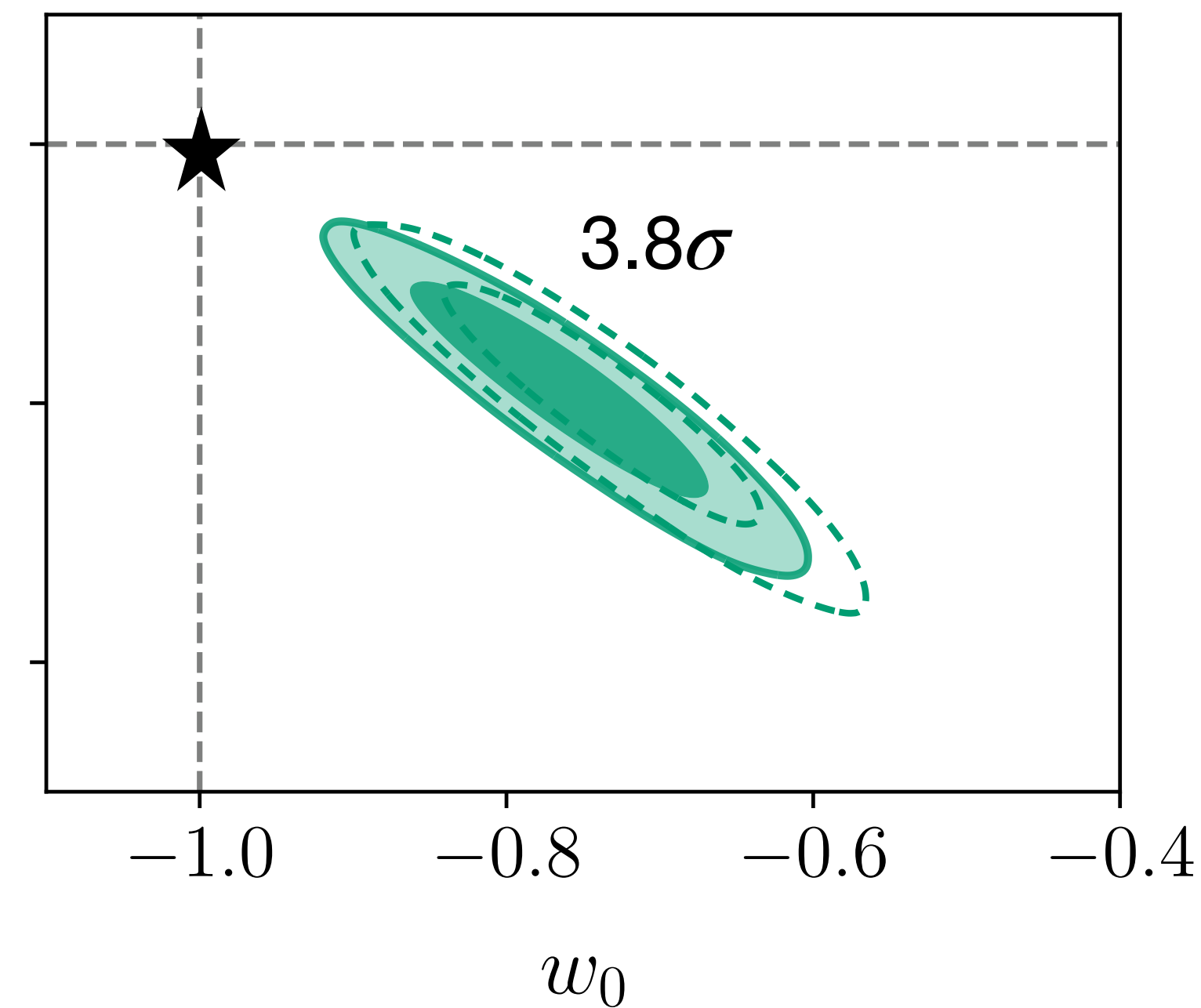
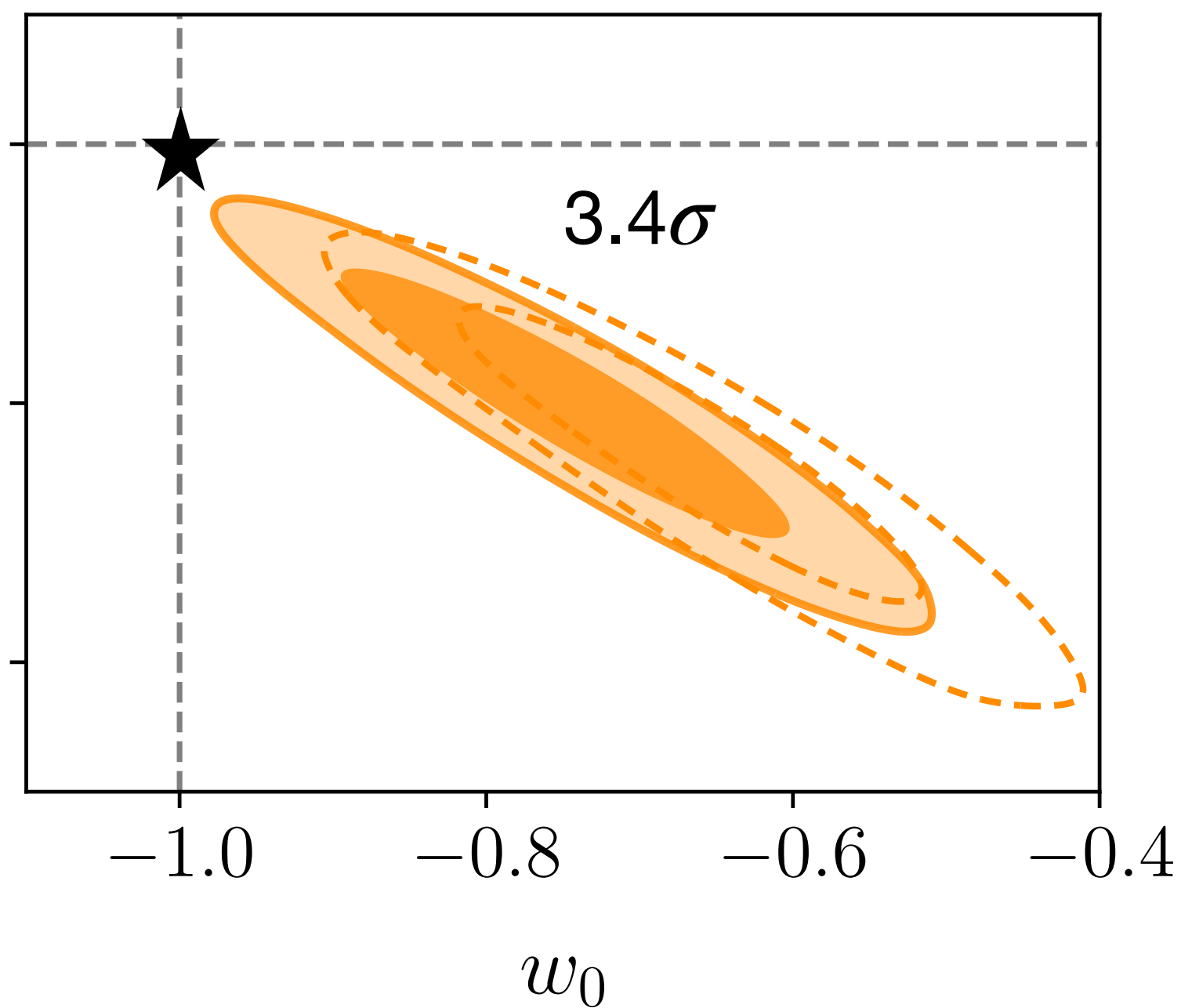
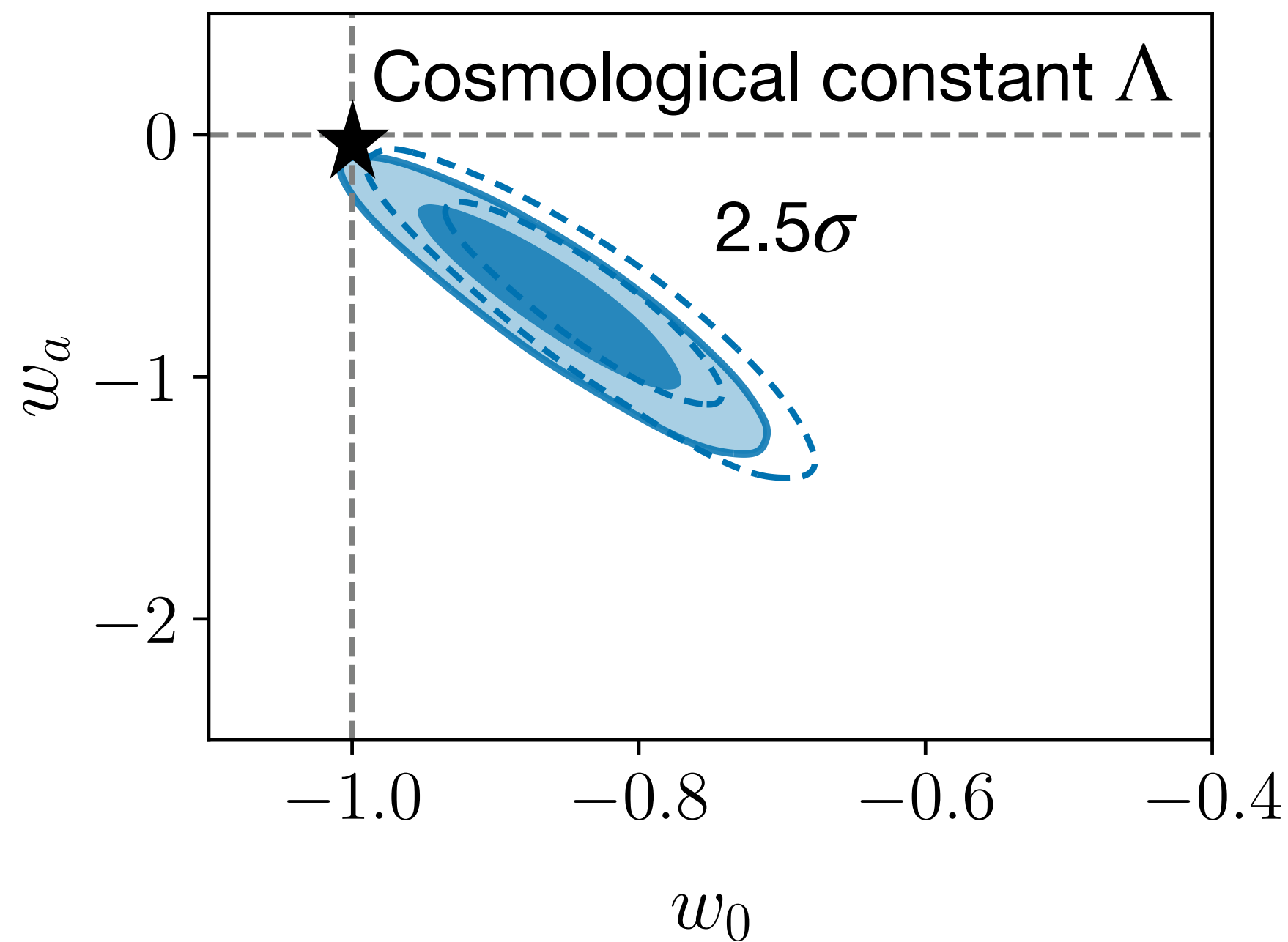
■ DESI (FS+BAO) + CMB + PantheonPlus

--- DESI (BAO) + CMB + Union3

■ DESI (FS+BAO) + CMB + Union3

--- DESI (BAO) + CMB + DES-SN5YR

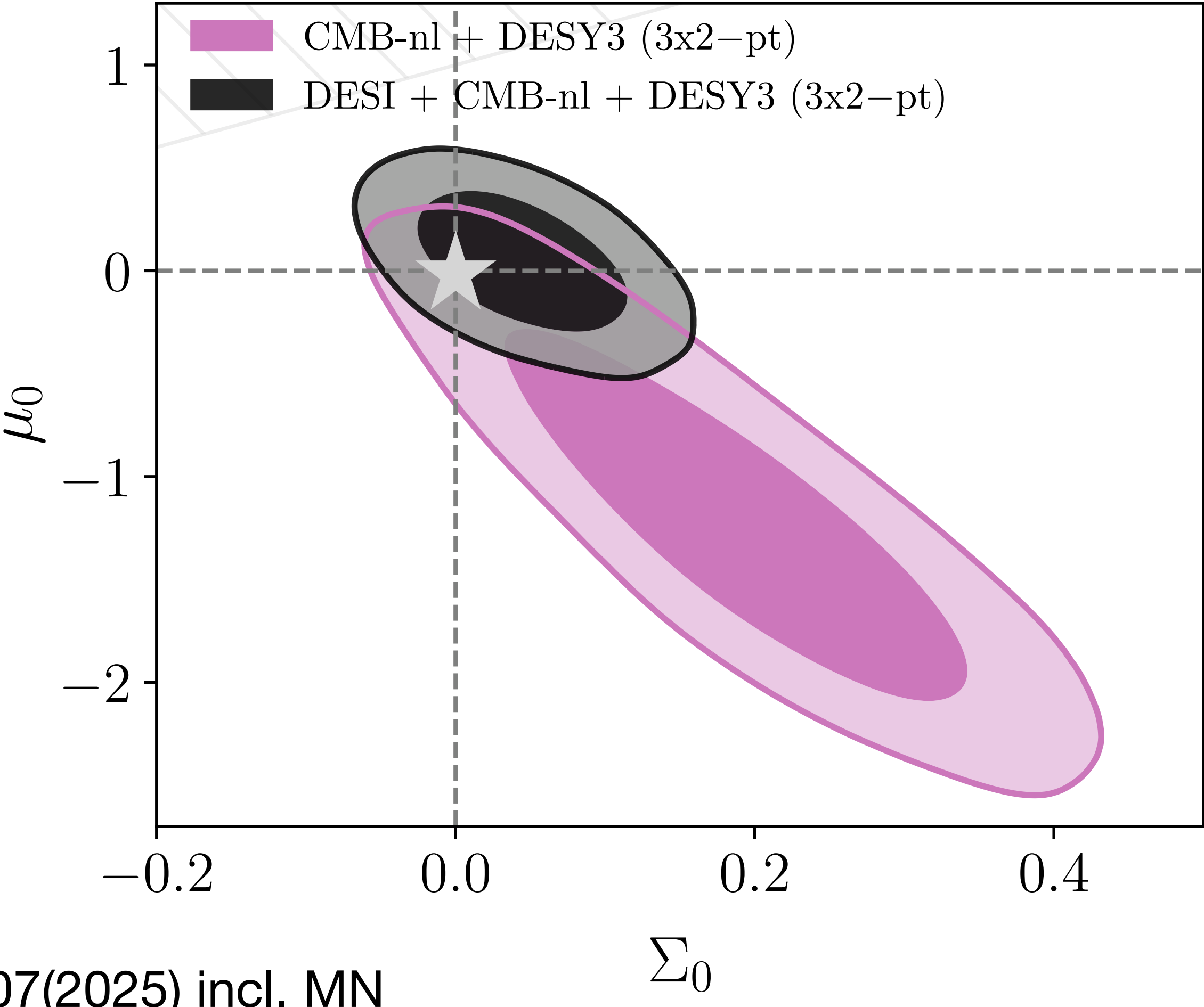
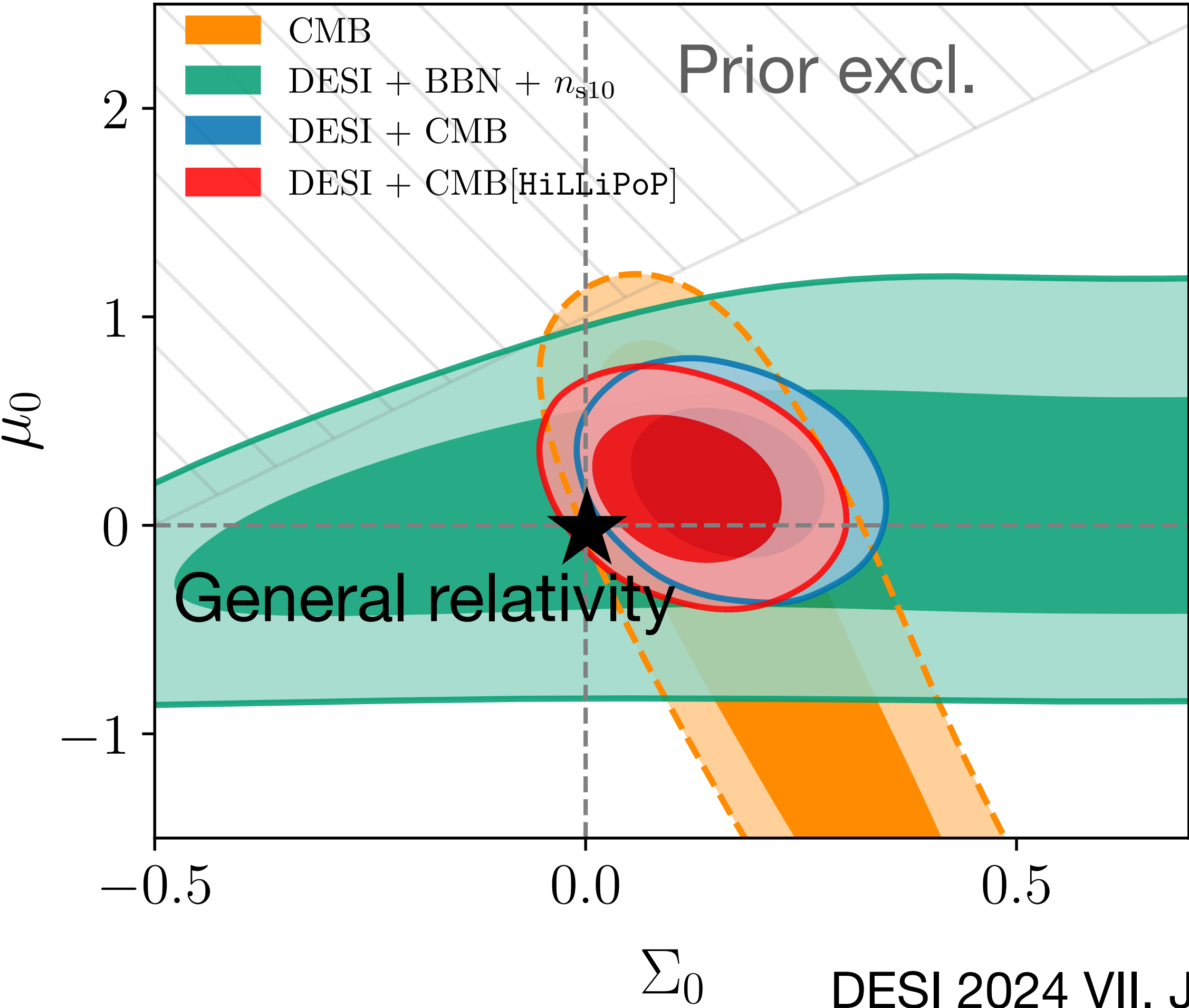
■ DESI (FS+BAO) + CMB + DES-SN5YR



Same conclusion at higher significance in DESI DR2 Results II, PRD 112, 083515

DESI DR1 results for beyond Λ CDM - modified gravity

No evidence for modified gravity beyond GR in (μ_0, Σ_0) extension



Field-level inference and new statistics of LSS

Beyond two-point statistics and beyond galaxy clustering

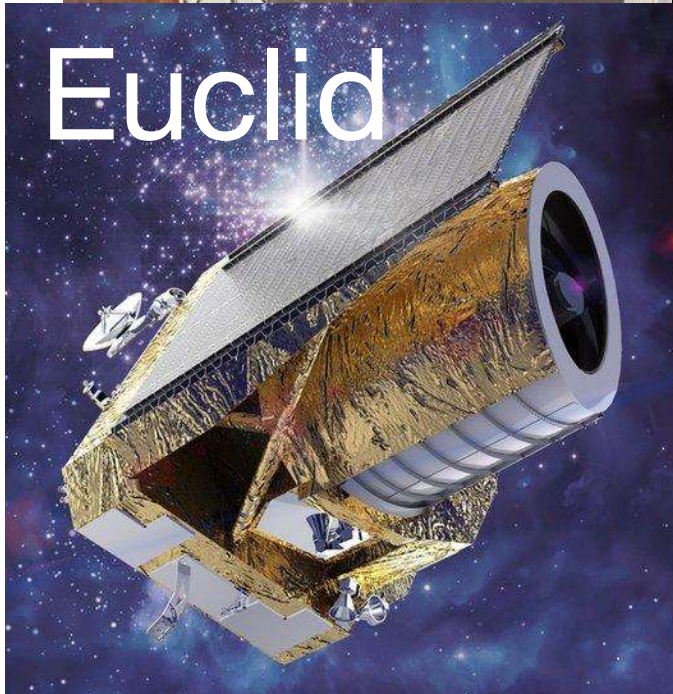
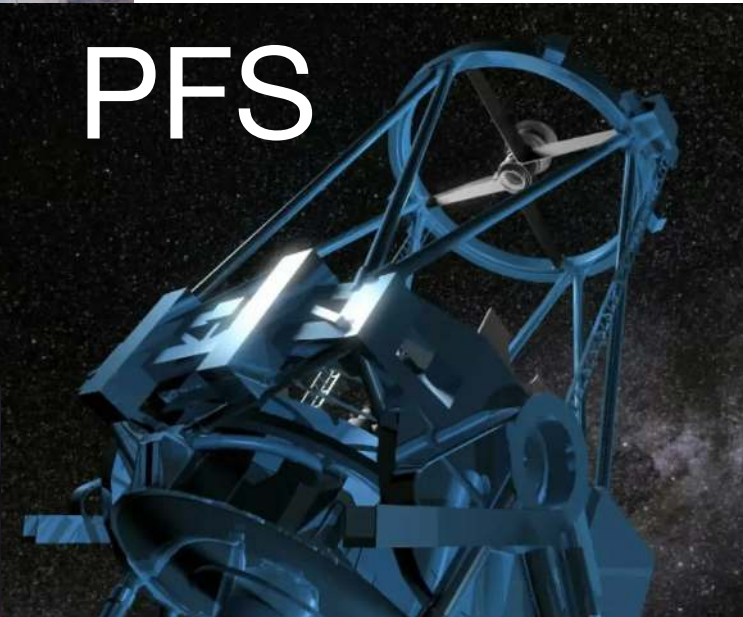


Credit: Dark Energy Spectroscopic Instrument

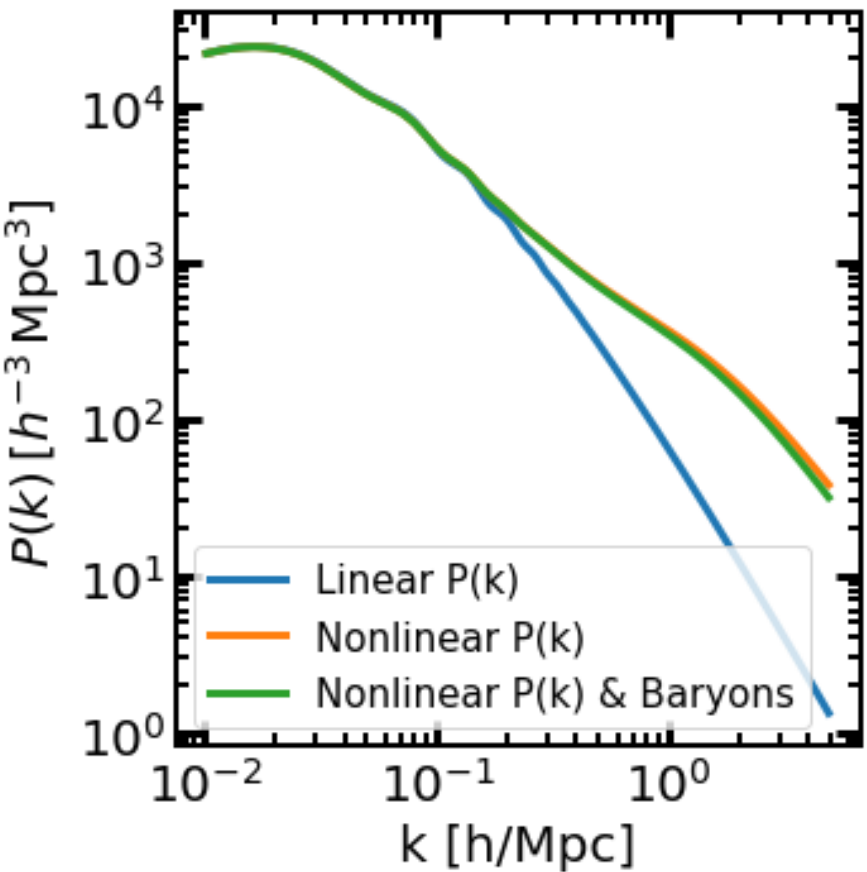
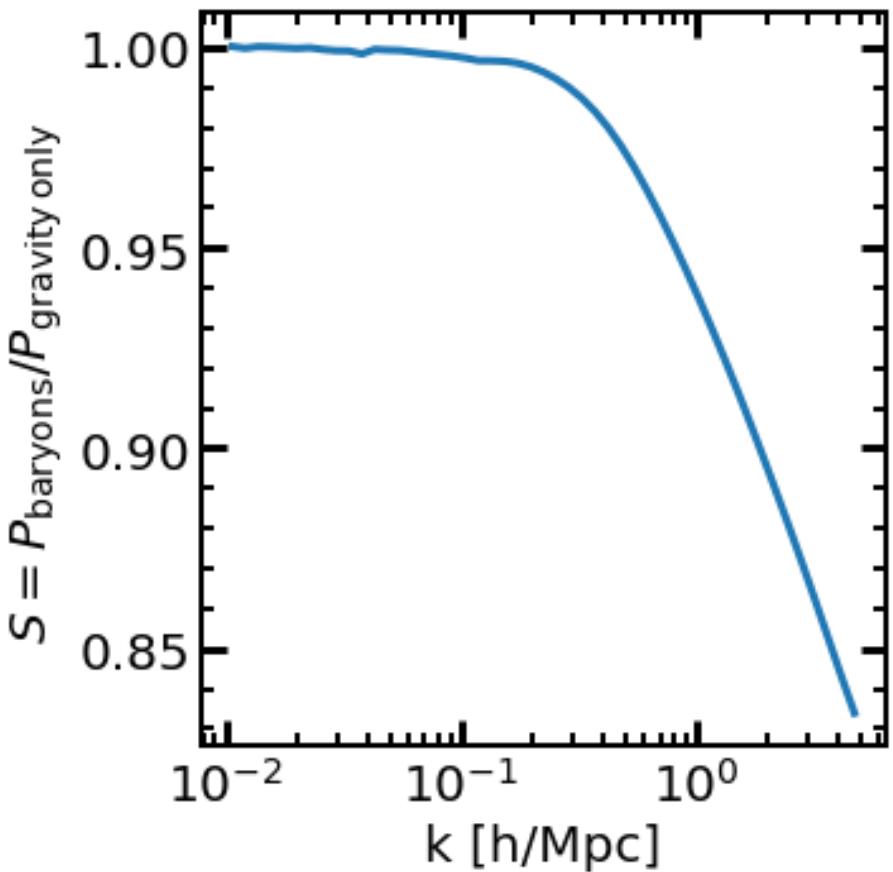
What else can we do without bigger telescopes and bigger sensors?

Diminishing returns

◆ We are here



LSS survey volume



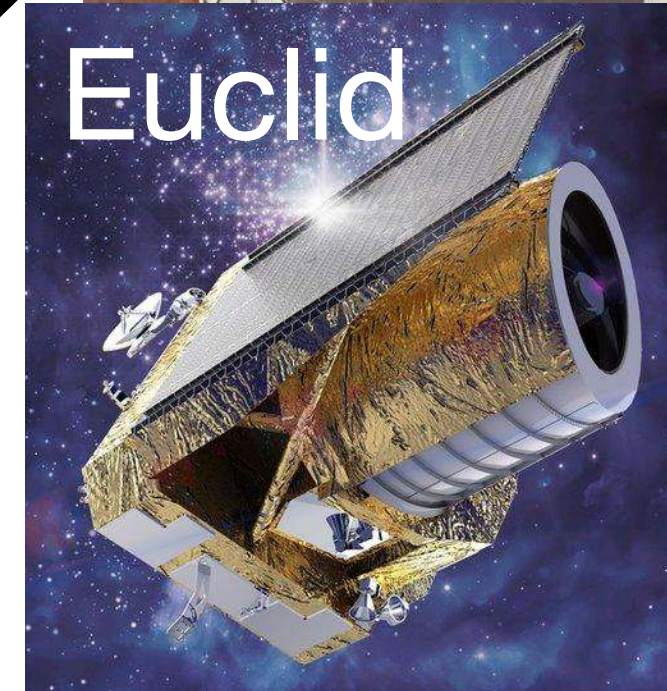
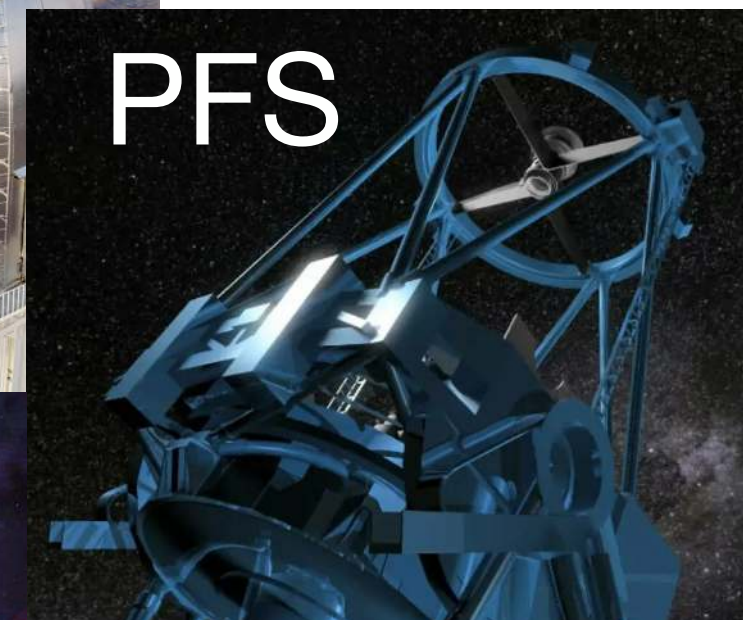
Credit: [BACCOemu](#)

LSS analysis cutoff scale

Astro complications

Diminishing returns

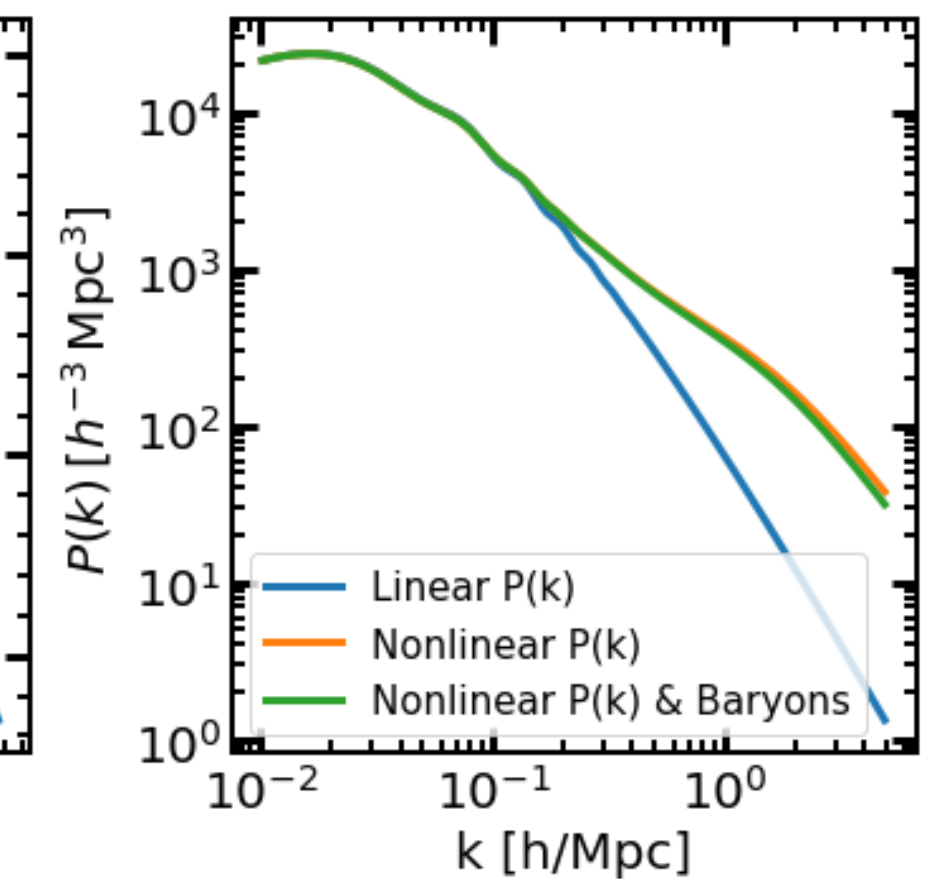
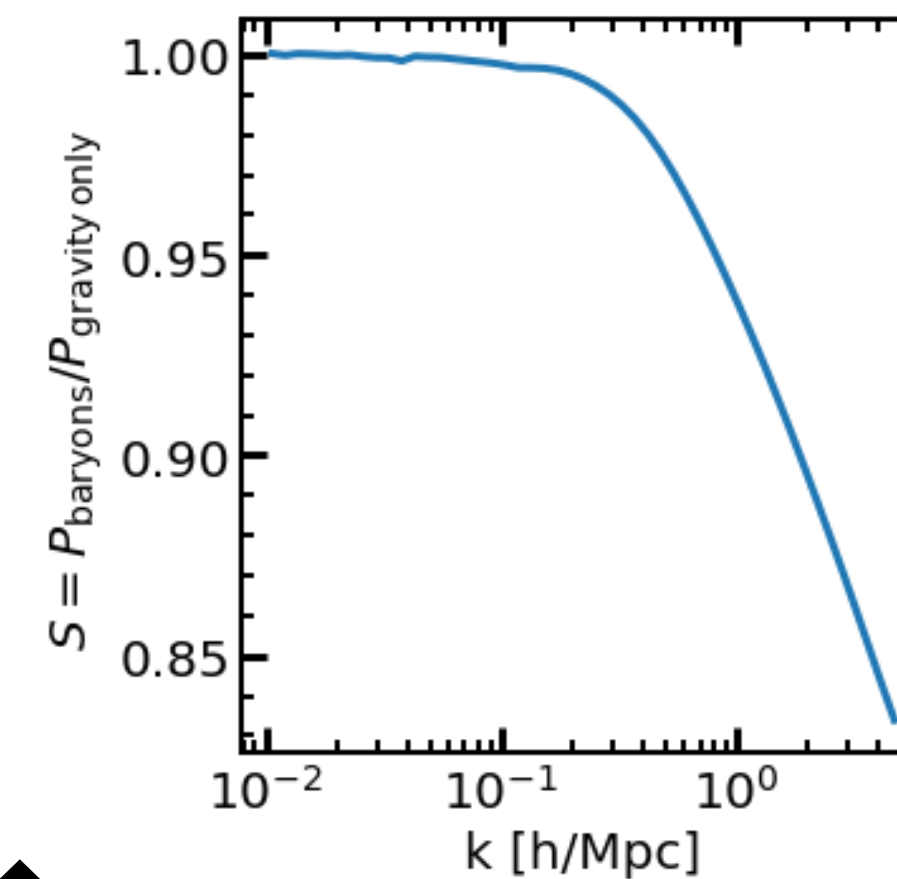
◆ We are here



LSS survey volume

← Under-explored dimension

LSS statistics



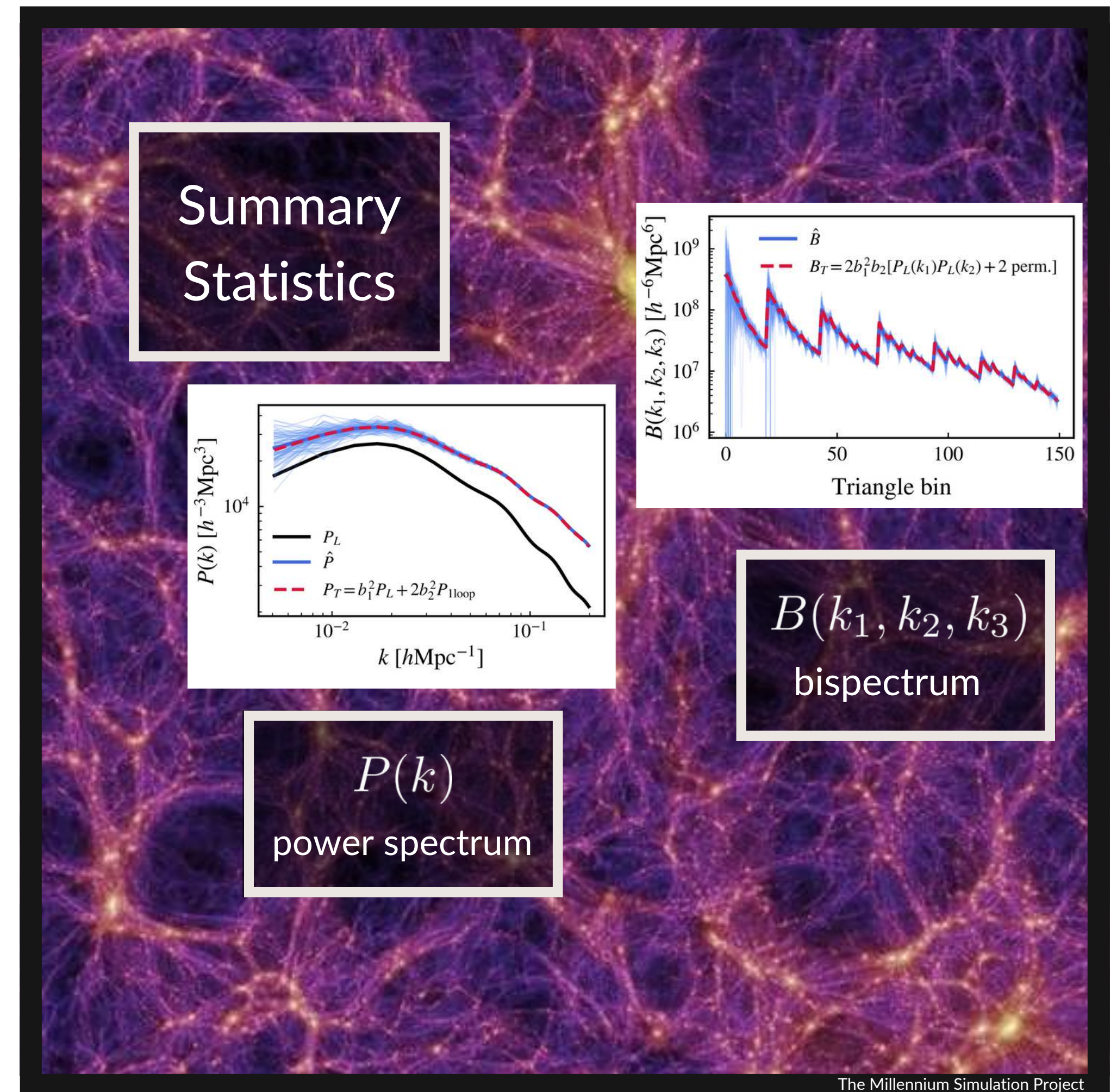
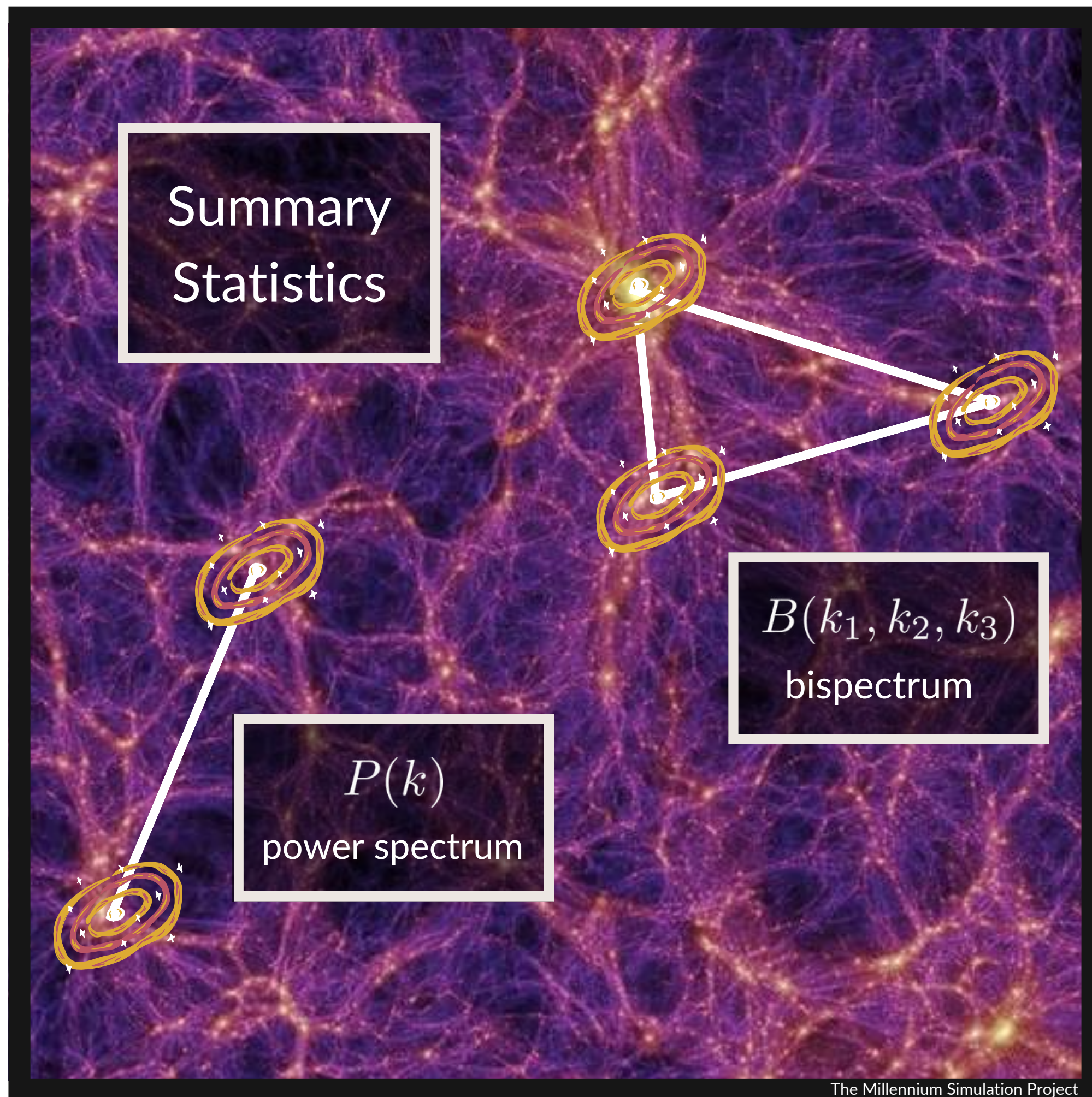
Credit: [BACCOemu](#)

LSS analysis cutoff scale

Astro complications

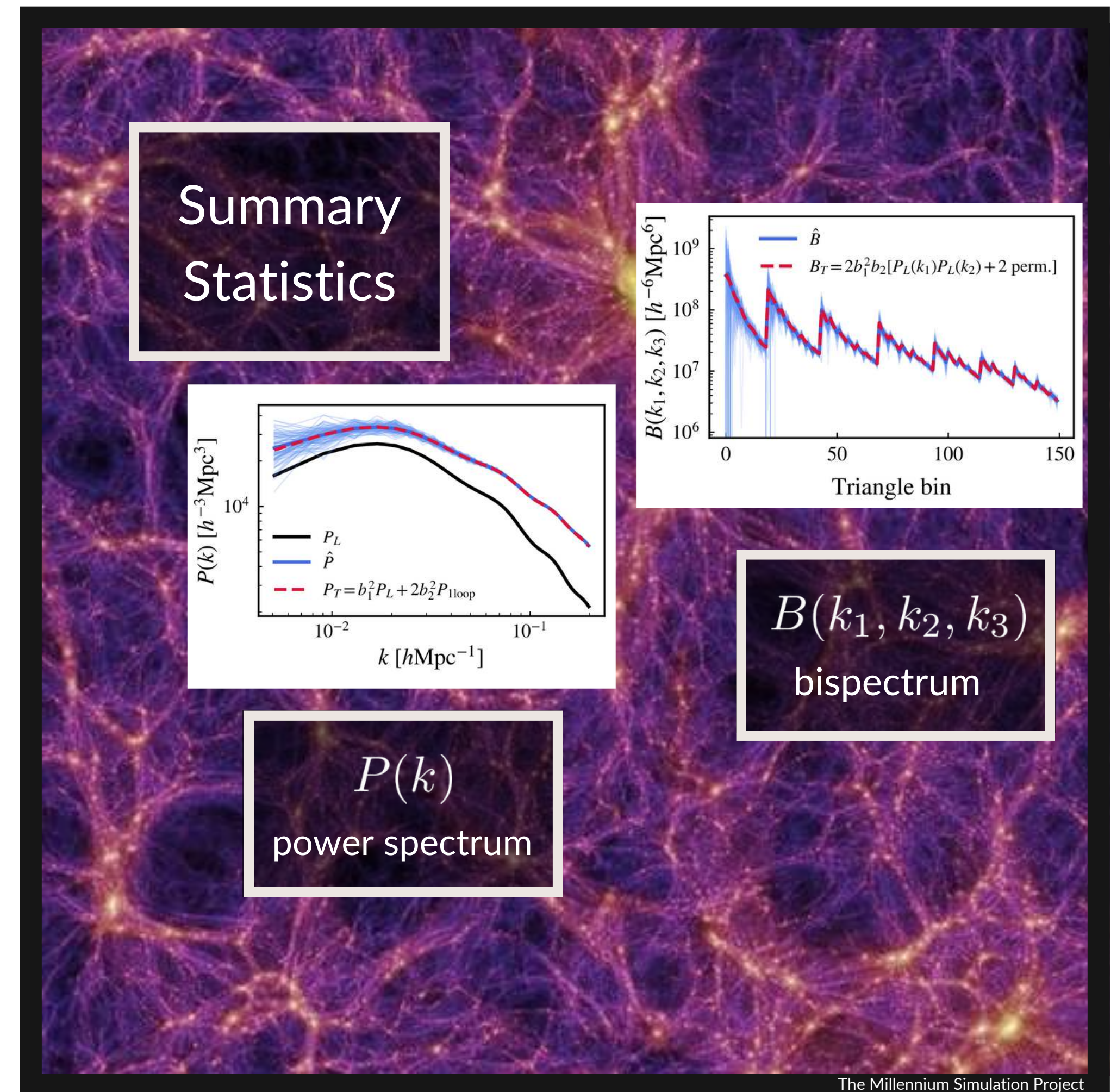
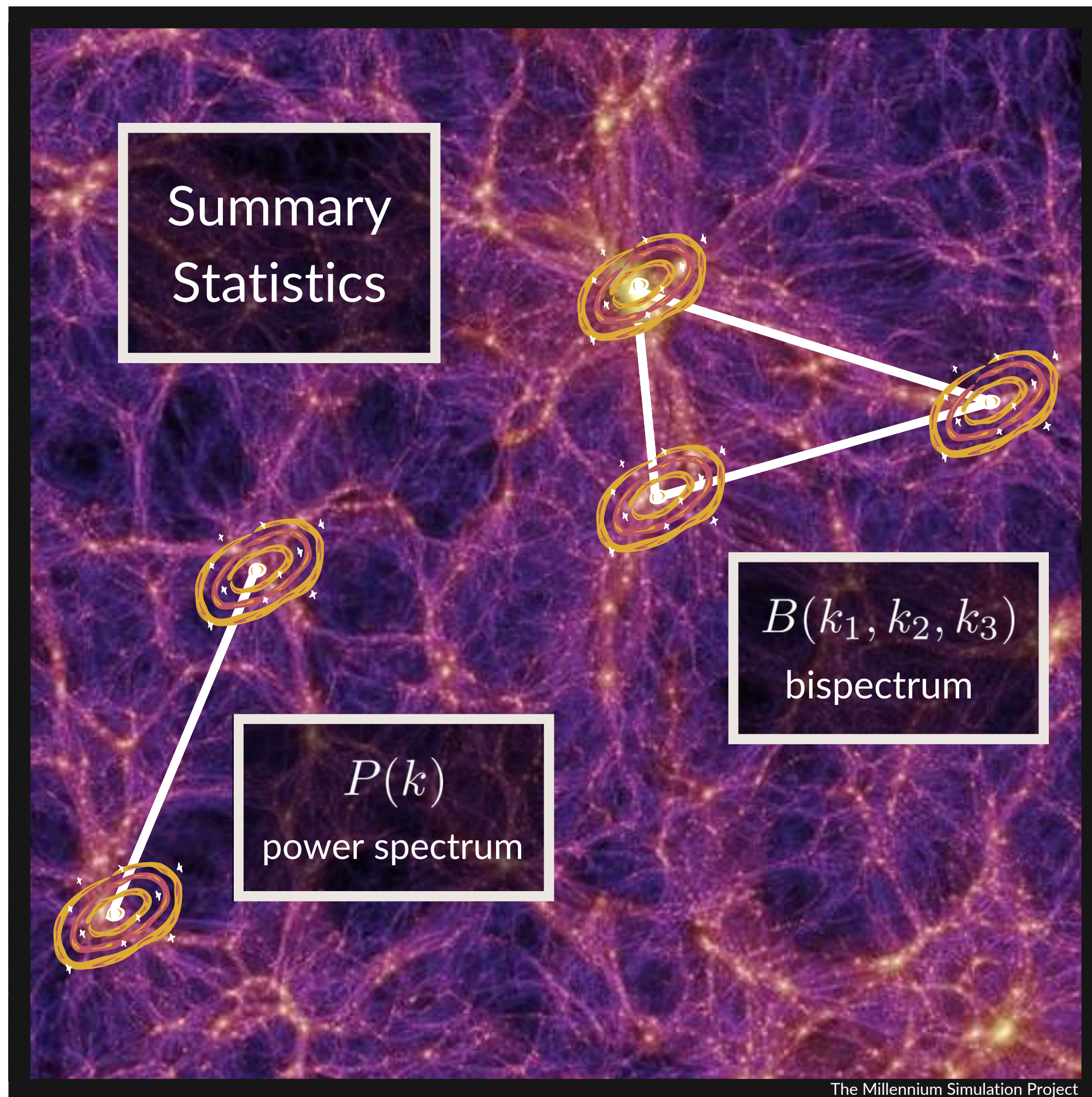
Beyond-two-point statistics = Three-point statistics?

Bispectrum probes triplets/triangles of galaxies adding higher-order information



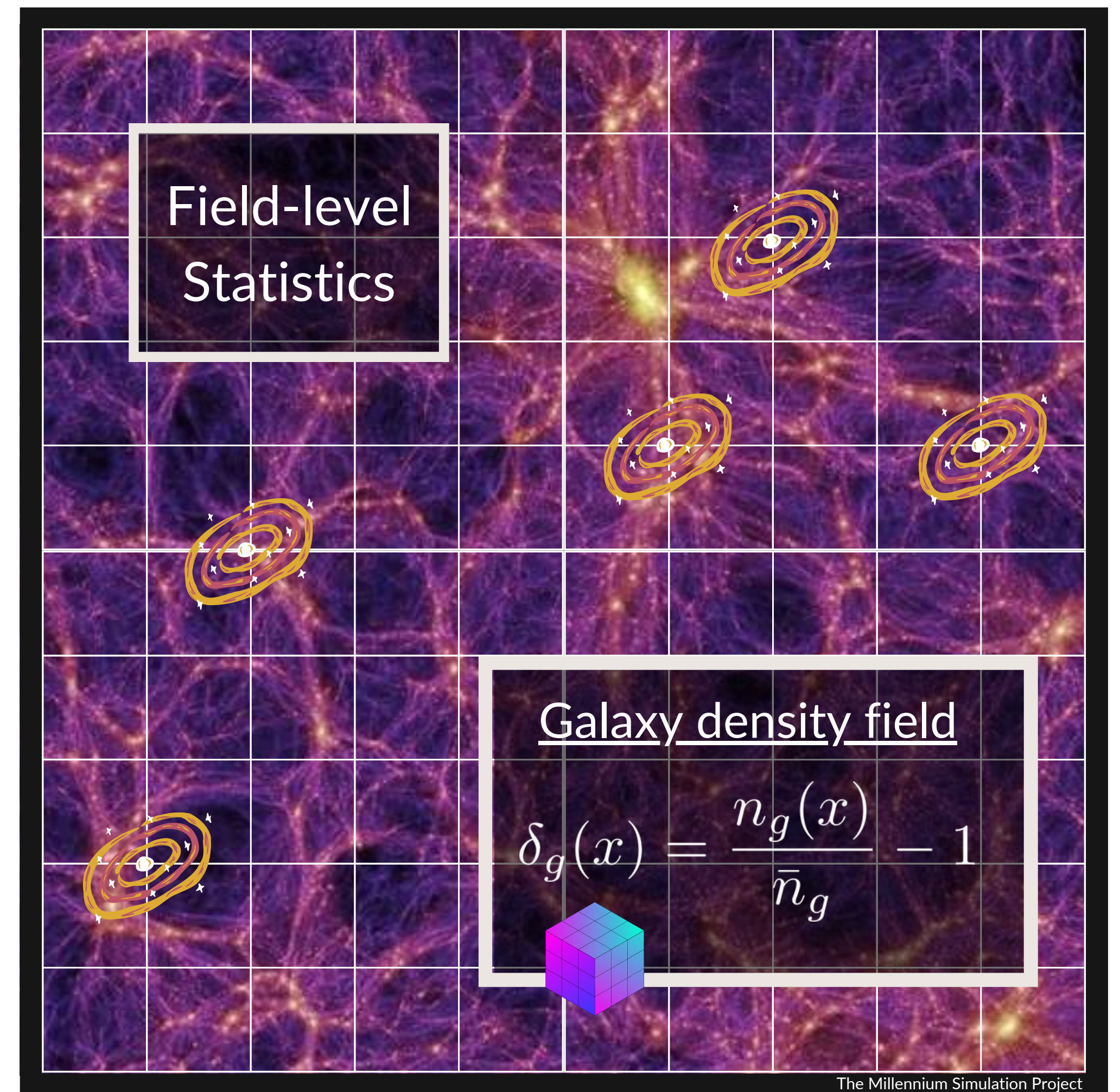
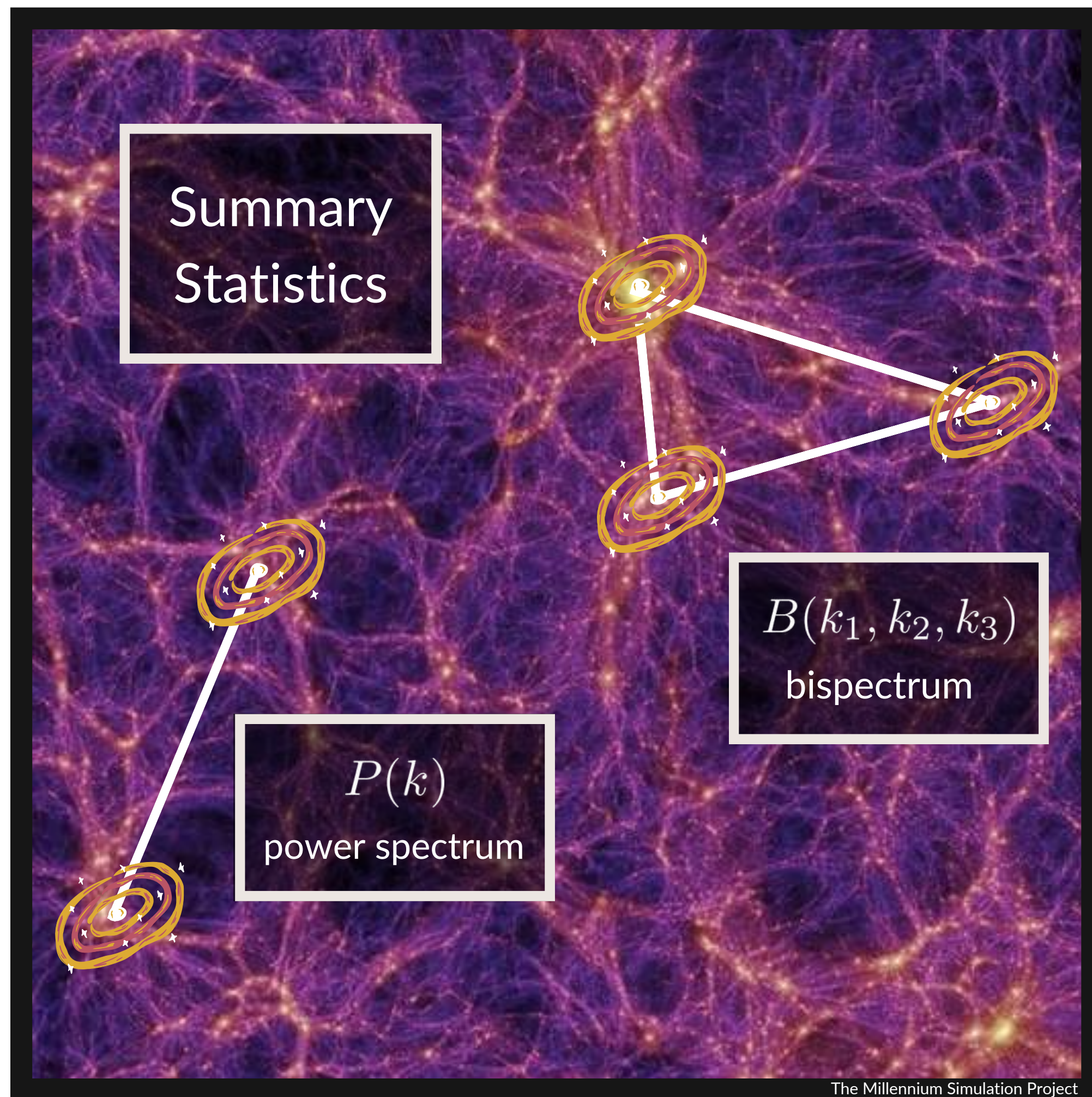
Beyond-two-point statistics = Three-point statistics?

Bispectrum probes triplets/triangles of galaxies adding higher-order information

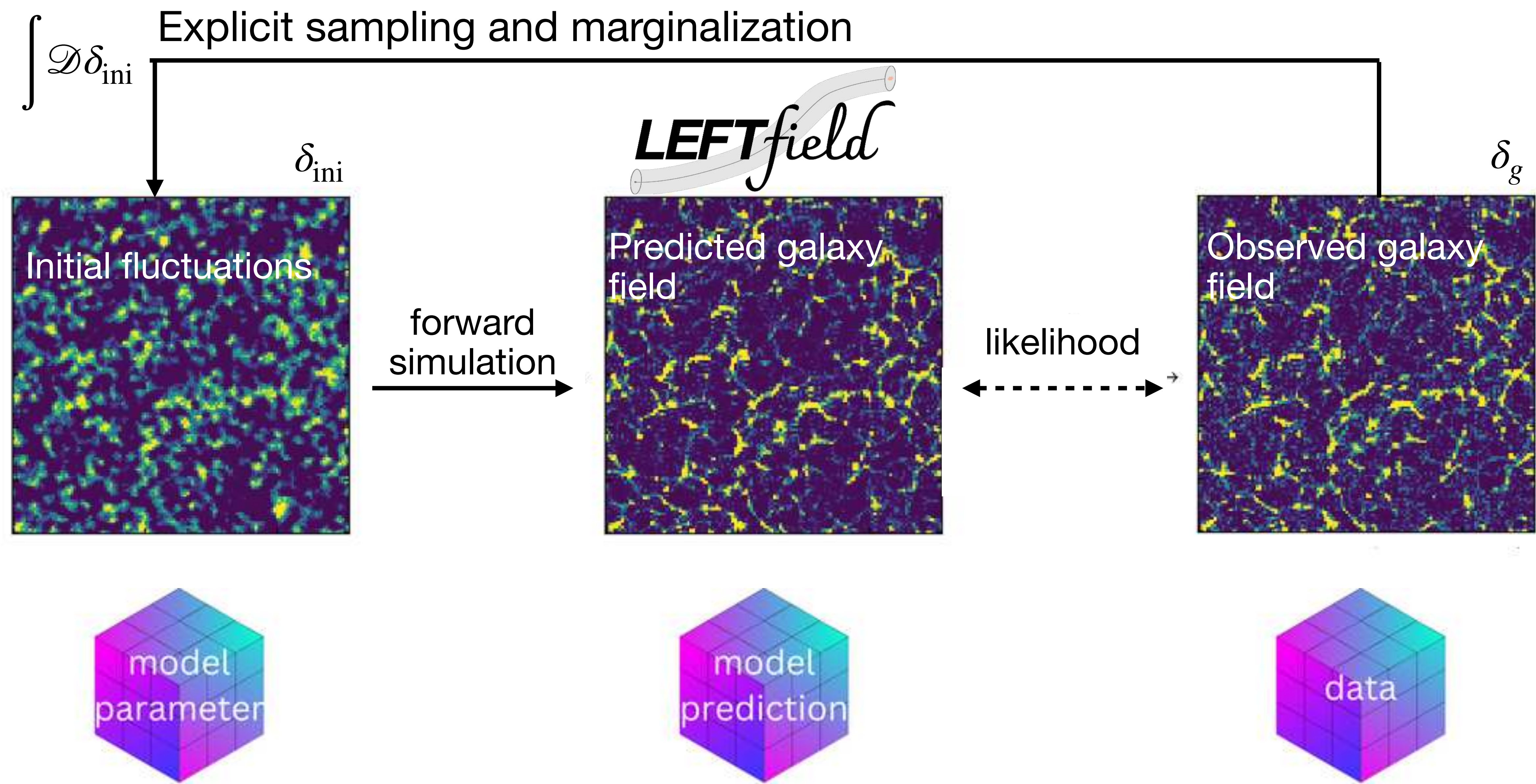


Field-level inference - rethinking how we analyze the data

Summary statistics can be lossy, can we directly analyze the data at the field level?



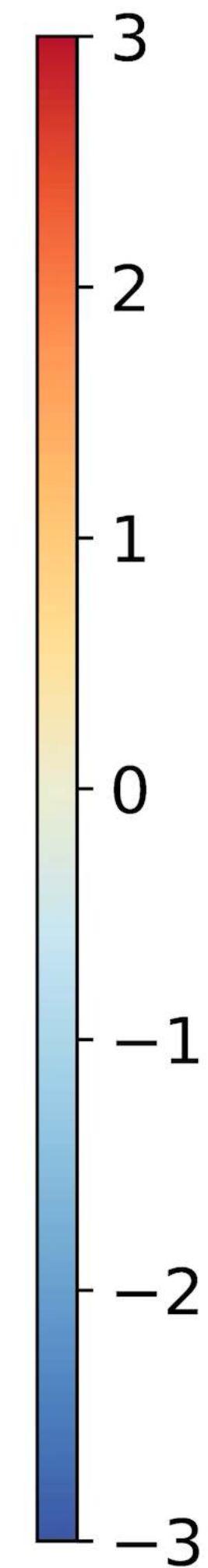
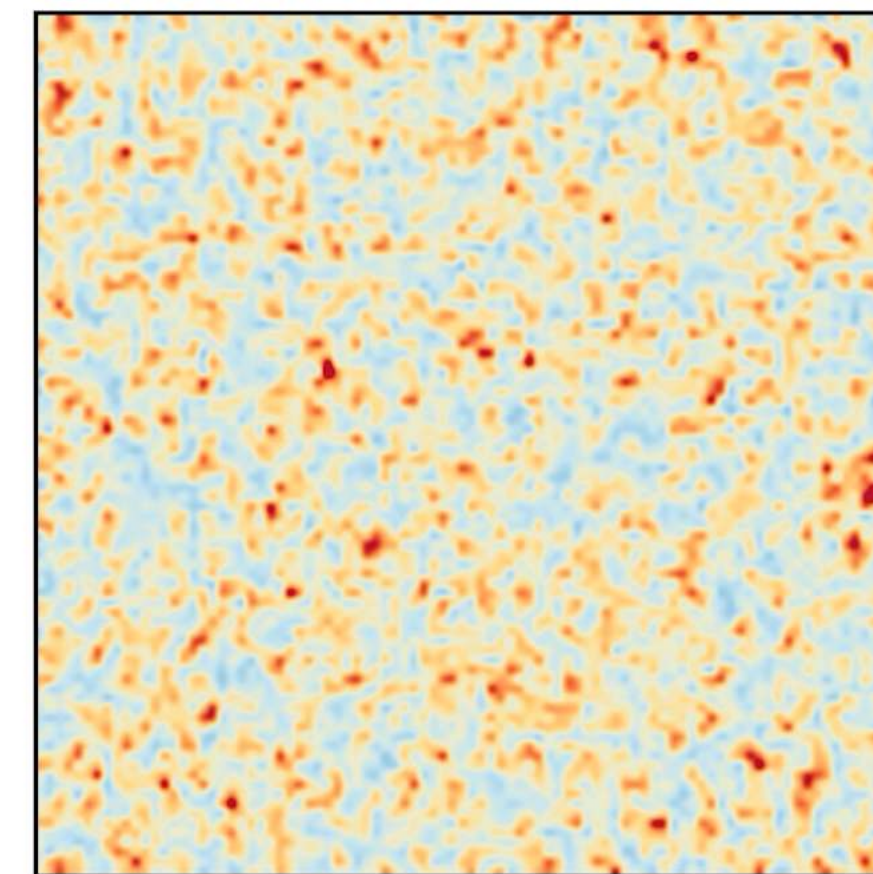
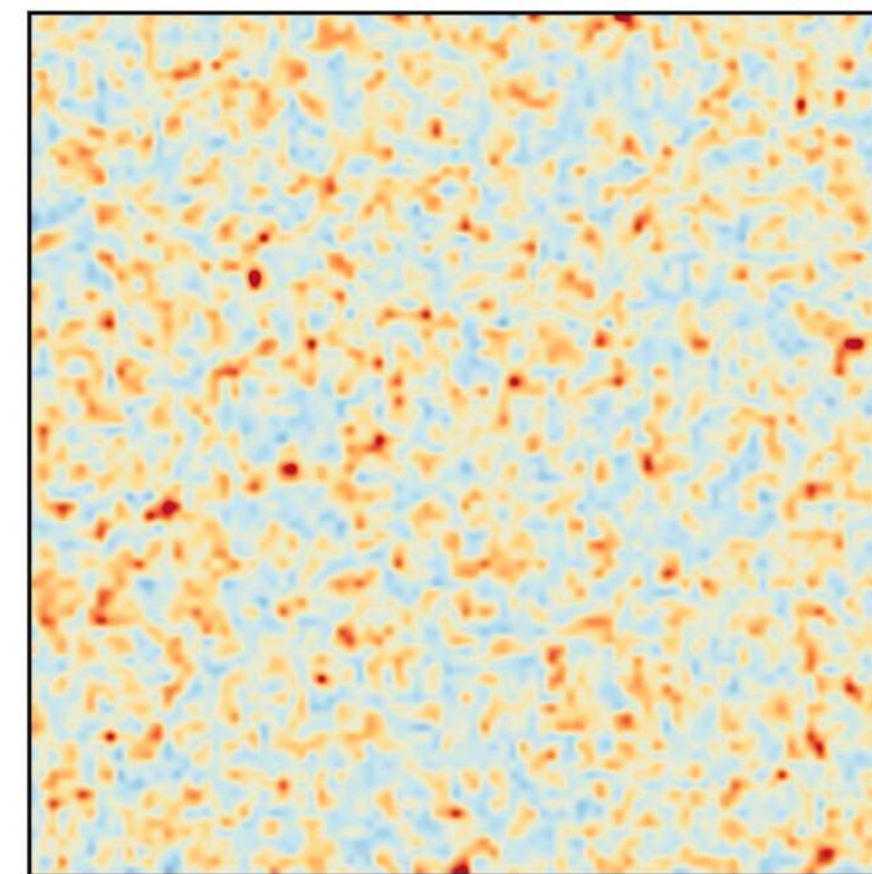
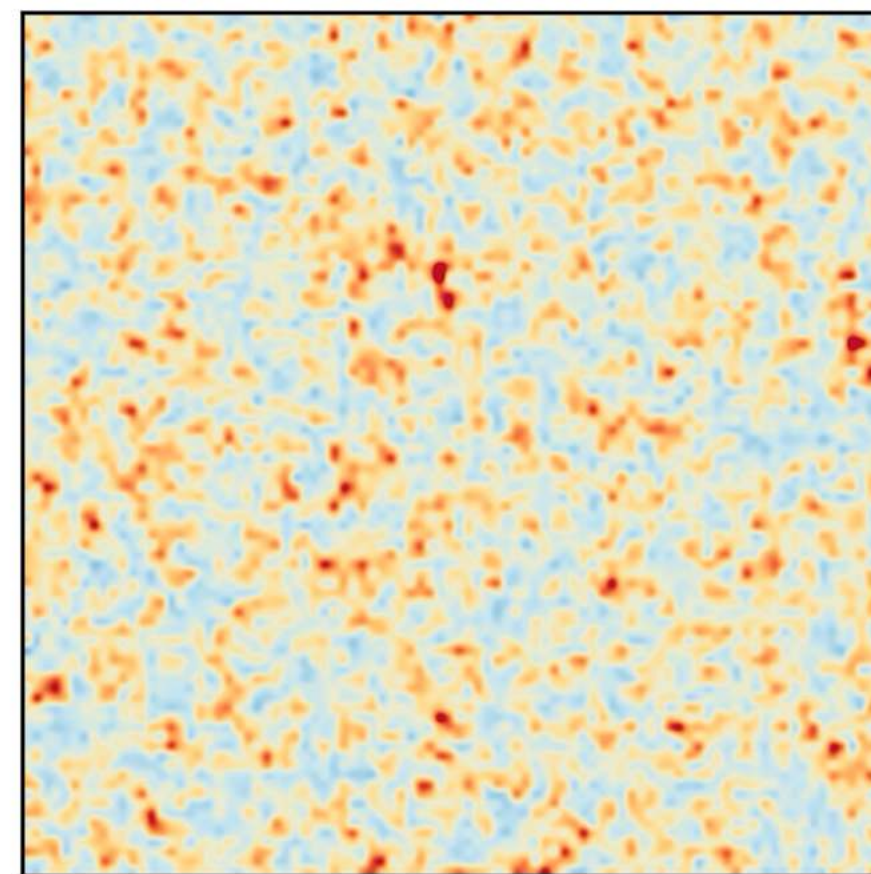
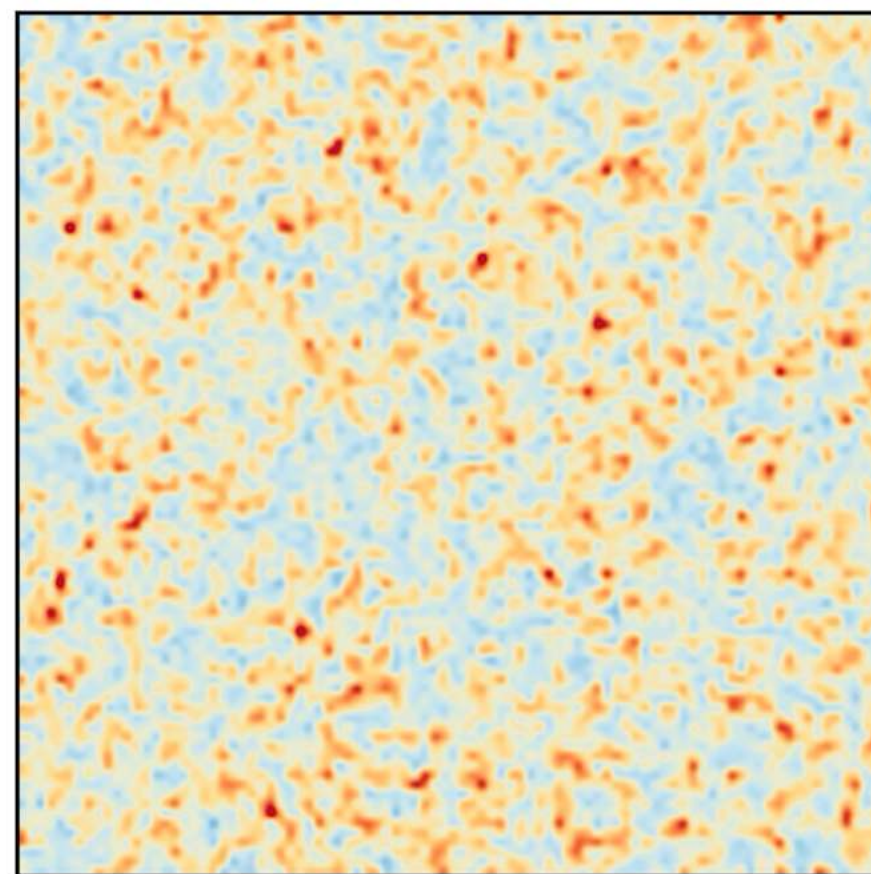
Field-level inference - rethinking how we analyze the data



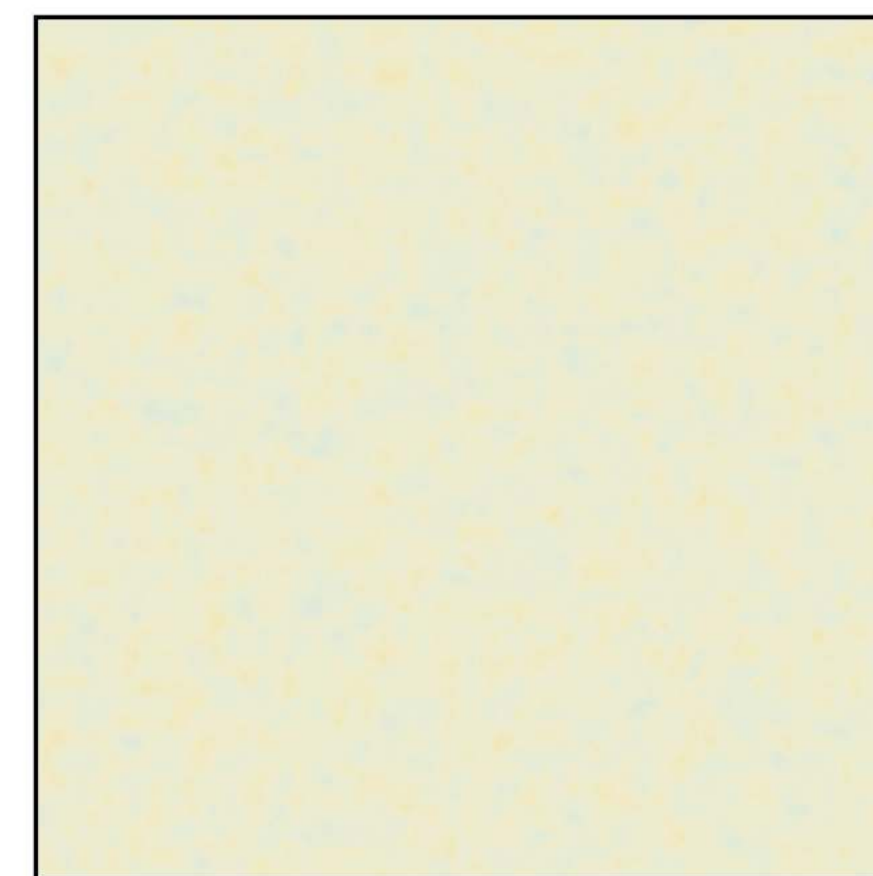
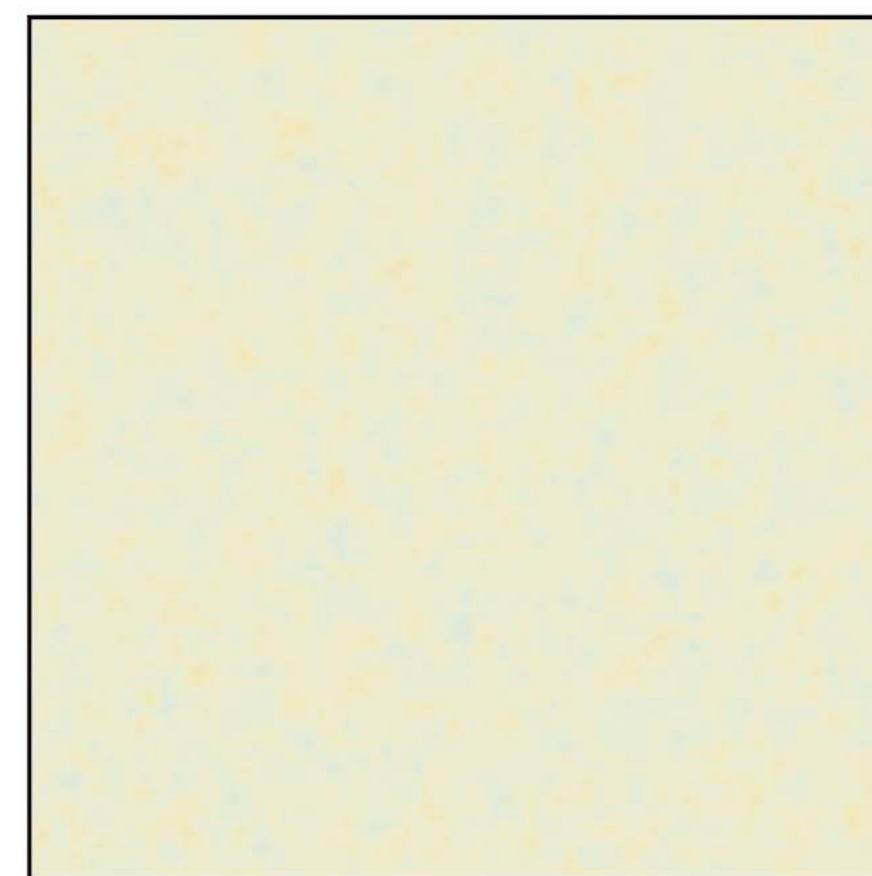
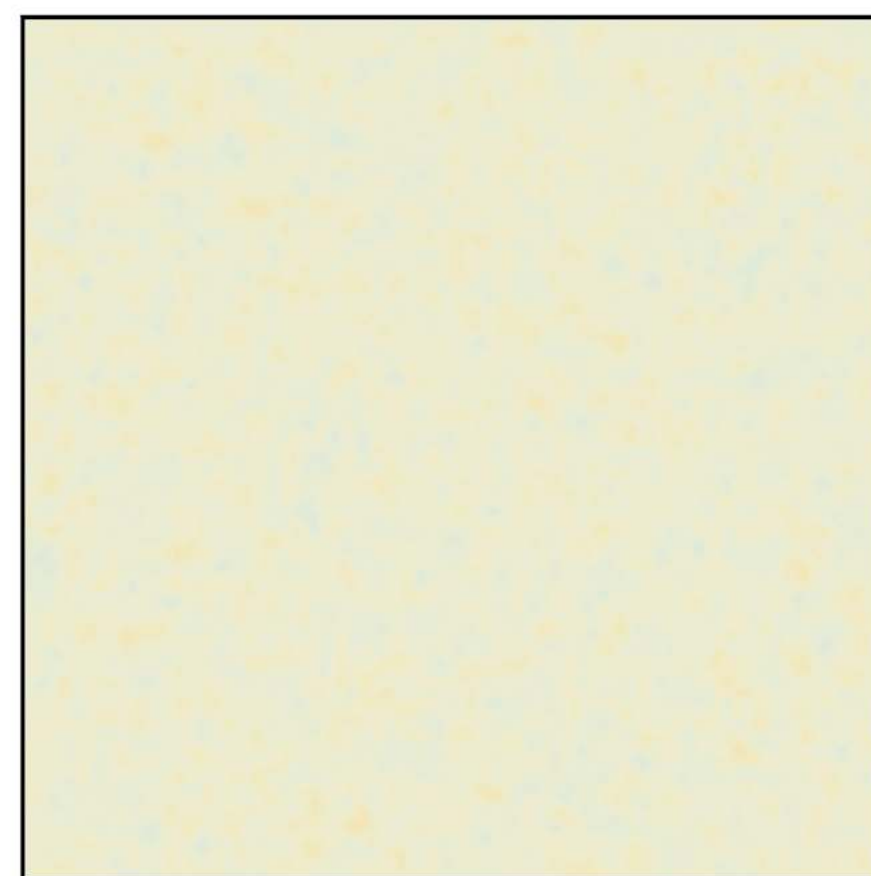
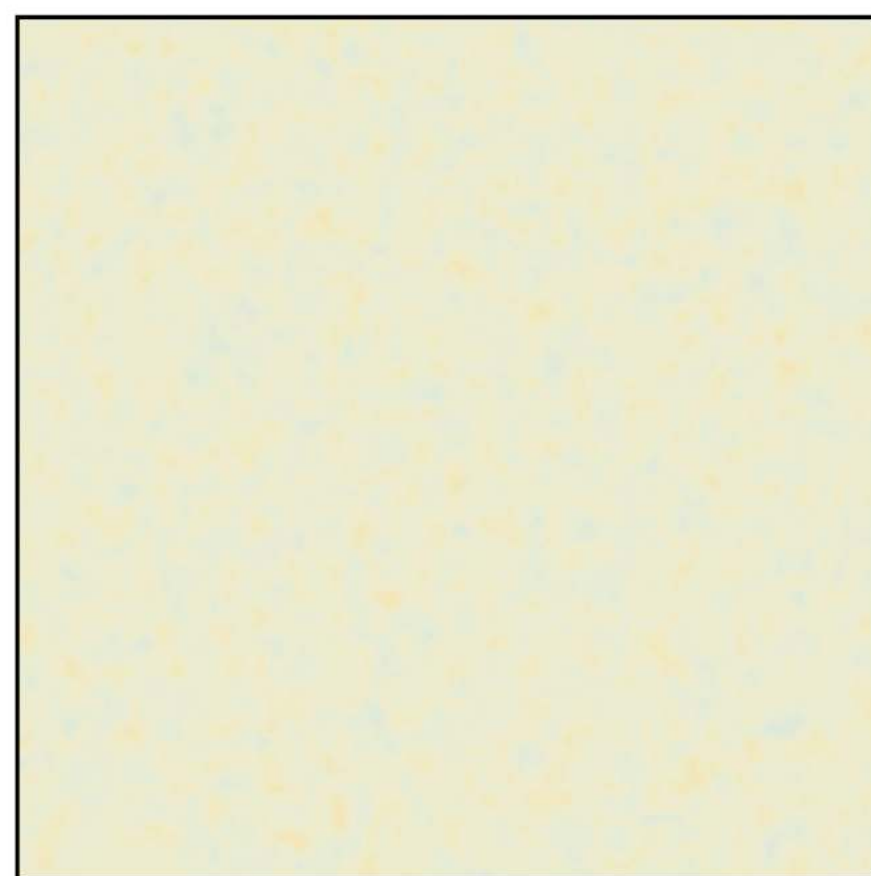
likelihood

$$\log \mathcal{L} = -1.184e+08$$

data



model
prediction



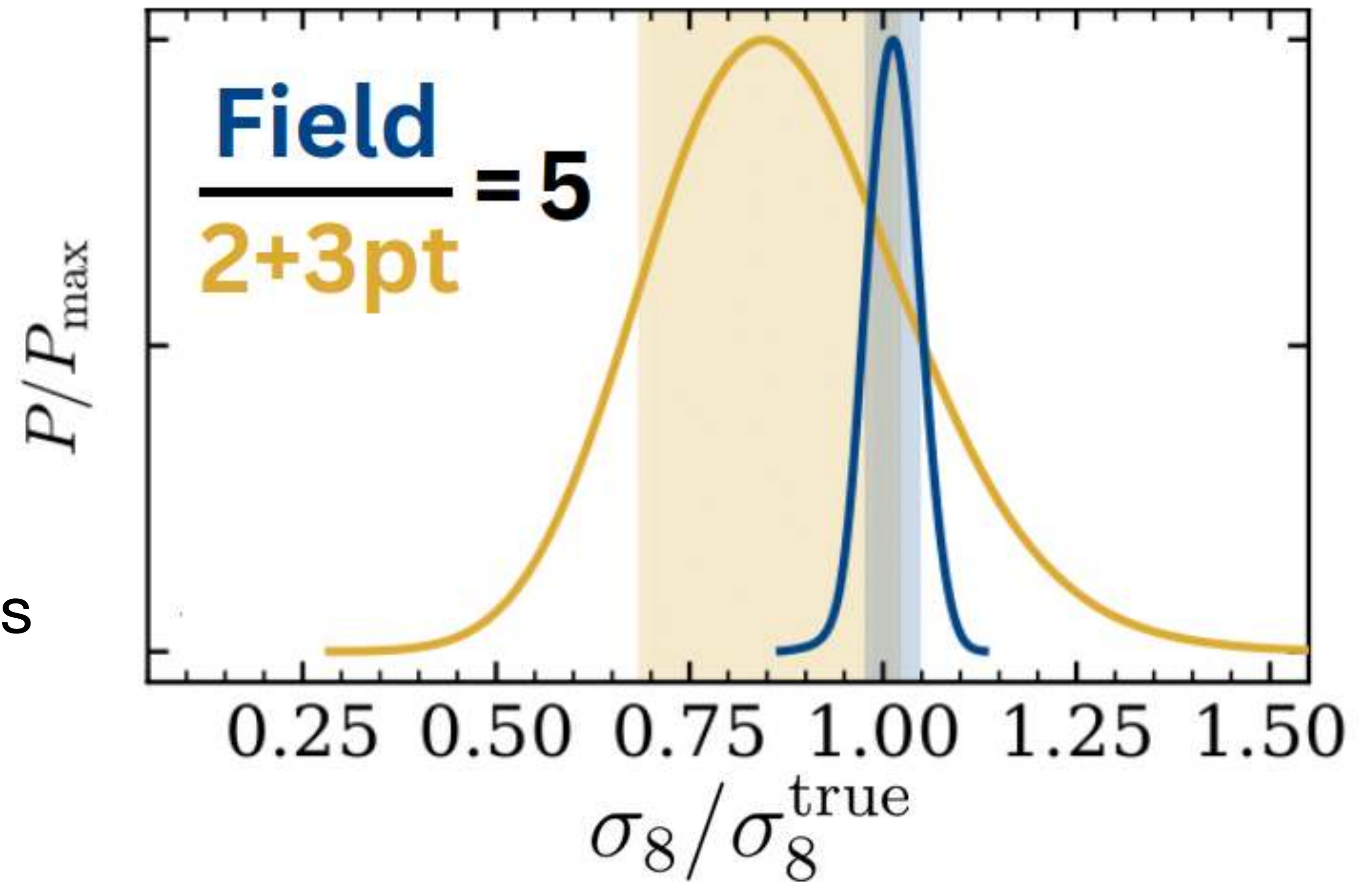
2+3-point (P+B) vs. Field-level inference comparison

Apple-to-apple comparison on

N-body halo catalogs

no redshift space distortion

conservative analysis scale cuts



Effectively x25 survey volume!

MN+2024 PRL 133, 221006

but see also Akitsu+2025

Public data challenge for novel beyond-two-point statistics to recover true cosmology from blind analyses

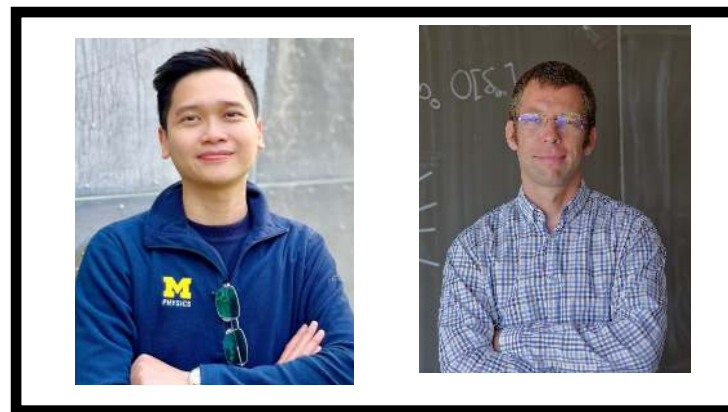
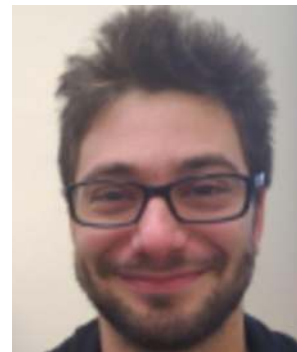
Beyond-2pt Collaboration, ApJ 990 99

incl. MN

A Parameter-Masked Mock Data Challenge for Beyond-Two-Point Galaxy Clustering Statistics*

THE BEYOND-2PT COLLABORATION

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CHIRAG MODI,^{22, 23} NHAT-MINH NGUYEN,^{24, 25} TAKAHIRO NISHIMICHI,^{2, 26, 27} ENRIQUE PAILLAS,^{28, 29}
MARCOS PELLEJERO IBAÑEZ,³⁰ OLIVER H. E. PHILCOX,^{31, 32} ALICE PISANI,^{33, 22, 34, 17} FABIAN SCHMIDT,³⁵
SATOSHI TANAKA,²⁶ GIOVANNI VERZA,^{36, 22} SIHAN YUAN,^{4, 6} MATTEO ZENNARO,³⁷



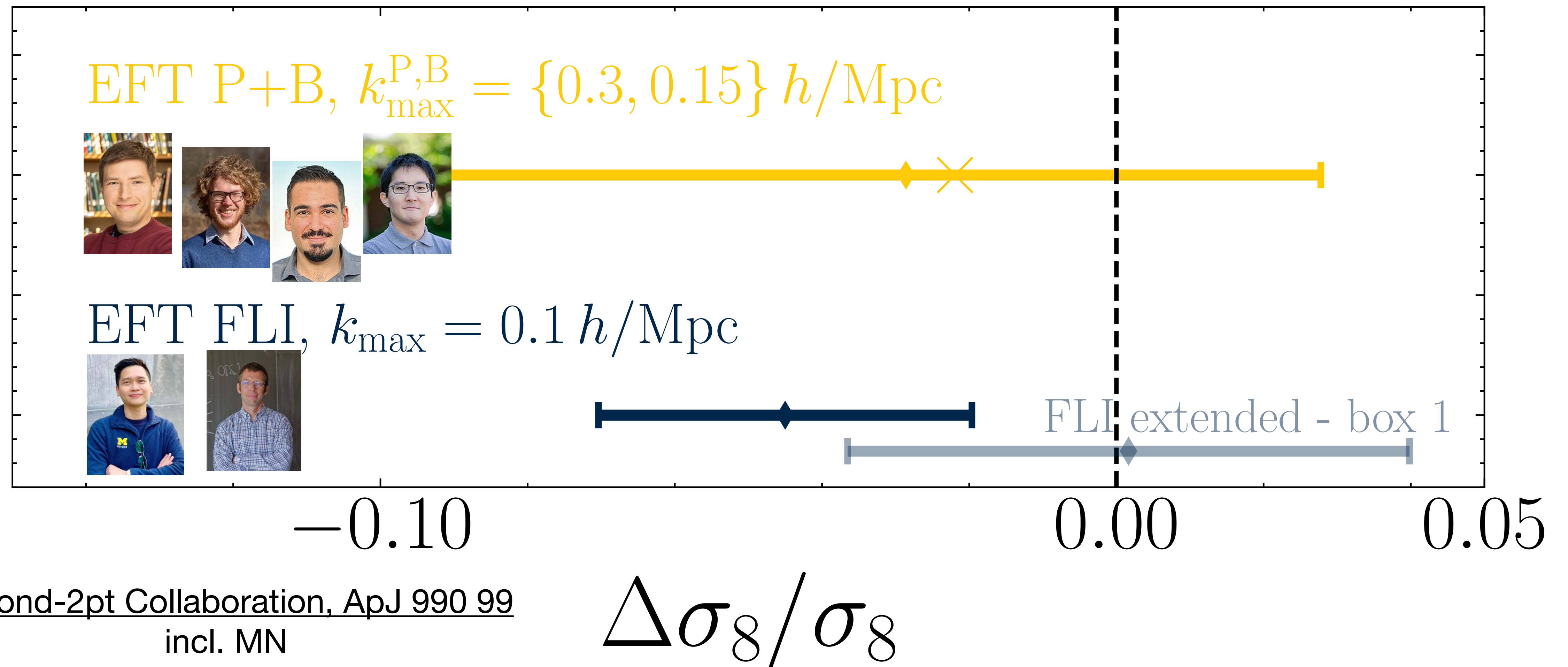
Challenge organizers



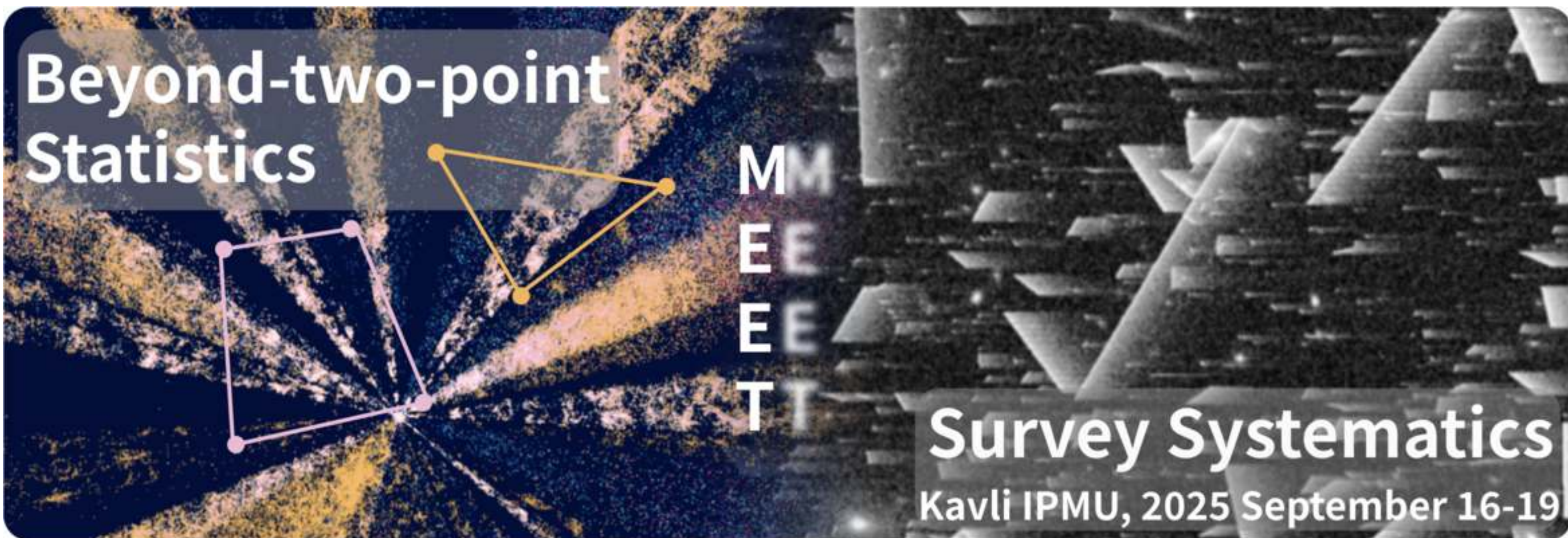
Our team

P+B vs FLI on HOD mocks in the beyond-2point blind data challenge

real-space snapshots (mean of 10 realizations), fixed $\omega_m, \omega_b, n_s, h$



New physics or systematics? The beyond-2pt community will be ready to answer that



~70 participants, mostly overseas
postdocs > PhDs > faculties



New maps of systematics

New models for systematics

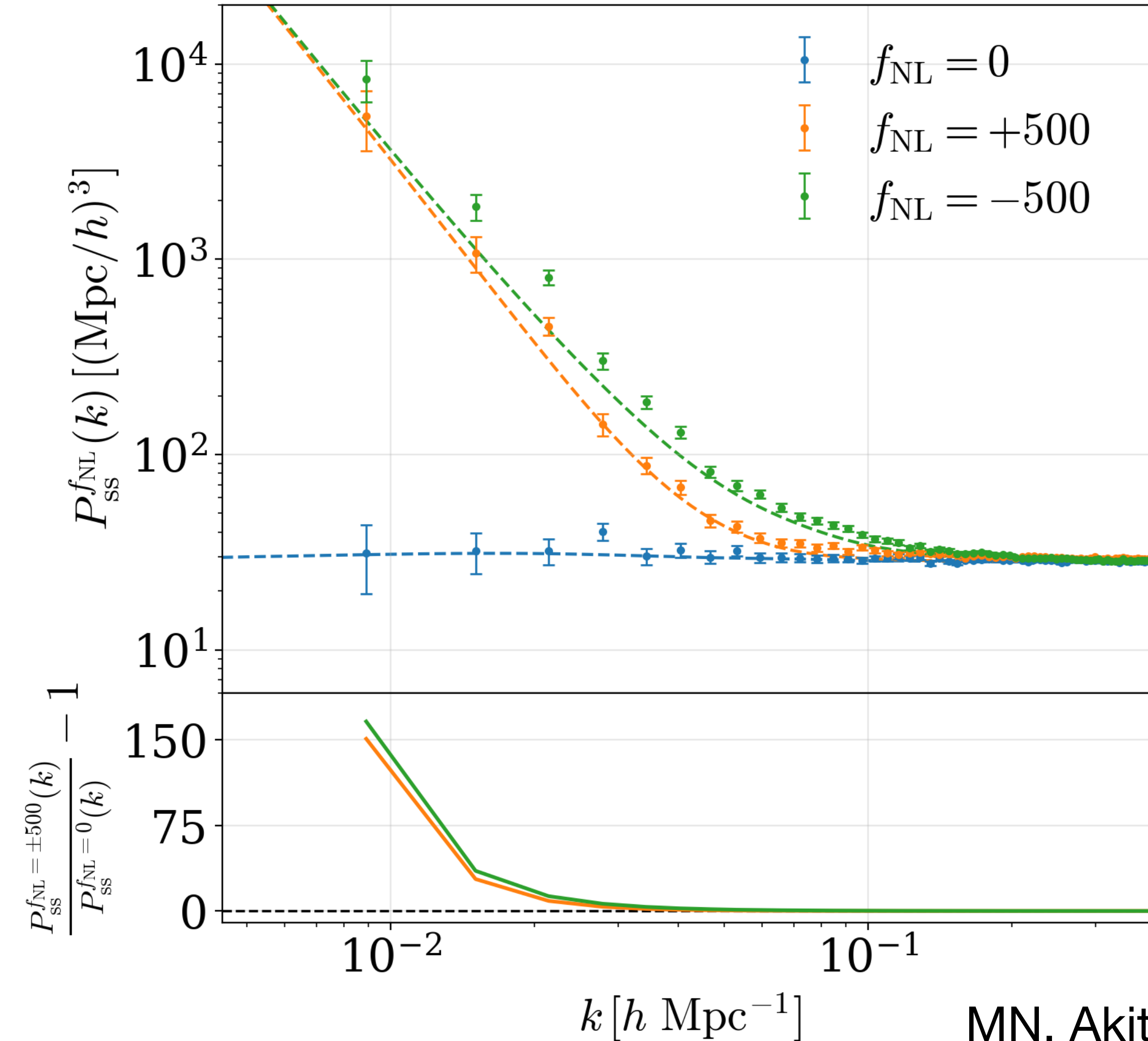


Standardize validation schemes

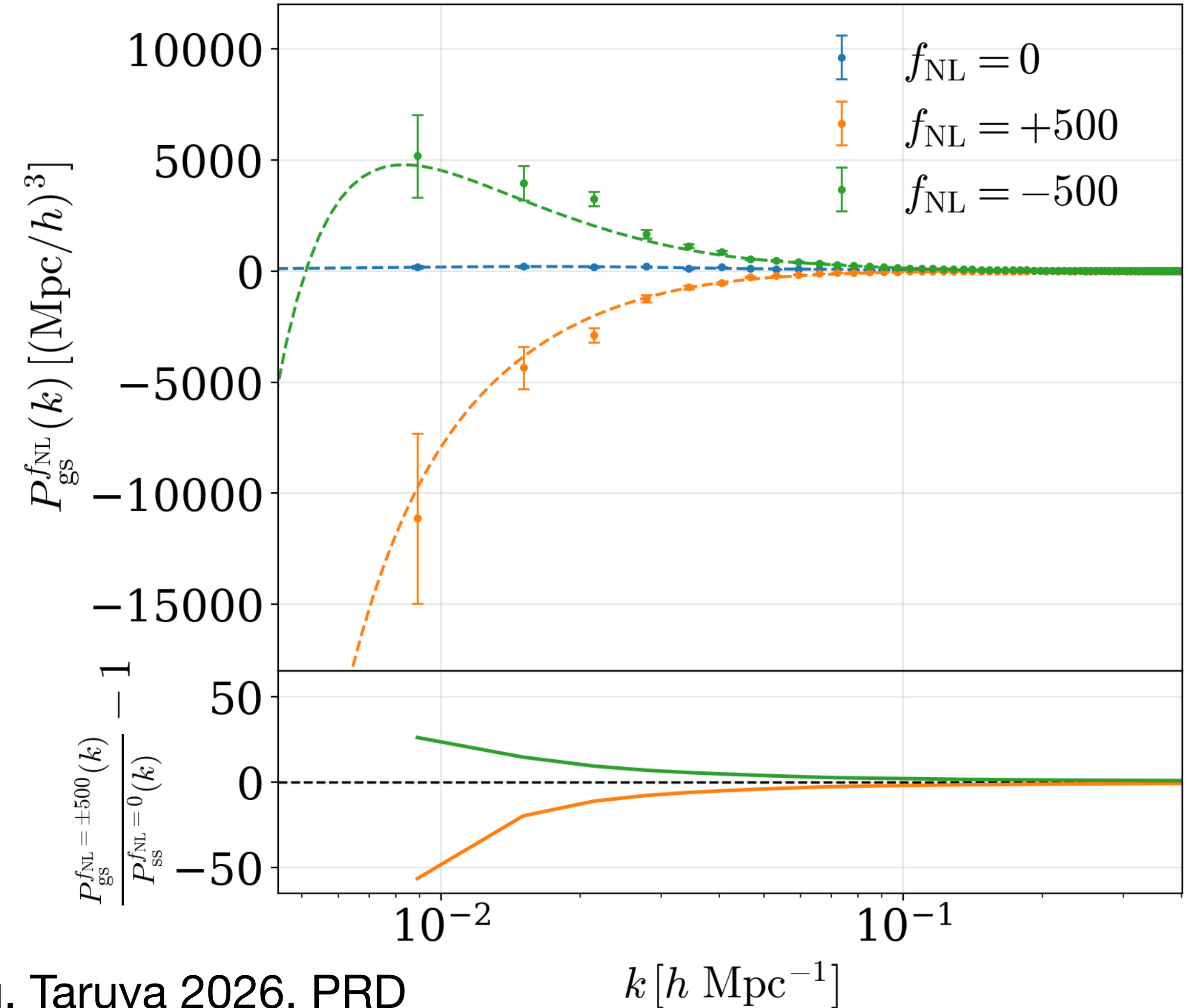
New data challenges!

Galaxy sizes as a new statistics to constrain local PNG

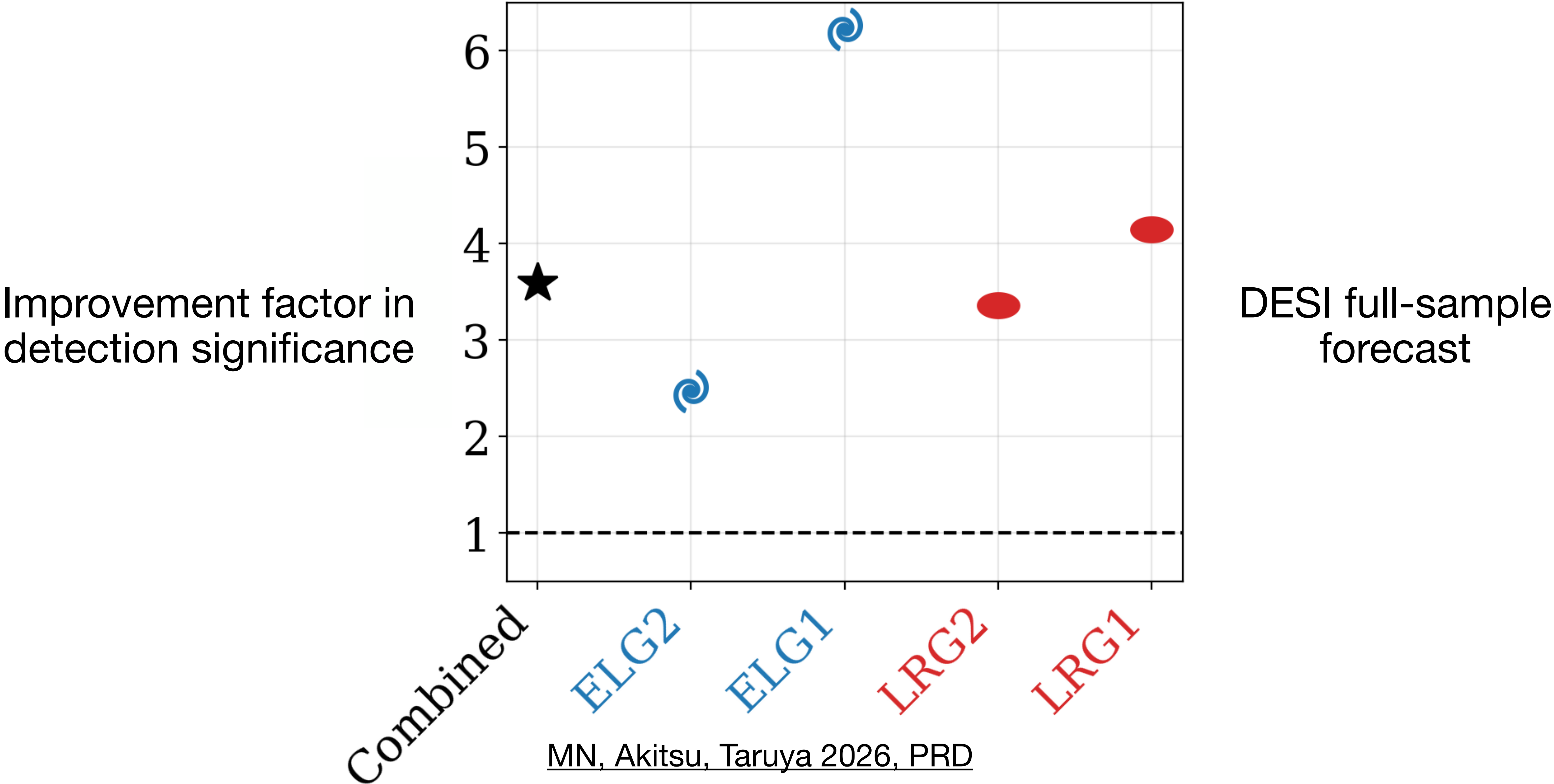
$$\Phi(\mathbf{x}) = \phi_G(\mathbf{x}) + f_{\text{NL}}^{\text{local}} \left[\phi_G^2(\mathbf{x}) - \langle \phi_G^2(\mathbf{x}) \rangle \right]$$



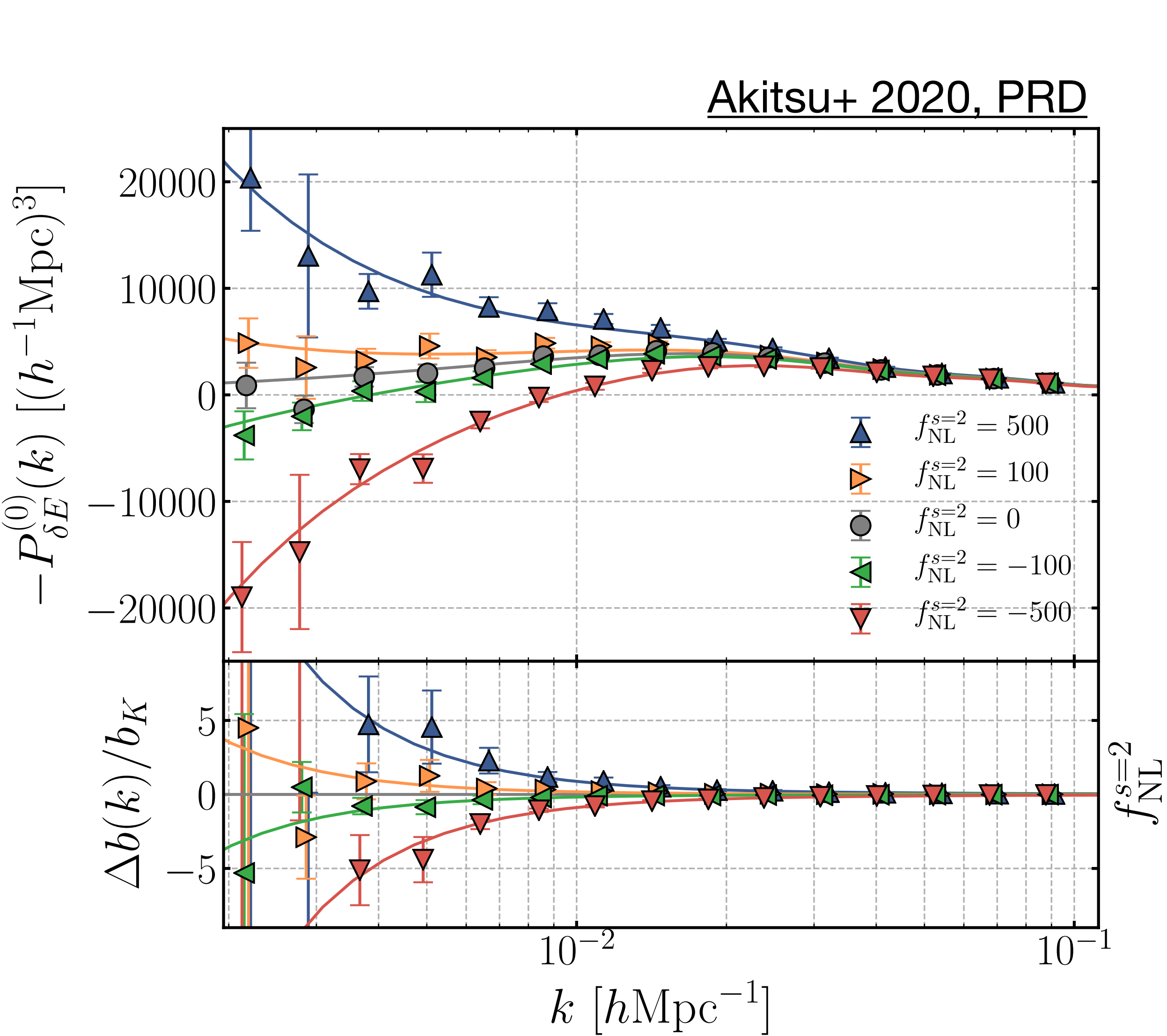
MN, Akitsu, Taruya 2026, PRD



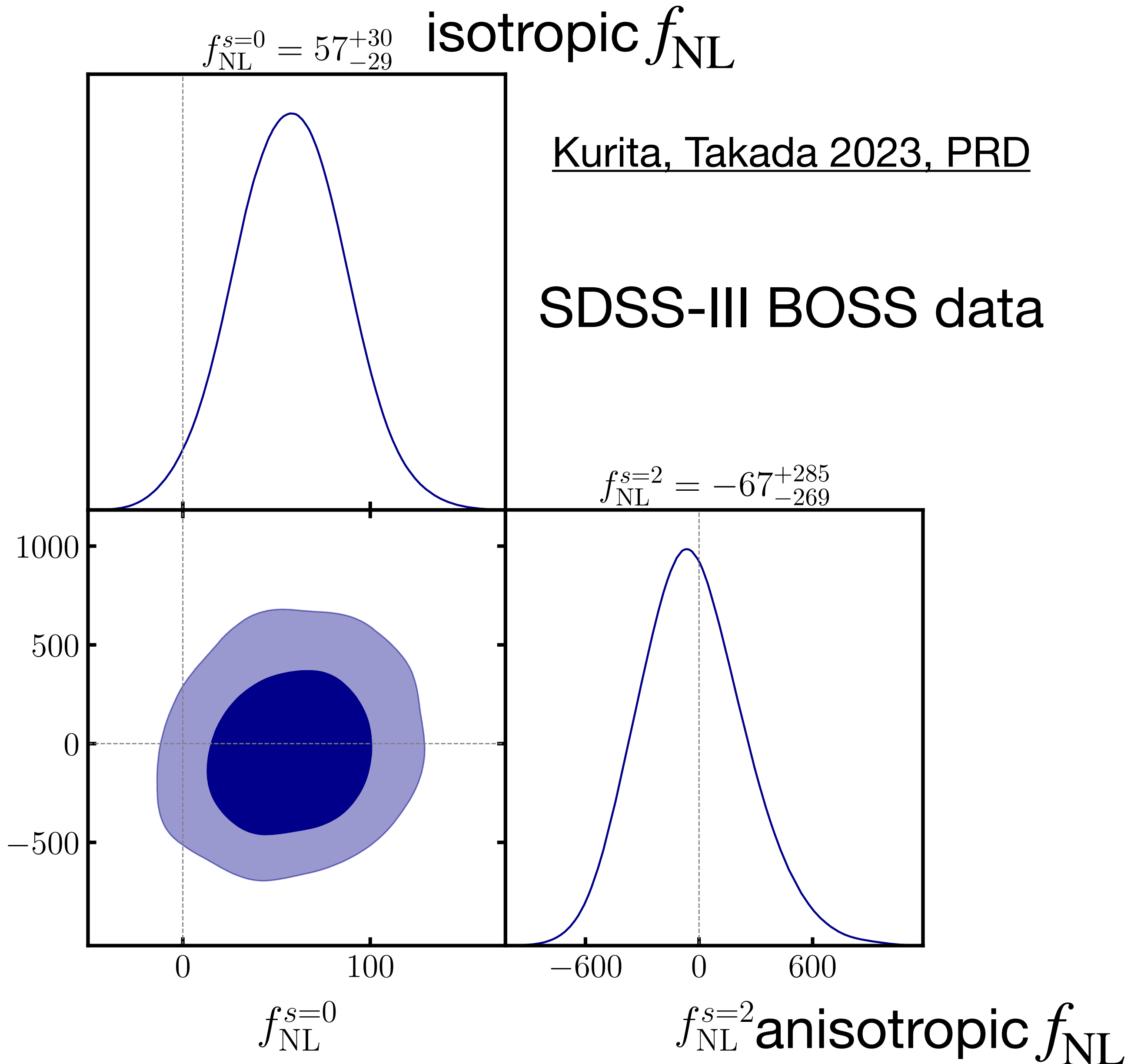
Galaxy sizes as a natural multitracer of local PNG



Galaxy shapes similarly probe *anisotropic* local PNG



High-resolution N-body simulation



The next era of LSS surveys and analysis

Precision tests of fundamental physics at cosmological scales

Search for new physics in both the late and early universe

New methods and statistics will maximize discovery potential

